



# 2<sup>nd</sup> INTERNATIONAL CONFERENCE ON COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017

20-22 May 2017, Istanbul, TURKEY

## ABSTRACT BOOK

**THE SECOND INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING  
SCIENCES (CMES-2017), ISTANBUL, 20-22 MAY 2017**

The Second International Conference on Computational Mathematics and Engineering Sciences (CMES-2017) will be held from May 20 to 22, 2017 in Istanbul, Turkey. It provides an ideal academic platform for researchers and professionals to discuss recent developments in both theoretical, applied mathematics and engineering sciences. This event aims also to stimulate interactions between researchers in the field of computational mathematics and their applications in science and engineering, to present the development reached in this areas, and to showcase the computational expertise of our invited speakers and participants.

The organizing Committee

©All Rights Reserved. No part of this book may be reproduced or utilized in any form or by any means, electronic or mechanical, including photocopying, recording, or by any information storage and retrieval system, without permission from the authors.

All kinds of information in this book is the responsibility of the authors.

**EDITORS**

*Zakia Hammouch*, FST Errachidia Moulay Ismail University, Morocco

*Hasan Bulut*, Firat University, Elazig, Turkey

**ASSISTANT EDITORS**

*Haci Mehmet Baskonus*, Munzur University, Tunceli, Turkey

*Emrah Yilmaz*, Firat University, Elazig, Turkey



## MESSAGE FROM THE GENERAL CHAIRS



Dear Conference Attendees,

We would like to welcome you to the **2nd International Conference on Computational Mathematics and Engineering Sciences (CMES-2017)** in Istanbul, Turkey. This year, the conference program includes 163 extended abstracts selected by the Program Committee from a number of 236 submissions received in response to the call for papers. The program features keynote talks by seven distinguished speakers: Kalyan Chakraborty of Harish Chandra Research Institute Allahabad, Necdet Bildik of Celal Bayar University, Abdellah Rababah of Jordan University, Rifat Colak of Firat University, Abdon Atangana of The Free State University, Dumitru Baleanu of Cankaya University, Devendra Kumar of Rajasthan University and Giri Debasis of Haldia Institute of Technology. The conference also includes contributed sessions, several posters and research highlights.

We would like to thank the Program Committee members and external reviewers for volunteering their time to review and discuss submitted abstracts. We would like to extend special thanks to the Honorary, Scientific and Organizing committees for their hard work in making CMES2017 a successful event. Last but not least we would like to thank all authors for presenting their work at the conference. We hope that you will find the CMES2017 technical program interesting and intellectually stimulating, and that you will enjoy meeting with and interacting with researchers from around the world.

*Zakia Hammouch*, FST Errachidia Moulay Ismail University Morocco.

*Hasan Bulut*, Firat University Elazig, Turkey.



## **TOPICS**

Applied Mathematics,  
Financial Mathematics,  
Control Theory,  
Game Theory  
Modeling of Bio-systems for Optimization and Control,  
Linear and Nonlinear programming and Dynamics,  
Artificial Intelligence,  
Geometry and Its Applications,  
Analysis and Its Applications,  
Statistics and Its Applications,  
Mathematics Education and Its Applications,  
Algebra and Its Applications.  
Engineering Sciences  
Computer Science  
Information technology  
Electrical and Electronic Engineering  
Ordinary, Partial, Stochastic and Delay Differential Equations  
Chaos and Dynamical Systems  
Numerical methods and scientific programming  
Fractional Calculus and Applications,  
Cryptography and its applications  
Computational Fluids mechanics, Heat and Mass Transfers.

## COMMITTEE CHAIRS

Zakia Hammouch, E3MI FST Errachidia Moulay Ismail University, Morocco

Hasan Bulut, Firat University Elazig, Turkey

## HONORARY COMMITTEE

Hassan Sahbi (President of Moulay Ismail University, Meknes, Morocco)

Kutbeddin Demirdag (Rector of Firat University, Elazig, Turkey)

Ahmet Ait Hou (Dean of FSTE Moulay Ismail University, Errachidia, Morocco)

Rifat Colak (Dean of Science Faculty, Firat University, Elazig, Turkey)

Abdelhadi El Ouali (Vice-President, Moulay Ismail University, Morocco)

Abdelaziz Raada (Vice-Dean of Research, FSTE, Moulay Ismail University, Morocco)

## SCIENTIFIC COMMITTEE

Claudio Rodrigo Cuevas Henriquez (Federal University of Pernambuco, Brazil)

Seenith Sivasundaram (Université de Bethune-Cookman, USA)

Abdon Atangana (University of the Free State, South Africa)

Abdullah Y. Öztoprak (Final International University, Girne, Cyprus)

Carlo Cattani (Tuscia University, Viterbo, Italy)

Armando Ciancio (University of Messina, Italy)

Christos Volos (Aristotle University, Greece)

Luis Manuel Sánchez Ruiz (Technical University of Valencia, Spain)

Ekrem Savas (Istanbul Ticaret University, Turkey)

Yury Luchko (Beuth Hochschule für Technik Berlin, Germany)

Michael Ruzhansky (Imperial College London, England)

Anna Sandulyak (Université de Moscow, Russia)

Robert Tchitnga (Dshang University, Cameroon)

Shilpi Jain (Poornima College of Engineering, India)

Etiyar Penahlı (Bakû State University, Bakû, Azerbaijan)

Eva Kaslik (University of Timisoara, Romania)

Dumitru Baleanu (Cankaya University, Turkey)

Ozlem Defterli (Cankaya University, Turkey)

Hamed Daei Kasmaei (Islamic Azad University of Tehran, Iran)

Nabil Gmati (Ecole National des Ingénieurs de Tunis, Tunisia)

Moncef Mahjoub (Ecole National des Ingénieurs de Tunis, Tunisia)

Fethi Bin Muhammad Belgacem (PAAET, Kuwait)

Abdellah Rababah (University of Science and Technology Irbid, Jordan)

Fahrettin Muhtarov (Bakû State University Bakû, Azerbaijan)

Kalyan Chakraborty (Harish-Chandra Research Institute, India)

Praveen Agarwal (ANAND International College of Engineers Jaipur, India)

Jagdev Singh (JECRC University, Jaipur, India)

S. G. Ahmed (Zagazig University, Zagazig, Egypt)

Ji-Huan He (Soochow University, Suzhou, China)

Xiao-Jun Yang (University of Mining and Technology, China)

Izhar Uddin (Jamia Milia Islamia, India)

Ebenezer Bonyah (Kumasi Polytechnic Institute, Ghana)

Erkinjon Tulkinovich Karimov (Sultan Qaboos University, Oman)



**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

Yusif Gasimov (Baku State University, Baku, Azerbaijan)  
Necdet Bildik (Celal Bayar University, Manisa, Turkey)  
Murat Sarı (Yıldız Technical University, Turkey)  
Fikret Aliev (Azerbaijan State University, Azerbaijan)  
Rizwan Ul Haq (Bahria University, Pakistan)  
Dogan Kaya (Istanbul Commerce University, Turkey)  
Yasar Bolat (Kastamonu University, Turkey)  
Ettaouil Mohamed (Sidi Mohamed Ben Abdellah University)  
Mehmet Zeki Sarıkaya (Duzce University, Turkey)  
Sunil Purohit (Maharana Pratap University, India)  
Ömer Akın (TOBB ETU University Ankara, Turkey)  
Duygu Dönmez Demir (Celal Bayar University, Turkey)  
Alaattin Esen (Inonu University Malatya, Turkey)  
Zakia Hammouch (FSTE, Moulay Ismail University, Morocco)  
Malika Ait Ben Haddou (Moulay Ismail University, Morocco)  
Toufik Mekkaoui (Université Moulay Ismail, Errachidia, Morocco)  
Said Agoujil (FSTE, Moulay Ismail University, Morocco)  
Youssef Qaraai (FSTE, Moulay Ismail University, Morocco)  
Moha Hajar (FSTE, Moulay Ismail University, Morocco)  
El Hassan El Kinani (ENSAM Moulay Ismail University, Morocco)  
Omar Eloutassi (FSTE, Moulay Ismail University, Morocco)  
Mabrouk Ben Hammou (Moulay Ismail University, Morocco)  
Elhoussine Azroul (Sidi Mohamed Ben Abdellah University, Fes, Morocco)  
Ettaouil Mohamed (Sidi Mohamed Ben Abdellah University, Fes, Morocco)  
Mrani Driss (Moulay Ismail University, Morocco)  
Lachgar Mohammed (FSTE, Moulay Ismail University, Morocco)  
Mama Foupoyagnigni (University of Yaounde I AIMS, Cameroon)  
İdris Dag (Eskisehir Osmangazi University, Eskisehir, Turkey)

Cigdem Bektas (Firat University, Elazig, Turkey)  
Huseyin Demir (Ondokuz Mayıs University, Turkey)  
Halim Özdemir (Sakarya University, Turkey)  
Anum Shafiq (Preston University Kohat Islamabad, Pakistan)  
Murat Subasi (Atatürk University, Erzurum, Turkey)  
Huseyin Bereketoglu (Ankara University, Turkey)  
Emine Misirli (Ege University İzmir, Turkey)  
Hasan Bulut (Firat University Elazig, Turkey)  
Necati Ozdemir (Balıkesir University, Turkey)  
Fevzi Erdogan (Yüzüncü Yil University, Turkey)  
Mehar Chand (Guru Kashi University, Talwandi Sabo-Bathinda, India)  
Oktay Muhtaroglu (Gaziosmanpasa University, Turkey)  
Ercan Celik (Ataturk University Erzurum, Turkey)  
Heybetkulu Mustafayev (Yüzüncü Yil University, Turkey)  
Cemil Tunc (Yüzüncü Yil University Van, Turkey)  
Baki Koyuncu (Final International University, Cyprus)  
Elgiz Bayram (Ankara University, Turkey)  
Nuri Ozalp (Ankara University, Turkey)  
Okay Celebi (Yeditepe University, Turkey)  
Yusuf Pandir (Bozok University Yozgat, Turkey)  
Zeynep Fidan Kocak (Mugla Sıtkı Kocman University, Turkey)  
Selçuk Kutluay (Inonu University, Turkey)  
Rifat Çolak (Firat University, Elazig, Turkey)  
Mikail Et (Firat University, Elazig, Turkey)  
Mehmet Bektas (Firat University, Elazig, Turkey)  
Vedat Asil (Firat University, Elazig, Turkey)  
Onur Alp İlhan (Erciyes University, Kayseri, Turkey)  
Adnan Khashman (Final International University, Girne, Cyprus)  
Onur Kıymaz (Ahi Evran University, Kirsehir, Turkey)  
Haci Mehmet Baskonus (Munzur University, Turkey)  
Devendra Kumar (JECRC University Jaipur, India)  
Elcin Yusufoglu (Usak University, Usak, Turkey)  
Yusuf Gurefe (Usak University, Usak, Turkey) Hasan Hüseyin Sayan (Gazi University, Ankara, Turkey)  
Asif Yokus (Firat University, Elazig, Turkey)  
Nesrin Ozsoy (Adnan Menderes University, Turkey)  
Necdet Çatalbaş (Firat University, Elazig, Turkey)



**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

Erdal Bas (Firat University, Elazig, Turkey)  
Muharrem Tuncay Gencoglu (Firat University, Turkey)  
Danyal Soybas (Erciyes University, Turkey)  
Mehmet Giyas Sakar (Yüzüncü Yil University, Van, Turkey)  
Hakan F. Oztop (Firat University, Elazig, Turkey)  
Mehmet Karay (Final International University, Girne, Cyprus)  
Ramazan Yaman (Balıkesir University, Turkey)  
Unal Ic (Firat University, Elazig, Turkey)  
Daniele Ritelli (University of Bologna, Bologna, Italy)  
Fatma Ayaz (Gazi University, Ankara, Turkey)  
Hikmet Kemaloglu (Firat University, Elazig, Turkey)  
Hıfı Altınok (Firat University, Elazig, Turkey)  
Gülnur Yel (Final International University, Cyprus)  
Mahmut Isik (Harran University, Turkey)  
Yavuz Altın (Firat University, Elazig, Turkey)  
Basak Karpuz (Dokuz Eylül University, İzmir, Turkey)  
Kemal Aydın (Selcuk University, Konya, Turkey)  
Murat Sat (Erzincan University, Erzincan, Turkey)  
Sinan Calik (Firat University, Elazig, Turkey)

Delfim F.M. Torres (University of Aveiro, Aveiro, Portugal)  
Resat Yilmazer, Firat University, Turkey  
Gülden Altay, Firat University, Turkey  
Aysegül Gokhan (Firat University, Elazig, Turkey)  
Cengiz Cinar (Gazi University, Ankara, Turkey)  
Ibrahim Yalcinkaya (Necmettin Erbakan University, Konya, Turkey)  
Nejla Gurefe (Usak University, Usak, Turkey)  
Oleksandr Berezko (Lviv Polytechnic National University, Lviv, Ukraine)  
Ali Karci (Inonu University, Malatya, Turkey)  
Cem Onat (Inonu University, Malatya, Turkey)  
Figen Ozpinar (Afyon Kocatepe University, Turkey)  
Muhsin Gencoglu (Firat University, Elazig, Turkey)  
Aysegül Ucar (Firat University, Elazig, Turkey)  
Resul Coteli (Firat University, Elazig, Turkey)  
Engin Avci (Firat University, Elazig, Turkey)  
Lachgar MohamedMy Ahmed (Moulay Ismail University, Morocco)

**ORGANIZING COMMITTEE**

Zakia Hammouch (Chair), E3MI FST Errachidia Moulay Ismail University, Morocco  
Hasan Bulut (Chair), Firat University, Turkey  
Haci Mehmet Baskonus (Co-Chair), Munzur University, Turkey  
Toufik Mekkaoui (Co-Chair), E3MI FST Errachidia Moulay Ismail University, Morocco  
Said Agoujil, E3MI FST Errachidia Moulay Ismail University, Morocco  
Youssef Qaraai, E3MI FST Errachidia Moulay Ismail University, Morocco



## LOCAL COMMITTEE

Mehmet Bektaş, Firat University, Turkey  
Hikmet Kemaloglu, Firat University, Turkey  
Resat Yilmazer, Firat University, Turkey  
Erdal Bas, Firat University, Turkey  
Yavuz Altın, Firat University, Turkey  
Munevver Tuz, Firat University, Turkey  
Ibrahim Enam Inan, Firat University, Turkey  
Tugba Yazgan, Firat University, Turkey

Emrah Yilmaz, Firat University, Turkey  
Asif Yokus, Firat University, Turkey  
Tolga Akturk, Ordu University, Turkey  
Tukur Abdulkadir Sulaiman, Firat  
University, Turkey  
Aysenur Akkilic, Firat University, Turkey  
Dilek Gunaydin, Firat University, Turkey

## PROCEEDINGS

Extended abstracts will be published in some Special Volumes of eight journals. Procedure, Guidelines and Checklist for the preparation and submission of a paper for the Proceedings of CMES-2017 can be found in the journals websites. The journals in which selected and peer-reviewed full papers of CMES-2017 will be published are:

**1. ITM Web of Conferences, (Web of Science, SCI-E)**

(Editor in Chief: Prof. Isaline AUGUSTO)  
<http://www.itm-conferences.org/>

**2. An International Journal of Optimization and Control: Theories & Applications (IJOCTA) (ULAKBIM)**

(Editor in Chief: Prof. Ramazan YAMAN)  
(Editor in Field : Prof. Necati OZDEMIR)  
<http://ijocta.balikesir.edu.tr/index.php/files>

**3. Non. Sci. Letters A, (It will be submitted for possible inclusion in SCI)**

(Editor in Chief: Prof. Ji-Huan HE)  
[http://www.nonlinearscience.com/journal\\_2076-2275.php](http://www.nonlinearscience.com/journal_2076-2275.php)

**4. Mathematics in Natural Science (MNS)**

(Editor in Chief: Prof. Abdon ATANGANA)  
<http://www.isr-publications.com/mns>

**5. International eJournal of Engineering Mathematics: Theory and Application**

(Editor in Chief: Prof. S.G. AHMET and Prof. Hamed DAEI KASMAEI)  
<http://iejemta.com/>

**6. Journal of Modern Technology and Engineering**

(Editor in Chief: Prof. Mutallimov Mutallim)

<http://jomardpublishing.com/journals.aspx?id=1>

**7. Hydrology**

(Editor in Chief: Prof. Abdon ATANGANA)  
[http://www.mdpi.com/journal/hydrology/special\\_issues/groundwater\\_flow](http://www.mdpi.com/journal/hydrology/special_issues/groundwater_flow)

**8. Mathematics in Engineering, Science and Aerospace (MESA)**

(Editor in Chief: Seenith Sivasundaram)  
<http://nonlinearstudies.com/index.php/ mesa/index>





## TABLE OF CONTENTS

### PLENARY AND INVITED SPEAKERS

AUTHOR	TITLE OF THE TALK	PAGE
Kalyan Chakraborty	CLASS NUMBERS OF CERTAIN QUADRATIC FIELDS	I
Abdon Atangana	FRACTAL-FRACTIONAL DIFFERENTIATION AND INTEGRATION	II
Necdet Bildik	A PRACTICAL METHOD FOR ANALYTICAL EVALUATION OF APPROXIMATE SOLUTIONS OF PARTIAL DIFFERENTIAL EQUATIONS	III
Rifat Çolak	STATISTICAL CONVERGENCE OF ORDER $\alpha$ AND STATISTICAL BOUNDEDNES OF ORDER $\alpha$ IN METRIC SPACES	IV
Dumitru Baleanu	ADVANCES IN DISCRETE FRACTIONAL CALCULUS: THEORY AND APPLICATIONS	V
Abedallah Rababah	MULTI-DEGREE REDUCTION OF SAID-BALL CURVES WITH ENDPPOINTS CONSTRAINTS	VI
Debasis Giri	THREE FOLD SECURITY IN REMOTE USER AUTHENTICATION PROTOCOLS	VII
Devendra Kumar	ANALYTICAL STUDY FOR NONLINEAR FRACTIONAL DIFFERENTIAL EQUATIONS	VIII

**PROCEEDINGS**

M.B. Riaz	ANALYTIC SOLUTIONS OF OLDROYD-B FLUID WITH FRACTIONAL DERIVATIVES IN A CIRCULAR DUCT DUE TO TENSION ON THE BOUNDARY	1
Abdelazize Raada, Driss Mrani, Rizwan Ul Haq	SIMULATION OF WATER-BASED MAGNETITE NANOPARTICLES BETWEEN TWO PARALLEL SURFACES WITH SUCTION/INJECTION	2
Agoujil Said	A NOTE ON A NUMERICAL METHOD FOR SYMMETRIC HAMILTONIAN MATRICES	3
Mohamed Mbehou	NUMERICAL METHODS OF A MIXED PROBLEM FOR A NONLINEAR KIRCHHOFF MODEL WITH MOVING BOUNDARY	4
Meriem Henkouche	M.L.E SPEED OF CONVERGENCE IN NONLINEAR AUTOREGRESSIVE PROCESSES	5
Ernesto Liñán-García, Juan Frausto-Solís, Norma Dominguez-Sarabia, Francisco Hernández-Rodríguez	SIMULATED ANNEALING HYBRIDIZED WITH DYNAMIC PROGRAMMING APPLIED TO SOLVE THE SEQUENCE ALIGNMENT PROBLEM	6
Abdellah Mamouni	COMMUTATIVITY THEOREMS IN RINGS WITH INVOLUTION: A SURVEY	7
Haci Mehmet Baskonus, Tukur Abdulkadir Sulaiman, Hasan Bulut	NEW SOLITARY WAVE SOLUTIONS TO THE (2+1)-DIMENSIONAL CALOGERO-BOGOYAVLENSKII-SCHI AND THE KADOMTSEV-PETVIASHVILI HIERARCHY EQUATIONS	8
Sanae Kouismi	A SCHEDULING PROBLEM FOR UNLOADING OPERATIONS INCONTAINER TERMINAL	9
Hicham Moussa, Francisco Ortegón Gallego, Mohamed Rhoudaf	CAPACITY SOLUTION TO A NONLINEAR ELLIPTIC COUPLED SYSTEM IN ORLICZ-SOBOLEV SPACES	10
Hamdi Houichet, Maher Moakher, Badreddine Rjaibi, Anis Theljani	A NONSTANDARD HIGHER-ORDER PDE FOR EDGE DETECTION IN MEDICAL IMAGING PROBLEMS	11
Triloki Nath, L.P. Singh	EXACT SOLUTION OF THE BLAST WAVE PROBLEM IN DUSTY GAS	12
Shashi Kant, Santwana Mukhopadhyay	AN INVESTIGATION ON A TWO DIMENSIONAL PROBLEM OF MODE-I CRACK UNDER AN EXACT HEAT CONDUCTION WITH A DELAY	13
Murat Sari, Huseyin Tunc	DISCUSSION OF ADVECTION-DIFFUSION PROCESS IN FINITE ELEMENT TECHNIQUES	14
Soumia Saidi	EVOLUTION PROBLEM GOVERNED BY THE SUBDIFFERENTIAL OPERATOR WITH DELAY	15

**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

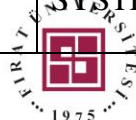
Muharrem Tuncay GENÇOĞLU	COMBINING CRYPTOGRAPHY WITH STEGANOGRAPHY	16
Sebahat Yetim Karaca, Özgür Altoğ	MISTAKES AND MISCONCEPTION ABOUT “ZERO” IN SOME TOPICS OF MATHEMATICS FOR 8TH GRADERS IN YENIMAHALLE, ANKARA	17
Gülnur Yel, Zeynep Fidan Koçak	ON THE EXACT SOLUTIONS OF THE FRACTIONAL (2+1)- DIMENSIONAL DAVEY- STEWARTSON EQUATION SYSTEM	18
Fouad Essahlaoui Ahmed ElAbbassi, Rachid Skouri	EMULATE ARTIFICIAL NEURAL NETWORK TO MAKE A DECISION IN WIRELESS SENSOR	19
Cem Onat, Mahmut Daskin Abdullah Turan	GAIN SCHEDULING LINEAR MODEL OF AN ELECTRO-HYDRAULIC ACTUATOR	20
Valery Antonov, Roman Davidov, Nikolay Kalinin, Alexey Rjahovski	MATHEMATICAL MODELING OF THE SYNTHESIS OF NEW MATERIALS	21
Obaid Algahtani	A NEW APPROACH TO INTERVAL MATHEMATICAL MODEL AND APPLICATIONS	22
Emine Nesligül Aksan, Hasan Bulut, Miraç Kayhan	SOME WAVE SIMULATION PROPERTIES OF THE (2+1) DIMENSIONAL BREAKING SOLUTION EQUATION	23
Adewale F. Lukman, Kayode Ayinde	REVIEW AND CLASSIFICATIONS OF THE RIDGE PARAMETER ESTIMATION TECHNIQUES	24
Samet KOYUNCU, Gökhan BAHADIR	INVESTIGATION OF INDUCTION MOTORS MEDIUM VOLTAGE GRID CONNECTED POWER SYSTEM STABILITY ANALYSIS	25
Selmahan Selim, Gozde Elver, Murat Sari	NUMERICAL BEHAVIOR OF SINGULAR TWO- POINT BOUNDARY VALUE PROBLEMS IN A COMPARATIVE WAY	26
Ammar Touati Brahim, Madjid Kidouche	ROBUST SPEED OBSERVER FOR MECHANICAL SYSTEMS WITH NON-HOLONOMIC CONSTRAINTS	27
Hande Uslu, Murat Sari	SOLUTIONS OF DIFFERENTIAL EQUATIONS THROUGH MONTE CARLO ALGORITHMS	28
Gökhan BAHADIR, Samet KOYUNCU	TRANSIENT ANALYSIS WITH THE FOUR-STEP RUNGE-KUTTA METHOD OF INDUCTION MOTOR WITH MATLAB	29
P. K. Mishra, S. Das	ELASTO-DYNAMIC RESPONSE OF CRACKED INFINITE ORTHOTROPIC ELASTIC STRIP UNDER IMPACT LOADING CONDITIONS	30
R. K. Gupta, L. P. Singh	SIMULATION OF TWO DIMENSIONAL SHALLOW WATER EQUATIONS WITH VARIABLE BOTTOM GEOMETRY USING FORCE METHOD	31
M. Rhoudaf, H. Sabiki	ON A NONLINEAR EIGENVALUE PROBLEM IN MUSIELAK-ORLICZ SPACES	32

**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

M.Tuncay Gençoğlu	CRYPTANALYSIS OF APPLICATION OF LAPLACE TRANSFORM FOR CRYPTOGRAPHY	33
Necdet Bildik, Sinan Deniz,	A NEW RELIABLE TREATMENT OF THE LANE-EMDEN TYPE EQUATIONS	34
Mehar Chand, Zakia Hammouch, Joshua Kiddy K. Asamoah	CERTAIN FRACTIONAL INTEGRALS AND SOLUTIONS OF FRACTIONAL KINETIC EQUATIONS INVOLVING THE PRODUCT OF S-FUNCTION	35
Zehra Pınar	COMBINATION OF LIE TRANSFORMATIONS AND AUXILIARY EQUATION METHOD FOR A CLASS OF NEW KDV-BURGERS-KURAMOTO TYPE EQUATION	36
Ozlem Defterli	HIDDEN SYMMETRIES WITHIN SOME NEW DERIVATIVES	37
Erdal Bas, Ramazan Ozarslan	A NOTE ON STURM-LIOUVILLE PROBLEM FOR DIFFERENCE EQUATIONS	38
Hasan Bulut, Tukur Abdulkadir Sulaiman, Haci Mehmet Baskonus, Tugba Yazgan	NOVEL HYPERBOLIC BEHAVIORS TO SOME IMPORTANT MODELS ARISING IN QUANTUM SCIENCE	39
Mikail Et	GENERALIZED CESÀRO SUMMABLE DIFFERENCE SEQUENCE SPACES AND THEIR DUAL SPACES	40
ZeynepFidan Koçak, Gülnur Yel	TRIGONOMETRIC FUNCTION SOLUTIONS OF FRACTIONAL DRINFELD'S SOKOLOV -WILSON SYSTEM	41
Erdal Bas, Funda Metin Turk	FRACTIONAL PROBLEM FOR DIFFUSION OPERATOR WITH IMPUSIVE CONDITION	42
Mehmet Karay	MODELING DISTRIBUTED WORKFLOW PROCESSES USING EXTENDED PETRI NETS	43
Yusuf Ali Tandogan, Yusuf Pandir	NEW MULTIPLE SOLITON SOLUTIONS OF MODIFIED KDV-KP EQUATION	44
Sinan Deniz, Necdet Bildik	OPTIMAL PERTURBATION ITERATION METHOD FOR SOLVING DELAY DIFFERENTIAL EQUATIONS	45
Latife Gizem Kambur, Yusuf Gurefe	AN APPLICATION OF WEIERSTRASS TRANSFORMATION METHOD TO SOME NONLINEAR PHYSICAL PROBLEMS	46
A. Amrane, A. Larabi, M.S.Boucherit	SPEED SENSORLESS VECTOR CONTROL WITH A STRATEGY OF LINEARIZATION BY STATE FEEDBACK OF INDUCTION MOTOR APPLIED MODEL REFERENCE ADAPTIVE SYSTEM	47
Tugcem Partal, Mustafa Bayram	STOCHASTIC RUNGE-KUTTA METHODS IN A GOMPERTZIAN STOCHASTIC MODEL	48
Rabar Mohammed Rasul, Hasan Bulut	TAN (F(xi)/2) -EXPANSION METHOD FOR EXACT SOLUTIONS OF THE (2+1)-DIMENSIONAL POTENTIAL CALOGERO-BOGOYAVLENSKII-SCHIFF EQUATION	49

**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

Hıfı Altınok, Damla Barlak	ON LACUNARY STATISTICAL CONVERGENCE OF ORDER $\beta$ FOR SEQUENCES OF FUZZY NUMBERS	50
Basant K. Jha, Muhammad L. Kaurangini	UNSTEADY FREE-CONVECTIVE EXOTHERMIC FLUID FLOW IN VERTICAL CHANNEL FILLED WITH POROUS MATERIAL	51
M. Jabha, A. Elalaoui, A. Jarid	THEORETICAL STUDY OF THE ELECTRON AND PHOTOVOLTAIC PROPERTIES OF CARBAZOLE-BASED OLIGOMERS	52
Rizwan Ul Haq	INFLUENCE OF ALIGNED MAGNETIC FIELD AND CNTS IN TWO DIFFERENT BASE FLUIDS OVER A MOVING SURFACE WITH SLIP EFFECTS	53
M. Ramzan, M. Bilal	FLOW OF UNSTEADY SECONG GRADE NANOFLUID PAST A PERMEABLE SURFACE	54
Onur Alp Ilhan, Tukur Abdulkadir Sulaiman, Hasan Bulut	ON THE NEW SOLUTIONS OF (3+1)- DIMENSIONAL MODIFIED KDV-ZAKHAROV- KUZNETSEV EQUATION	55
Figen Özpınar, Fethi Bin Muhammed Belgacem	THE DISCRETE HOMOTOPY PERTURBATION SUMUDU TRANSFORM METHOD FOR SOLVING PARTIAL DIFFERENCE EQUATIONS	56
Erdem Isik, Hasan Bulut, Sibel Sehriban Atas	SOME PROTOTYPE RESULTS OF THE SYMMETRIC REGULARIZED LONG WAVE EQUATION ARISING IN NONLINEAR ION ACOUSTIC WAVES	57
Z. El Malki, M. Bouachrine, M. Hamidi, F. Serein-Spirau, J. P. Lère-Porte, J. Marc Sotiropoulos	A NEW DONOR- $\pi$ -ACCEPTOR COMPOUNDS BASED ON CARBAZOLE, THIOPHENE AND BENZOTHIADIAZOLE FOR PHOTOVOLTAIC APPLICATION AS DYE-SENSITIZED SOLAR CELLS: THEORETICAL STUDY	58
M. Benhamou, H. Kaidi	EFFECTIVE PAIR-POTENTIAL BETWEEN DROPLETS WITH END-GRAFTED POLYMERS WITHIN PICKERING EMULSIONS VERSUS GRAFTING-DENSITY, SOLVENT QUALITY AND MONOMER CONCENTRATION	59
M.H Aabidi, C. Baidada, B. El Mahi, A.Jakimi, Hany Ammar	BENEFITS OF REVERSE ENGINEERING TECHNOLOGIES IN SOFTWARE DEVELOPMENT MAKERSPACE	60
E. H. El Kinani, A. Ouhadan	INVARIANT SUBSPACE METHOD: APPLICATION TO NONLINEAR DISPERSIVE EQUATION WITH TIME- CAPUTO-FABRIZIO FRACTIONAL DERIVATIVE	61
Duygu Dönmez Demir, Aylin Zeybek	THE NUMERICAL SOLUTION OF FRACTIONAL BRATU-TYPE DIFFERENTIAL EQUATIONS	62
ElOutassi Omar, ElHajrat Nourddne, Zouine Younes	INCREASING THE CAPACITY OF O-MIMO SYSTEMS USING MGDm TECHNIQUE	63



**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

Fatih Selimefendigil, Hakan F. Öztop	MHD MIXED CONVECTION IN A LID-DRIVEN TRIANGULAR CAVITY FOR VARIOUS ELECTRICAL CONDUCTIVITY MODELS	64
Gülşen OrucovaBüyükoğ, Mustafa Bayram	NUMERICAL SOLUTIONS OF VECTOR STOCHASTIC DIFFERENTIAL EQUATIONS	65
Dilara Altan Koç, MustafaGülsu	NUMERICAL APPROACH FOR SOLVING TIME FRACTIONAL DIFFUSION EQUATION	66
Mbarki Wajih Aouadi Saloua Zemzemi Nejib	STABILITY ANALYSIS OF DECOUPLED TIME-STEPPING SCHEMES FOR THE SPECIALIZED CONDUCTION SYSTEM/MYOCARDIUM COUPLED PROBLEM IN CARDIOLOGY	67
Esen Ersoy, Emine Şendurur, İsmail Çetin	THE CREATIVITY DIMENSION OF INSTRUCTIONAL MATERIALS DESIGNED BY PROSPECTIVE TEACHERS: THE COMPARISON ACROSS DOMAINS	68
Fahim Mohamed, Jakimi Abdeslam, ElBermi Lahcen, E. H. El Kinani	PERSONALIZATION OF LEARNING SITUATIONS WITHIN A VIRTUAL ENVIRONMENT FOR TRAINING BASED ON FUZZY CLUSTERING	69
Hacene Chaouche Soumeya, Mohamed Dalah	THE WEAK SOLUTION OF ANTIPLANE ELECTRO-VISCOELASTIC CONTACT PROBLEM WITH REGULARIZED FRICTION LAW	70
Belgin Bal-İncebacak, Esen Ersoy	DEVELOPING AN ACHIEVEMENT TEST FOR FRACTION TEACHING: VALIDITY AND RELIABILITY ANALYSIS	71
Esen Ersoy, Belgin Bal-İncebacak	THE EVALUATION OF THE PROBLEM SOLVING IN MATHEMATICS COURSE ACCORDING TO STUDENT VIEWS	72
Esen Ersoy, Belgin Bal-İncebacak	PISA QUESTION AND REASONING SKILL	73
Vitaliy Pronin, Petr Shkatov, Anna Sandulyak, Haci Mehmet Baskonus	TECHNOLOGIES OF A CONTINUOUS ULTRASONIC THICKNESS MEASURING	74
Anna Sandulyak, Alexander Sandulyak, Maria PolismakovaDarya Sandulyak	TWO-EXPONENTIAL MODEL MAGNETIC CONTROL OF FERROIMPURITIES IN VARIOUS ENVIRONMENTS	75
Petr Shkatov, Irina Lisitsyna, Anna Sandulyak, Hasan Bulut	MEASUREMENT OF DEPTH OF CLOSE LOCATED SUPERFICIAL CRACKS BY ELECTROPOTENTIAL METHOD	76
Debasis Giri, Tanmoy Maitra	A THREE FACTOR REMOTE USER AUTHENTICATION SCHEME USING COLLISION RESIST FUZZY EXTRACTOR IN SINGLE SERVER ENVIRONMENT	77



**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

Ozlem Isik, Ozge Irmak Degirmenci, Hasan Bulut	CLASSIFICATIONS ON THE TRAVELLING WAVE SOLUTIONS TO THE (3+1)- DIMENSIONAL GENERALIZED KP AND JIMBO- MIWA EQUATIONS	78
Cem Onat, Mahmut Daskin Abdullah Turan	GAIN SCHEDULING PI CONTROL OF AN ELECTRO-HYDRAULIC ACTUATOR FOR ACTIVE SUSPENSION SYSTEMS	79
Ahu Ercan, Etibar S. Panakhov	HALF INVERSE PROBLEM FOR HILL'S EQUATION	80
Etibar Panakhov, Ahu Ercan	HALF INVERSE PROBLEM FOR A DISCONTINUOUS INTEGRO DIFFERENTIAL OPERATOR	81
Yusuf Gurefe, Tolga Akturk, Yusuf Pandir	NEW FUNCTION METHOD TO SOLVE THE ZHIBER-SHABAT EQUATION	82
Mustafa Ali Dokuyucu, Ercan Çelik	ANALYSIS OF KELLER-SEGEL MODEL WITH CAPUTO AND CAPUTO-FABRIZIO DERIVATIVES	83
Hasan Bulut, Betül Demirdağ, Haci Mehmet Baskonus	REGARDING ON THE NOVEL FORMS OF THE (3+1)-DIMENSIONAL KADOMTSEV- PETVIASHVILI EQUATION	84
Resat Yilmazer	DISCRETE FRACTIONAL SOLUTIONS OF A CHEBYSHEV EQUATION	85
Resat Yilmazer, Okkes Ozturk	AN APPLICATION OF THE NISHIMOTO'S OPERATOR FOR THE RADIAL SCHRODINGER EQUATION	86
Fatih Bulut, Ömer Oruç, Alaattin Esen	A 3-SCALE HAAR WAVELET COLLOCATION METHOD FOR SOLVING PDEs	87
S. Hussain, H. F. Oztop	DOUBLE DIFFUSIVE MIXED CONVECTION IN A NANOFLUID FILLED CONFINED CAVITY HEATED FROM BOTTOM WALL	88
Murat Sari, Arshed A. Ahmad, Lamyaa Almashhadani	CAPTURING THE BEHAVIOR OF ADVECTION- DIFFUSION PROCESS THROUGH MONTE CARLO SIMULATION	89
İnci ÇİLİNGİR SÜNGÜ	NUMERICAL INVESTIGATION ON MHD FLOW AND HEAT TRANSFER OVER AN EXPONENTIALLY STRETCHING SHEET WITH VISCOUS DISSIPATION AND RADIATION EFFECTS	90
Murat Sari, Eren Dincer	VARIOUS METHODS FOR THE BURGERS EQUATION	91
Çiğdem A. Bektaş, Sinan Ercan	ON SOME PROPERTIES OF SEQUENCE SPACES DEFINED BY A SEQUENCE OF MODULUS FUNCTION	92
Sinan Ercan, Çiğdem A. Bektaş	ON STATISTICAL CONVERGENCE OF SEQUENCES GENERATED BY THE DIFFERENCE OPERATOR OF FRACTIONAL ORDER	93



**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

Hasan Bulut, Hilal Arslanoglu Isik, Tukur Abdulkadir Sulaiman	ON SOME COMPLEX ASPECTS OF THE (2+1)- DIMENSIONAL BROER-KAUP-KUPERSHMITD SYSTEM	94
Recep Şahin, M. Baki Yağbasan, Ayşegül Çetinkaya, İ. Onur Kıymaz, Oğuz Yağcı	NEW GENERALIZATIONS OF EXTENDED GAMMA AND BETA FUNCTIONS	95
Oğuz Yağcı, Recep Şahin, M. Baki Yağbasan, Ayşegül Çetinkaya, İ. Onur Kıymaz	NEW GENERALIZATIONS OF GAUSS AND CONFLUENT HYPERGEOMETRIC FUNCTIONS	96
Ayşegül Çetinkaya, İ. Onur Kıymaz, Recep Şahin, M. Baki Yağbasan, Oğuz Yağcı	ON A NEW GENERALIZATION OF RIEMANN- LIOUVILLE FRACTIONAL DERIVATIVE OPERATOR	97
İ. Onur Kıymaz, Ayşegül Çetinkaya, M. Baki Yağbasan, Recep Şahin, Oğuz Yağcı	ON A NEW GENERALIZATION OF CAPUTO FRACTIONAL DERIVATIVE OPERATOR	98
Gülnur Yel, Haci Mehmet Baskonus, Hasan Bulut	NOVEL STRUCTURE TO THE COUPLED NONLINEAR MACCARI'S SYSTEM BY USING MODIFIED TRIAL EQUATION METHOD	99
Cemil Tunç	ON EXPONENTIAL STABILITY OF NONLINEAR VOLTERRA INTEGRO-DIFFERENTIAL EQUATIONS WITH CONSTANT TIME-LAG	100
Çiğdem Lazoğlu, İsmail Gür	ESTIMATION OF EARTHQUAKE PROBABILITIES WITH NON PARAMETRIC METHODS IN SEMI-MARKOV MODEL	101
Cemil Tunç, Osman Tunç	ON THE PROPERTIES OF SOLUTIONS TO NON- LINEAR VOLTERRA INTEGRO-DIFFERENTIAL EQUATIONS WITH MULTIPLE TIME-LAGS	102
Mehmet Gıyas Sakar, Fevzi Erdogan, Onur Saldır	NON-UNIFORM HAAR WAVELET METHOD FOR SINGULARLY PERTURBED CONVECTION- DIFFUSION EQUATIONS	103
Onur Saldır, Mehmet Gıyas Sakar, Fevzi Erdogan	LEGENDRE REPRODUCING KERNEL METHOD FOR FRACTIONAL TWO POINT BOUNDARY VALUE PROBLEM	104
Hasan Bulut, Sibel Sehriban Atas, Haci Mehmet Baskonus	SOME NOVEL EXPONENTIAL AND COMPLEX STRUCTURAL PROPERTIES OF THE FISHER EQUATION ARISING IN MATHEMATICAL BIOSCIENCE	105
N. Sotehi, W. Bouaffar	NUMERICAL STUDY OF CONVECTIVE DRYING OF POROUS MATERIAL	106



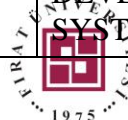
**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

Abdelghani Talhaoui, Imad Manssouri, Abdellah El Hmaidi	HYBRID METHODS COUPLING STATIONARY WAVELET TRANSFORM AND ARTIFICIAL NEURAL NETWORKS FOR THE CLASSIFICATION OF HERCYNIAN GRANITOIDS BASED ON THEIR GEOCHEMICAL CHARACTERISTICS: CASE OF AOULI PLUTON (HIGH MOULOYA, MOROCCO)	107
Bouchra Boudebouz, Imad Manssouri, Ahmed Mouchtachi	USE OF A HYBRID MODEL BASED ON ARTIFICIAL NEURAL NETWORKS-RBF COUPLED TO WAVELET DECOMPOSITION FOR THE CLASSIFICATION OF OPERATING MODES: CASE OF AN INDUSTRIAL INSTALLATION	108
Kaya Tubay, Erman Orhan, Aydın Sevinç, Yılmaz Ökkeş	THE PROTECTIVE EFFECTS OF GOLDENBERRY ( <i>Physalisperuviana</i> L.) EXTRACT AGAINST DESTRUCTIVE EFFECTS IN OF TYPE I DIABETES IN LIVER TISSUE OF RATS	109
Hüseyin Demir, Yücel Baltürk	ON NUMERICAL SOLUTION OF FRACTIONAL ORDER BOUNDARY VALUE PROBLEM WITH SHOOTING METHOD	110
Utku Erdoğan, Gabriel J. Lord	A FAMILY OF EFFICIENT TIME STEPPING METHODS FOR SEMI-LINEAR STOCHASTIC DIFFERENTIAL EQUATIONS	111
Hakkı Duru, Akbar Barati Chiyaneh	UNIFORM DIFFERENCE METHOD FOR SINGULARLY PERTURBED DELAY SOBOLEV PROBLEMS	112
Muaz Seydaoglu, Hüseyin Koçak, Utku Erdoğan	NUMERICAL INTEGRATION OF THE AIRY-TYPE EQUATIONS	113
Fevzi Erdogan, Mehmet Gıyas Sakar, Onur Saldır	HIGHER ORDER DIFFERENCE SCHEMES FOR SINGULARLY PERTURBED DIFFERENTIAL EQUATIONS WITH DELAY	114
Berat Karaağaç, N. Murat Yağmurlu, Alaattin ESEN	A STUDY ON THE IMPROVED $\tan\left(\phi(\xi)/2\right)$ -EXPANSION METHOD	115
Ozan Gül, Nusret Tan	ANALYSIS OF OUTPUT VOLTAGE HARMONICS OF VOLTAGE SOURCE INVERTER USED PI AND PID CONTROLLERS OPTIMIZED WITH ITAE PERFORMANCE CRITERIA	116
Mahmut Işık, Kübra Elif Akbaş	ON ASYMPTOTICALLY LACUNARY STATISTICAL EQUIVALENT OF ORDER A IN PROBABILITY	117
Keziban Taş, Etibar S. Panakhov	ON THE INVERSE PROBLEM FOR DIRAC SYSTEM	118
Gulistan Iskandarova, Dogan Kaya	SYMMETRY SOLUTION ON FRACTIONAL EQUATION	119
Berfin Elma, Emine Mısırlı	NEW EXACT WAVE SOLUTIONS OF SOME EVOLUTION EQUATIONS WITH FUNCTIONAL VARIABLE METHOD	120



**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

Gizel Bakıcıerler, Emine Mısırl	THE MODIFIED SIMPLE EQUATION METHOD FOR NEW EXACT WAVE SOLUTIONS OF SOME NONLINEAR PHYSICAL EQUATIONS	121
Asıf Yokus, Hasan Bulut	NUMERICAL SIMULATION OF KDV EQUATION BY FINITE DIFFERENCE METHOD	122
Djemaï Naimi, Ahmed Salhi, Ahboub Dihem	A MODIFIED ALGORITHM GENETIC APPLIED TO POWER SYSTEM OPTIMIZATION	123
Meryem Odabasi	ANALYTICAL SOLUTIONS OF THE CONFORMABLE FRACTIONAL DIFFERENTIAL EQUATIONS	124
Alaattin Esen, Ömer Oruç, Fatih Bulut	CHEBYSHEV WAVELET METHOD FOR NUMERICAL SOLUTIONS OF PDEs	125
Nejla Gürefe, Ceren Öncül, Hasan Es	INVESTIGATION OF NUMBER SENSE ACHIEVEMENTS ON SECONDARY SCHOOL STUDENTS ACCORDING TO VARIOUS VARIABLES	126
Nejla Gürefe	OPINIONS OF PROSPECTIVE MATHEMATICS TEACHERS ABOUT SOME TEACHING-LEARNING MODELS USED IN MATHEMATICS CLASSES	127
Munevver Tuz	BOUNDARY VALUES FOR AN EIGENVALUE PROBLEM WITH A SINGULAR POTENTIAL	128
Münevver Tuz, Etibar Panakhov	ON INVERSE STURM- LIOUVILLE PROBLEMS WITH SYMMETRIC POTENTIALS	129
Bilgehan Gurunlu, Serkan Ozturk	QUANTUM ENCRYPTION IN WIRELESS NETWORK TECHNOLOGY	130
Mehmet Ali Balcı, Sibel Paşalı Atmaca, Ömer Akgüller	POISSON BRACKET ON MEASURE CHAINS	131
Hikmet Kemalolu, Ünal İç, Tuba Gulsen	AN INVERSE NODAL PROBLEM FOR DIFFERENTIAL PENCILS WITH COMPLEX SPECTRAL PARAMETER DEPENDENT BOUNDARY CONDITIONS	132
Seyfollah Mosazadeh, Hikmet Kemalolu, Emrah Yılmaz	THE STABILITY OF THE INVERSE PROBLEM WITH AN INTEGRO-DIFFERENTIAL OPERATOR	133
Seyfollah Mosazadeh, Hikmet Kemalolu	AN INVERSE PROBLEM FOR DIRAC OPERATOR AND THE STABILITY THEOREM	134
Anis Bel Hadj Hassin, Sinda Khalfallah	VIRTUAL CONTROL AND CRACK IDENTIFICATION: 2D HEAT EQUATION	135
Seyma Tuluçe Demiray, Hasan Bulut	A NEW APPROACH FOR NIZHNIK-NOVIKOV-VESELOV SYSTEM	136
Seyma Tuluçe Demiray, Hasan Bulut	ANALYTICAL SOLUTIONS OF PHI-FOUR EQUATION	137
Saleem Al-Zoubi	DEVELOPING M-LEARNING PROTOTYPE SYSTEM	138



**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

Semiha Makinist, İbrahim Rıza Hallaç, Betül Karakuş, Galip Aydın	PREPARATION OF IMPROVED TURKISH DATASET FOR SENTIMENT ANALYSIS IN SOCIAL MEDIA	139
Haci Mehmet Baskonus, Fevzi Erdogan, Arif Ozkul, Ilham Asmouh	NOVEL BEHAVIORS TO THE NONLINEAR EVOLUTION EQUATION DESCRIBING THE DYNAMICS OF IONIC CURRENTS ALONG MICROTUBULES	140
Fouad Essahlaoui, Ahmed El Abbassi, Rachid Skouri	EMULATE ARTIFICIAL NEURAL NETWORK TO MAKE A DECISION IN WIRELESS SENSOR	141
Murat Şat	INVERSE PROBLEM FOR STURM-LIOUVILLE OPERATOR WITH SINGULARITY	142
E. Bonyah O. K. Okosun M. Altaf Khan	MATHEMATICAL MODELING OF CHURCH GROWTH	143
Samer Al Ghour	ON TWO TYPES OF COUNTABLE DENSE HOMOGENEOUS SPACES	144
Anum Shafiq, Zakia Hammouch	RADIATIVE MHD FLOW OF SECOND-GRADE FLUID TOWARDS A STRETCHED SPHERE	145
Toufik Mekkaoui, Ebenzer Bonyah, Zakia Hammouch	A CAPUTO-FABRIZIO FRACTIONAL-ORDER NETWORK MODEL FOR ZIKA VIRUS: NUMERICAL SIMULATIONS AND DYNAMICS	146
Yunus ÇAKIR, Nesrin ÖZSOY	PERCEPTIONS OF HIGH SCHOOL STUDENTS TO USE MOBILE LEARNING IN MATHEMATICS COURSE	147
S. Şule Şener, Yeşim Saraç	SOLVING AN PROBLEM OF OPTIMIZING THE INITIAL CONDITION IN A HEAT EQUATION	148
Abdulkadir Karakaş, Yavuz Altın	ON STATISTICAL CONVERGENCE OF FUZZY SEQUENCES	149
Yavuz Altın, Mikail Et, Hifsi Altınok	STATISTICAL CONVERGENCE OF ORDER $\alpha$ IN AMENABLE SEMIGROUPS	150
Mikail Et, Yüksel Erol	ON DEFERRED STATISTICAL CONVERGENCE OF ORDER $\alpha$ OF SEQUENCES OF FUZZY NUMBERS	151
M. Emre Kavgacı, Hüseyin Bereketoğlu, Özgür Aydoğmuş	WEAKLY NONLINEAR ANALYSIS OF INTEGRO-DIFFERENCE EQUATIONS FOR GROWTH-DISPERSAL MODELS	152
Müge Yeldan, Samet Gençgönül	EFFICIENCY ANALYSIS FOR INSURANCE COMPANY WITH DATA ENVOLEPMENT ANALYSIS	153
Mehtap Lafcı, Hüseyin Bereketoğlu	ON A PARTIAL DIFFERENTIAL EQUATION WITH PIECEWISE CONSTANT MIXED ARGUMENT	154
Yusuf Pandir, Yusuf Gürefe	NEW JACOBI FUNCTION SOLUTIONS OF COMBINED KDV-MKDV EQUATION	155

**2<sup>nd</sup> INTERNATIONAL CONFERENCE ON  
COMPUTATIONAL MATHEMATICS AND ENGINEERING SCIENCES - CMES2017**  
20-22 May 2017, Istanbul, TURKEY

Ali Demir, Ender Başarı, Duygu Dönmez Demir	FINITE ELEMENT MODELLING OF A REINFORCED CONCRETE STRUCTURE OCCURING GROUND SETTLEMENT	156
Mehmet Ali Balcı, Sibel Paşalı Atmaca, Ömer Akgüller	THE BOUNDARY CURVATURES OF GRAPH COMMUNITIES	157
Hatice Aslan	APPROXIMATION PROPERTIES OF DE LA-VALLEE POUSSIN MEANS FOR SERIES BY NONLINEAR FOURIER ATOMS	158
Serbay Duran, Muzaffer Askin, Tukur Abdulkadir Sulaiman	NEW SOLITON PROPERTIES TO THE OF ILL-POSED BOUSSINESQ EQUATION ARISING IN NONLINEAR PHYSICAL SCIENCE	159
Anum Shafiqa, Faiza Naseemb, Lifeng Zhaob and Anum Naseem	KEROSENE OIL BASED SQUEEZING FLOW OF CARBON NANOTUBE BETWEEN TWO RIGA DISKS	160
Burak Tufan Gökmen, Tuğba Petik, Halim Özdemir	THE QUADRATICITY OF LINEAR COMBINATIONS OF A QUADRATIC AND A CUBIC MATRIX THAT COMMUTE	161
S. Ali Tahir, A. Bouhamidi, M. Sari	SYNCHRONIZATION OF IDENTICAL AND NON- IDENTICAL CHAOTIC DYNAMICAL SYSTEMS	162
Tolga Akturk, Yusuf Gurefe, Hasan Bulut	NEW FUNCTION METHOD TO THE (N+1) DIMENSIONAL NONLINEAR PROBLEMS	163
N. Boussof, C. Benhamideche, H. Sahraoui, M. F. Mosbah	EDX analysis, microstructure and transport properties of MgO doped Bi2212 superconductors	164
Choubeila Boubechou, Ali Bouchoucha, Hamid Zaidi	STUDY OF THE TRIBOLOGICAL BEHAVIOR OF A SLIDING CONTACT BRASS-STEEL COUPLE	165
Gheribi Hassina, Boukebbab Salim	MEASUREMENT UNCERTAINTY ON A GEOMETRICAL SPECIFICATION IN THREE- DIMENSIONAL MEASUREMENT	EK-1
Elnur Nuri, Elvin Nasibov	A PACKAGED SOFTWARE FOR SOLUTION OF THE PROBLEM OF OPTIMAL PLACEMENT AND INTEGRATION OF OIL AND GAS PLATFORMS	EK-2
Ayşe T. Bugatekin and Sinan Çalık	ON MOMENTS GENERATING FUNCTIONS OF SAMPLE EXTREMES OF ORDER STATISTICS FROM DISCRETE UNIFORM DISTRIBUTION	EK-3
Gökhan Gökdere	USEFUL INEQUALITIES FOR UPPER AND LOWER BOUNDS OF REPAIRABLE AGING COLD STANDBY SYSTEM	EK-4
Mehmet Gürçan, Sinan Çalık, Yunus Güral	SEQUENCES WITH RANDOM INDICES IN CLASSICAL BANACH SPACE	EK-5
Mehmet Bektaş	AN INTEGRAL FORMULA ON THE LORENTZIAN MANIFOLD	EK-6
Mine Babaoglu, Etibar S. Panakhov	ON SOME SPECTRAL PROBLEMS FOR DIFFUSION OPERATOR	EK-7
Aisha Jabeen	MULTIPLICATIVE LIE TRIPLE HIGHER DERIVATION ON UNITAL ALGEBRA	EK-8
Mahvish Ali	LIE ALGEBRA REPRESENTATIONS AND 1- PARAMETER 2D-HERMITE POLYNOMIALS	EK-9

## POSTERS

Kaya Tubay, Erman Orhan, Aydın Sevinç, Yılmaz Ökkeş	THE ANTIOXIDANT EFFECTS OF GOLDENBERRY ( <i>Physalis peruviana</i> L.) EXTRACT AGAINST TO THE OXIDATIVE EFFECTS OF TYPE I DIABETES IN MUSCLE TISSUE OF RATS	166
Ebru Koçak, Mehmet Bektaş	THE CHARACTERIZATIONS OF NULL QUATERNIONIC CURVE IN $R_1^4$	167
Mehmet Bektaş, Münevver Yıldırım Yılmaz	A NOTE ON SIACCI'S THEOREM	168
Mihriban Külahcı, Fatma Almaz, Mehmet Bektaş	A NEW APPROACH FOR SMARANDACHE CURVES IN THE NULL CONE $Q^3$	169
M. Baki Yağbasan, Recep Şahin, İ. Onur Kıymaz, Ayşegül Çetinkaya, Oğuz Yağcı	NEW GENERALIZATIONS OF SOME MULTIPLE HYPERGEOMETRIC FUNCTIONS	170
Ayşe Arslan, Erdal Ekici	ON A SPECIAL CLOPENNESS	171
Elif Karataş, Erdal Ekici	ON APPLICATIONS OF A GENERALIZED MAP	172
Burak Meral, Erdal Ekici	A NEW CLOSED MAPPING	173
Said Boucetta, Boubaker Othmani	THERMAL STABILITY AND ELASTIC PROPERTIES OF $Mg_3CuH_{0.6}$ TERNARY HYDRIDE	174
Boubaker Othmani, Said Boucetta	INVESTIGATION ON STRUCTURAL, ELASTIC AND THERMODYNAMIC PROPERTIES OF $MgNi_3$ INTERMETALLIC COMPOUND	175

# PLENARY TALKS





## CLASS NUMBERS OF CERTAIN QUADRATIC FIELDS

**Kalyan Chakraborty**

Harish-Chandra Research Institute, Chhatnag Road, Jhansi Allahabad, India  
kalyan@hri.res.in

### **Abstract**

The talk will be based on some of my recent results with Dr. Azizul Hoque, concerning the divisibility of the class numbers of certain families of real (respectively imaginary) quadratic fields. The main target will be to show the existence of a new family of infinitely many quadratic fields whose class number is divisible by a given integer. The talk will begin with motivation for the problems and will be inclusive.

**Keywords:** Quadratic fields, Divisibility, Class numbers

### **REFERENCES**

1. Kalyan Chakraborty, Azizul Hoque, Yasuhiro Kishi and Prem Prakash: Divisibility of the class numbers of imaginary quadratic fields (submitted).
2. Azizul Hoque and Kalyan Chakraborty: Divisibility of class numbers of certain families of quadratic fields (submitted).



## **FRACTAL-FRACTIONAL DIFFERENTIATION AND INTEGRATION**

**Abdon Atangana**

Institute for Groundwater, Faculty of Natural and Agricultural Science, University of the Free  
State, 9300 Bloemfontein, South Africa.

AtanganaA@ufs.ac.za

### **Abstract**

New operators of differentiation have been introduced in this paper as convolution of power law, exponential decay law, generalized Mittag-Leffler law with fractal derivative. The new operators aimed to attract more non-local natural problems that display at the same time fractal behaviors. Some new properties are presented, the numerical approximation of these new operators is also presented with some applications to real world problem.

**Keywords:** Fractal Fractional differentiation; non-locality, non-singularity, numerical approximation.

### **REFERENCE**

1. Badr Saad T. Alkahtani, " Chua's circuit model with Atangana–Baleanu derivative with fractional order Chaos, Solitons & Fractals", Volume 89, August 2016, Pages 547–551
2. Obaid Jefain Julaighim Algahtani. Comparing the Atangana–Baleanu and Caputo–Fabrizio derivative with fractional order: Allen Cahn model Chaos, Solitons & Fractals, Volume 89, August 2016, Pages 552–559
3. Caputo, Michele. "Linear model of dissipation whose Q is almost frequency independent-II". Geophys. J. R. Astron. Soc. 13 (5) (1967) pp. 529–539.
4. Hadamard, J., Essai sur l'étude des fonctions données par leur développement de Taylor, Journal of pure and applied mathematics, vol. 4, no. 8, pp. 101–186, 1892.
5. Kober, Hermann (1940). "On fractional integrals and derivatives". The Quarterly Journal of Mathematics (Oxford Series). 11 (1): 193–211.





## **A PRACTICAL METHOD FOR ANALYTICAL EVALUATION OF APPROXIMATE SOLUTIONS OF PARTIAL DIFFERENTIAL EQUATIONS**

**Necdet Bildik**

Department of Mathematics, Manisa Celal Bayar University, Manisa, Turkey  
necdet.bildik@cbu.edu.tr

### **Abstract**

In this talk, a framework is constructed to get more approximate solutions to nonlinear partial differential equations by applying perturbation iteration technique. This technique is reformulated and improved to solve the Fisher's, the Burgers' and regularized long wave equations. Comparison between obtained solutions and the known exact solutions reveals that this technique is highly effective, reliable and accurate in solving nonlinear problems. Convergence analysis and error estimate are also provided by using some related theorems. The basic ideas indicated in this work are anticipated to be further developed to handle nonlinear models.

**Keywords:** Perturbation iteration method, partial differential equation, nonlinear diffusion, wave equations, convergence.

### **REFERENCES**

1. Shivanian, Elyas, and Saeid Abbasbandy. "Predictor homotopy analysis method: Two points second order boundary value problems." *Nonlinear Analysis: Real World Applications*, 15 (2014): 89-99.
2. Aksoy, Yigit, et al. "New perturbation-iteration solutions for nonlinear heat transfer equations." *International Journal of Numerical Methods for Heat & Fluid Flow*, 22.7 (2012): 814-828.
3. Aksoy, Yiğit, and Mehmet Pakdemirli. "New perturbation--iteration solutions for Bratu-type equations." *Computers & Mathematics with Applications*, 59.8 (2010): 2802-2808.



## STATISTICAL CONVERGENCE OF ORDER $\alpha$ AND STATISTICAL BOUNDEDNESS OF ORDER $\alpha$ IN METRIC SPACES

Rifat Çolak

Department of Mathematics, Firat University, 23119, Elazig, TURKIYE

rftcolak@gmail.com

### Abstract

The concept of statistical convergence was first introduced in 1935. It was built in its today meaning in 1950 and it has been worked intensively in the last 30-40 years. Statistical convergence of order  $\alpha$  was given and studied in 2010 for number sequences. The subject has been a major improvement over the past five to ten years and has been the focus of many mathematicians working on this field. The order of statistical convergence of a sequence of positive linear operators was introduced by Gadjiev and Orhan in 2002 and then the statistical convergence of order  $\alpha$  ( $0 < \alpha \leq 1$ ) and strong  $\rho$ -Cesàro summability of order  $\alpha$  were introduced and studied by Çolak in 2010 for number sequences, using the notion  $\alpha$ -density of a subset of the set  $\mathbb{N}$  of positive integers.

In this talk, using the notations  $S_d^\alpha$ ,  $BS_d^\alpha$  and  $w_{\rho d}^\alpha$  for the spaces of sequences in question we introduce and give  $d$ -statistical convergence of order  $\alpha$  ( $0 < \alpha \leq 1$ ),  $d$ -statistical boundedness of order  $\alpha$  ( $0 < \alpha \leq 1$ ), and  $d$ -strong  $\rho$ -Cesàro summability of order  $\alpha$  ( $\alpha > 0$ ) for a sequence in a metric space. Furthermore we investigate the relations between the sets of  $d$ -statistically convergent sequences of order  $\alpha$ , between the sets of  $d$ -statistically bounded sequences of order  $\alpha$  and between the sets of  $d$ -strongly  $\rho$ -Cesàro summable sequences of order  $\alpha$  for various values of  $\alpha$ 's. Also, we establish some relations between these concepts.

**Keywords:**  $\alpha$ -density; statistical convergence; statistical convergence of order  $\alpha$ ; statistical boundedness of order  $\alpha$ ; strong  $\rho$ -Cesàro summability.



## **ADVANCES IN DISCRETE FRACTIONAL CALCULUS: THEORY AND APPLICATIONS**

**Dumitru Baleanu** <sup>1,2</sup>

<sup>1</sup> Department of Mathematics, University of Firat, Elazig, Turkey

dumitru@cankaya.edu.tr

<sup>2</sup> Institute of Space Science, Magurele- Bucharest, Romania

### **Abstract**

In this talk, I will report some new results in the field of fractional calculus and its applications in science and engineering.

**Keywords:** Discrete fractional calculus; Caputo derivative; Caputo-Fabrizio derivative; Mittag-Leffler kernel.

### **REFERENCES**

1. Guo-Cheng Wu, Dumitru Baleanu, He-Ping Xie, Fu-Lai Chen, Chaos synchronization of fractional chaotic maps based on the stability condition, *Physica A-Statistical Mechanics and its Applications* Vol: 460, 374-383, 2016.
2. Guo-Cheng Wu, Dumitru Baleanu, He-Ping Xie, Riesz Riemann-Liouville difference on discrete domains, *Chaos*, Vol: 26, No: 8, Article Number: 084308, 2016.
3. Thabet Abdeljawad, Dumitru Baleanu, Discrete fractional differences with nonsingular discrete Mittag-Leffler kernels, *Advances in Difference Equations*, Article Number: 232, 2016



## **MULTI-DEGREE REDUCTION OF SAID-BALL CURVES WITH ENDPOINTS CONSTRAINTS**

**Abedallah Rababah**

Department of Mathematics, Jordan University of Science and Technology, Irbid  
22110, Jordan  
rababah@just.edu.jo

### **Abstract**

In this talk, a new approach for multi-degree reduction of Said-Ball curves is investigated. Conditions for continuities and tangent continuities at both bound aries of the curve are given. The distance between the original Said-Ball curve and the degree reduced Said-Ballcurve is measured in L2-norm under the satisfaction of  $G^0$ -and  $G^1$ -continuity conditions. Several numerical examples, figures, and comparisons show that the proposed methods produce better results than existing methods in the literature.

**Keywords:** Said-Ballcurves; degreereduction;  $G^0$ -continuity;  $G^1$ -continuity.

### **REFERENCES**

1. T. N. T. Goodman and H. Said (1991). Shape-preserving properties of the generalized Ballbasis, Computer Aided Geometric Design, 8:2, 115-121.
2. A. Rababah, B.G. Lee, and J. Yoo (2007). Multiple degree reduction and elevation of Bezier curves using Jacobi-Bernstein basis transformations. Numerical Functional Analysis and Optimization 28, Issue 9-10: 1179-1196.
3. A. Rababahand Y. Hamza, Multi-degree reduction of disk Bezier curves with  $G^0$ - and  $G^1$ -continuity, Journal of Inequalities and Applications, 2015 (2015), 307.
4. H. Said (1989), Generalized Ball curve and its recursive algorithm, ACM Trans. Graph. 8, 360-371.



## **A THREE FACTOR REMOTE USER AUTHENTICATION SCHEME USING COLLISION RESIST FUZZY EXTRACTOR IN SINGLE SERVER ENVIRONMENT**

**Debasis Giri<sup>1</sup> and Tanmoy Maitra<sup>2</sup>**

<sup>1</sup>Department of Computer Science and Engineering, Haldia Institute of Technology, Haldia-721657, India

<sup>2</sup>Department of Computer Science and Engineering, Jadavpur University, Kolkata-700032, India

debasis\_giri@hotmail.com, tanmoy.maitra@live.com

### **Abstract**

Due to rapid growth of online applications, it is needed to provide such a facility by which communicators can get the services by applying the applications in a secure way. As communications are done through an insecure channel like Internet, any adversary can trap and modify the communication messages. Only authentication procedure can overcome the aforementioned problem. Many researchers have proposed so many authentication schemes in this literature. But, this paper has shown that many of them are not usable in real world application scenarios because, the existing schemes cannot resist all the possible attacks. Therefore, this paper has proposed a three factor authentication scheme using hash function and fuzzy extractor. This paper has further analyzed the security of the proposed scheme using random oracle model. The analysis shows that the proposed scheme can resist all the possible attacks. Furthermore, comparison between proposed scheme and related existing schemes shows that the proposed scheme has better trade-off among storage, computational and communication costs.

**Keywords:** Attack; Authentication; Biometric; Password; Smart card.

### **REFERENCES**

1. Leslie Lamport. Password authentication with insecure communication. Commun. ACM, Vol. 24, No: 11, 770-772, 1981.
2. Debasis Giri, R. Simon Sherratt, Tanmoy Maitra, A novel and efficient session spanning biometric and password based three-factor authentication protocol for consumer USB Mass Storage Devices. IEEE Trans. Consumer Electronics, Vol. 62, No: 3, 283-291, 2016.



## **ANALYTICAL STUDY FOR NONLINEAR FRACTIONAL DIFFERENTIAL EQUATIONS**

**Devendra Kumar**

Department of Mathematics, JECRC University, Jaipur-303905, Rajasthan, India  
devendra.maths@gmail.com

### **Abstract**

Fractional differential equations are the generalizations of differential by the application of fractional calculus. Fractional differential equations are increasingly used to model problems in research areas as diverse as dynamical systems, mechanical systems, control, chaos, chaos synchronization, continuous-time random walks, anomalous diffusive and subdiffusive systems, unification of diffusion and wave propagation phenomenon and others. The most important advantage of using fractional differential equations in these and other applications is their non-local property. In view of the great importance of fractional differential equations in science and engineering, we discuss some analytical techniques for solving nonlinear fractional differential equations. To show the efficiency of analytical techniques, we present some numerical examples. The numerical results are presented graphically. The results show that the analytical scheme is very fantastic and user friendly for solving nonlinear fractional differential equations describing physical problems.

**Key words:** Fractional differential equations, Analytical methods, Caputo fractional derivative.

### **REFERENCES**

1. I. Podlubny, Fractional differential equations, Academic Press, San Diego, Calif, USA 198 (1999) 340 pages.
2. M. Caputo, Elasticita e Dissipazione, Zani-Chelli, Bologna, 1969.
3. A.A. Kilbas, H.M. Srivastava and J.J. Trujillo, Theory and applications of fractional differential equations, Elsevier, Amsterdam 204 (2006) 540 pages.
4. H.M. Baskonus, T. Mekkaoui, Z. Hammouch and H. Bulut, Active Control of a Chaotic Fractional Order Economic System, Entropy, 17(8) (2015), 5771-5783.
5. S.J. Liao, Beyond Perturbation: Introduction to homotopy analysis method. Chapman and Hall / CRC Press, Boca Raton, 2003.
6. S.J. Liao, On the homotopy analysis method for nonlinear problems, Applied Mathematics and Computation 147 (2004), 499–513.

# PROCEEDINGS



# ANALYTIC SOLUTIONS OF OLDROYD-B FLUID WITH FRACTIONAL DERIVATIVES IN A CIRCULAR DUCT DUE TO TENSION ON THE BOUNDARY

**M.B. Riaz**

Department of Mathematics, University of Management and Technology, Lahore, Pakistan

bilal.riaz@umt.edu.pk

## **Abstract**

The aim of this talk is to analyze the rotational flow of an Oldroyd-B fluid with fractional derivatives, induced by an infinite circular cylinder that applies a constant couple to the fluid. Such kind of problem in the settings of fractional derivatives has not been found in the literature. The solutions are based on an important remark regarding the governing equation for the nontrivial shear stress. The solutions that have been obtained satisfy all imposed initial and boundary conditions and can easily be reduced to the similar solutions corresponding to ordinary Oldroyd-B, fractional/ordinary Maxwell, fractional/ordinary second-grade, and Newtonian fluids performing the same motion. The obtained results are expressed in terms of Newtonian and non-Newtonian contributions. Finally, the influence of fractional parameters on the velocity, shear stress and a comparison between generalized and ordinary fluids is graphically underlined.

**Keywords:** Oldroyd-B fluid; Fractional calculus; Velocity field; Shear stress; Circular duct; Analytic solutions.

## **REFERENCES**

1. Corina Fetecau, M. Rana, N. Nigar, C. Fetecau, First exact solutions for flows of rate type fluids in a circular duct that applies a constant couple to the fluid, Z. Naturforsch. 69 (a) 232–238 2014



## **SIMULATION OF WATER-BASED MAGNETITE NANOPARTICLES BETWEEN TWO PARALLEL SURFACES WITH SUCTION/INJECTION**

**Abdelazize Raada<sup>1</sup>, Driss Mrani<sup>1</sup>, Rizwan Ul Haq<sup>2</sup>**

<sup>1</sup>Department of Mathematics, Faculty of Sciences and Techniques Errachidia, Morocco

<sup>2</sup>Bahria University, Pakistan

### **Abstract**

The present work examines the fully developed squeezing flow of water functionalized magnetite nanoparticles between two parallel permeable surfaces. For strongly magnetite fluid three different types of nanoparticles having better thermal conductivity: Magnetite ( $\text{Fe}_3\text{O}_4$ ), Cobalt ferrite ( $\text{CoFe}_2\text{O}_4$ ) and Mn-Zn ferrite ( $\text{Mn-ZnFe}_2\text{O}_4$ ) are incorporated within the base fluid (water). Systems of equations containing the nanoparticle volume fraction are rehabilitating in the form of partial differential equations. Resulting mathematical model is converted in the form of ordinary differential equations with the help of compatible similarity coordinates. Results are analyzed for velocity, temperature, reduced skin friction and reduced Nusselt number with variation of different emerging parameters and determine the superb thermal conductivity among mentioned nanoparticles.

**Keywords:** Squeezing channel, Magnetite nanoparticles, Thermal conductivity, Simulation.

### **References**

1. Atlas, M., Haq, R. U., & Mekkaoui, T. (2016). Active and zero flux of nanoparticles between a squeezing channel with thermal radiation effects. *Journal of Molecular Liquids*, 223, 289-298.
2. Haq, R. U., Hammouch, Z., & Khan, A. W. (2014). Water-based squeezing flow in the presence of carbon nanotubes between two parallel disks. *Thermal Science*, (00), 148-148.

# A NOTE ON A NUMERICAL METHOD FOR SYMMETRIC HAMILTONIAN MATRICES

Agoujil Said

Department of Computer Sciences, Faculty of Sciences and Techniques Errachidia  
Moulay Ismail University, Morocco  
agoujil@gmail.com

## Abstract

We present in this study a numerical methods to get eigenvalue of the particular case of structured matrices. Our approach here is based on symplectic reflector defined in  $R^{2N \times 2}$ . Numerical examples are presented.

**Keywords:** Hamiltonian and Skew-Hamiltonian matrices, Symplectic and symmetric matrix, reflecteur symplectic, eigenvalues

## REFERENCES

- 1.S. Agoujil and A. H. Bentbib, New symplectic transformation on  $C^{2N \times 2}$ : Symplectic reflectors, Int. Jour. of Tomography and Statistics (IJTS), 11, Summer, 2009.
- 2.S. Agoujil AND A. H. Bentbib, On the reduction of Hamiltonian matrices to a Hamiltonian Jordan canonical form, Int. Jour. Math. Stat. (IJMS), 4, 12–37, Spring 2009.

# NUMERICAL METHODS OF A MIXED PROBLEM FOR A NONLINEAR KIRCHHOFF MODEL WITH MOVING BOUNDARY

Mohamed Mbehou

Department of Mathematical Sciences, University of South Africa, Pretoria, South Africa

mohamm@unisa.ac.za

## Abstract

With the use of the coordinate transformation which fixes the boundaries, the finite element formulation is presented for the space variable. Its convergence and error bounds in the energy norm and for the first time derivative in the  $L^2$ -norm are established. In particular, the error in the energy norm and for the first time derivative in the  $L^2$ -norm is shown to converge with the optimal order  $O(h^r)$  with respect to the mesh size  $h$  and the polynomial degree  $r \geq 1$ . To obtain the fully discrete solution, the generalized- $\alpha$  method is adapted to the semidiscrete formulation. Finally, some numerical simulations that validated the theoretical findings are exhibited.

**Keywords:** Kirchhoff model, moving boundaries, optimal error estimate, Newmark schemes, generalized- $\alpha$  method, Galerkin finite element method.

## **M.L.E SPEED OF CONVERGENCE IN NONLINEAR AUTOREGRESSIVE PROCESSES**

**Meriem Henkouche**

Department of Mathematics, U.S.T.O.M.B, Oran, Algeria

mhenk1094@yahoo.fr

### **Abstract**

In this study, we deal with some asymptotic properties of the maximum likelihood estimators of a multivariate parameter for nonlinear autoregressive processes. Under suitable assumptions, the consistency, the asymptotic normality and the rate of convergence in distribution ( $O(n^{-1/2})$ ) are settled. This rate is the same as in i-i-d case. The method is by the Edgeworth expansions and Berry Essen bounds.

**Keywords:** Autoregressive process; Berry Essen bound; Edgeworth; Maximum likelihood estimators.

### **REFERENCES**

1. R. N. Bhattacharya and R. Rao, Normal approximation and Asymptotic expansions, J. Wiley, New York, 1976.
2. M. Henkouche, Maximum likelihood estimators in nonlinear autoregressive processes, Int. Journal of Mathematical Analysis, 6, 25, 1205-1226, 2012.
3. T. Kato, Perturbation theory for linear operators, Springer Verlag, Berlin, Heidelberg, 1966.
4. X. Milhaud and A. Raugi, Etude de l'estimateur du maximum de vraisemblance dans le cas d'un processus autoregressif: convergence, normalité asymptotique et vitesse de convergence, Annales de l'Inst. Henri Poincaré, 25, 4, 383-427, 1989.

## **SIMULATED ANNEALING HYBRIDIZED WITH DYNAMIC PROGRAMMING APPLIED TO SOLVE THE SEQUENCE ALIGNMENT PROBLEM**

**Ernesto Liñán-García<sup>1</sup>, Juan Frausto-Solís<sup>2</sup>, Norma Dominguez-Sarabia<sup>1</sup>,  
Francisco Hernández-Rodríguez<sup>1</sup>**

<sup>1</sup>Universidad Autónoma de Coahuila, Saltillo, Coahuila, México.

<sup>2</sup>Instituto Tecnológico de Ciudad Madero, Ciudad Madero, Tamaulipas, México.

<sup>1</sup>ernesto\_linan\_garcia@uadec.edu.mx,

### **Abstract**

In this study, a new algorithm based on Simulated Annealing (SA) to solve the sequence alignment problem is proposed, which is named Simulated Annealing with Dynamic Programming (SADP). This new algorithm is a combination of the classical Simulated Annealing (SA) and the Dynamic Programming (DP). This algorithm is implemented to obtain results of pair sequence alignment. Simulated Annealing is a simulation of cooling of a metal to solve an optimization problem. The Dynamic Programming is an optimization algorithm, which transforms a problem into several simple problems. In order to create new solutions of sequence alignment problem, the proposed algorithm applies dynamic programming with very small DNA subsequences into Metropolis Cycle of Simulated Annealing, this approach increases the quality of the solution to the problem of alignment genomic sequences. The parameters of proposed algorithm, for certain instances, are tuned by an analytical method and some parameters have been experimentally calculated. SADP's results are compared with the classical SA, Simulated Annealing with Previous Solutions (SAPS) and Dynamic Programming (DP). The instances used are specific genes of the HIV (Human Immunodeficiency Virus), SIV (Simian Immunodeficiency Virus), HPV (Human papillomavirus), CPV (Canine Papillomavirus) and HHV (Human Herpesvirus) viruses.

**Keywords:** Alignment Sequence Problem; Simulated Annealing Algorithm; Dynamic Programming;

### **REFERENCES**

1. Ernesto Liñán-García, Lorena Marcela Gallegos-Araiza, Simulated Annealing with Previous Solutions Applied to DNA Sequence Alignment, ISRN Artificial Intelligence, vol: 2012, 2012.
2. I.Ö. Bucak, V. Uslan. An analysis of sequence alignment: heuristic algorithm. Conf Proc IEEE Eng Med Biol Soc, 2010.

## **COMMUTATIVITY THEOREMS IN RINGS WITH INVOLUTION: A SURVEY**

**Abdellah Mamouni**

Department of Mathematics, Faculty of Sciences and Techniques Errachidia, Morocco

mamouni\_1975@live.fr

### **Abstract**

In this study, we investigate commutativity of ring  $R$  with involution  $*$  which admits a derivation satisfying certain algebraic identities. Some well-known results characterizing commutativity of prime rings have been generalized. Finally, we provide examples to show that various restrictions imposed in the hypotheses of our theorems are not superfluous.

**Keywords:** Prime ring, involution, commutativity, derivation.

### **References**

1. M. Ashraf and N. Rehman, on commutativity of rings with derivation, Results Math. 42 (2002), no. 1-2, 3-8.
2. S. Ali, N. A. Dar and A. N. Khan, On strong commutativity preserving like maps in rings with involution, Miskolc Mathematical Notes. J. 16 (2015), 1, 17-24.
3. H. E. Bell and M. N. Daif, On derivations and commutativity in prime rings, Acta Math. Hungar. 66 (1995), 337-343.

## **NEW SOLITARY WAVE SOLUTIONS TO THE (2+1)- DIMENSIONAL CALOGERO-BOGOYAVLENSKII- SCHI AND THE KADOMTSEV-PETVIASHVILI HIERARCHY EQUATIONS**

**Haci Mehmet Baskonus<sup>1</sup>, Tukur Abdulkadir Sulaiman<sup>2</sup>, Hasan Bulut<sup>3</sup>**  
<sup>1</sup>Department of Computer Engineering, Munzur University, Tunceli, Turkey  
<sup>2,3</sup>Department of Mathematics, University of Firat, Elazig, Turkey  
hmbaskonus@gmail.com, mtukur74@yahoo.com, hbulut@firat.edu.tr

### **Abstract**

By means of the sine-Gordon expansion method, we construct new solitary wave solutions to the Calogero-Bogoyavlenskii-Schi and Kadomtsev-Petviashvili hierarchy equations. The solutions obtained are complex, hyperbolic and trigonometric function solutions. All the obtained solutions satisfy their corresponding equation (that is equation (3.1) and (3.10)), we carry out the test of satisfaction with help of Wolfram Mathematica 9. We also plot the three- and two-dimensional graphics by using the same code in Wolfram Mathematica 9.

**Keywords:** Sine-Gordon expansion method; Calogero-Bogoyavlenskii-Schi equation; Kadomtsev-Petviashvili hierarchy equation; complex function solutions; hyperbolic function solutions; trigonometric function solutions.

### **REFERENCES**

1. AR Seadawy and A Sayed Abstract and Applied Analysis, 2014, 7, 2014.
2. R Arora and A Kumar Applied Mathematics 1(2) 59, 2011.
3. W Jia L Biao and Y Wang-Chuan Chin. Phys. B 19(3), 7, 2010.
4. Y Li and D Li Applied Mathematical Sciences 6(12), 579, 2012.
5. J Cao M Song and J Zhou Int. Journal of Math. Analysis 6(43) 2141, 2012.
6. MF Aghdai and J Manafianheris Journal of Mathematical Extension, 5(2), 91, 2011.
7. MJ Ablowitz B Prinari and AD Trubatch Dynamics of PDE 1(3) 239, 2004.

## **A SCHEDULING PROBLEM FOR UNLOADING OPERATIONS INCONTAINER TERMINAL**

**Sanae Kouismi**

Equipe MOAD-SCM, Ecole Mohammadia d'Ingénieurs, University Mohammed 5 in Rabat,  
Morocco

sanaekouismi@research.emi.ac.ma,

### **Abstract**

This study deals with the problem of minimizing the completion time of unloading containers from a train in the dry port MITA in Casablanca/Morocco. The main objective is to solve a real-world optimization problem. In the literature, problems related to unloading containers in a terminal can be classified into three kinds: first, the problems related to the planning of port handling equipment as presented by Lee et al. [1]: problem of allocating resources of a container terminal taking into account the global processing time or the delays. Then the problems using different types of handling equipment and their impact on each other (Bish et al. [2]); Problems related to interference of handling equipment. In this context, we present a new model to minimize the processing time of a waiting train on the railway dry port terminal. This treatment includes the unloading, transport and placement of all containers on the train to storage areas using the available cranes. That is to allocate optimally cranes and storage areas to containers. We present a new Mixed Integer Programming (MIP) model for the scheduling and storage problem taking into account the storage constraints. To test the performance of the proposed model, numerical tests are conducted and analysed. The results show the good quality of the obtained solutions.

**Keywords:** Scheduling; Makespan; Optimization; Crane assignment; Container terminal.

### **REFERENCES**

1. Der-Horng Lee, Jin Xin Cao, Qixin Shi, Jiang Hang Chen, A heuristic algorithm for yard trucks scheduling and storage allocation problems, *Transportation Research Part E: Logistics and Transportation Review*, Vol: 45, No: 5, 810-820, 2009.
2. Ebru K. Bish, Frank Y. Chen, Yin Thin Leong, Barry L. Nelson, Jonathan Wing Cheong Ng, and David Simchi-Levi, Dispatching vehicles in a mega container terminal; *OR Spectrum*, Vol: 27, No: 4, 491-506, 2005.



# CAPACITY SOLUTION TO A NONLINEAR ELLIPTIC COUPLED SYSTEM IN ORLICZ-SOBOLEV SPACES

Hicham Moussa\*, Francisco Ortegón Gallego and Mohamed Rhoudaf

\*Université Moulay-Ismaïl-Meknès. Faculté des Sciences de Meknès, Equipe: EDPs et  
Calculs Scientifiques, Morocco  
hichammoussa23@gmail.com

## Abstract

We shall give the existence of a capacity solution for a nonlinear elliptic coupled system, whose unknowns are the temperature inside a semi conductor material  $u$ , and the electric potential  $\varphi$ , Within the proof we use truncation methods, monotonicity arguments techniques, the integration by parts formula also we use Schauder's fixed point theorem to prove a weak solution, then we introduce a sequence of approximate problems which converges (upto a subsequence) in a certain sense to a capacity solution which have been adapted to non-reflexive Orlicz spaces.

**Keywords:** Capacity solution; Weak solution; Coupled system; Orlicz-Sobolev spaces.

## REFERENCES

1. J. P. Gossez, Some approximation properties in Orlicz-Sobolev, *Studia Math.* 74, (1982), pp. 17-24.
2. M. T. Gonzalez Montesinos and F. Ortegón Gallego, Existence of a capacity solution to a coupled nonlinear parabolic-elliptic system. *Commun. Pure Appl. Anal.*, {6}, No. 1 (2007), 23-42.
3. X. Xu, On the existence of bounded temperature in the thermistor problem with degeneracy. *Nonlinear Anal. T. M. A.* {42} (2000), 199-213.

## **A NONSTANDARD HIGHER-ORDER PDE FOR EDGE DETECTION IN MEDICAL IMAGING PROBLEMS**

**Hamdi Houichet, Maher Moakher, Badreddine Rjaibi, Anis Theljani**

Université de Tunis El Manar, Ecole Nationale d'Ingénieurs de Tunis, Laboratoire de  
Modélisation Mathématique et Numérique dans les Sciences de l'Ingénieur, B.P. 37, 1002  
Tunis, Tunisia.

hamdi.houichet@enit.utm.tn, maher.moakher@enit.utm.tn, badreddine.rjaibi@lamsin.rnu.tn,  
thaljanianis@gmail.com,

### **Abstract**

In this work, we address a nonstandard variational energy for important features detection and multiplicative noise removal in medical imaging problems. Our contribution consists in minimizing a  $p(\cdot)$ -Bilaplace energy with a variable exponent function  $p(\cdot)$ . We study the well-posedness of the proposed model and we consider an adaptive choice of  $p(\cdot)$  based on the topological gradient method. We give a numerical solution method based on splitting convexity schema and we present several numerical examples to show the robustness of the proposed approach.

**Keywords:**  $q(\cdot)$ -Laplace operator; topological gradient; ultrasound imaging; speckle noise.

### **REFERENCES**

1. H. Houichet, M. Moakher, B. Rjaibi, A topological sensitivity approach for noise removal and edge detection in ultrasound images, submitted, 2016.
2. F. Li, Z. Li, L. Pi, Variable exponent functionals in image restoration, Applied Mathematics and Computation, Vol:216, 870–882, 2010.

## **EXACT SOLUTION OF THE BLAST WAVE PROBLEM IN DUSTY GAS**

**Triloki Nath and L.P. Singh**

Department of Mathematical Sciences, Indian Institute of Technology (BHU), Varanasi, India  
trilokinath.rs.apm12@itbhu.ac.in

### **Abstract**

The aim of this study is to find the new exact solution of the blast wave problem in one-dimensional unsteady adiabatic flow for generalized geometry in a compressible, inviscid ideal gas with dust particles. The density of the undisturbed region is assumed to vary according to a power law of the distance from the point of explosion. It is observed that the presence of dust particles in the gas yields more complex expression as compared to the ordinary Gasdynamics. The exact solution of the problem in form of a power in the distance and the time is obtained. Further, the behaviour of the total energy carried out by the blast wave for planar, cylindrically symmetric and spherically symmetric flow corresponding to different Mach number of the fluid flow in a dusty gas is presented.

**Keywords:** Blast wave; strong shock; dusty gas.

### **REFERENCES**

1. GB. Whitham. Linear and Non-linear waves. Wiley and Sons, New York, 1974.
2. A. Sakurai. On the propagation and the structure of blast wave I. J. Phys. Soc. Japan 1953; 8: 662-669.
3. A. Sakurai. On the propagation and the structure of blast wave II. J. Phys. Soc. Japan 1954; 9: 256-266.
4. Murata S. New exact solution of the blast wave problem in gas dynamics. Chaos Soliton Fract. 2006; 28:327-330.

## AN INVESTIGATION ON A TWO DIMENSIONAL PROBLEM OF MODE-I CRACK UNDER AN EXACT HEAT CONDUCTION WITH A DELAY

**Shashi Kant and Santwana Mukhopadhyay**

Indian Institute of Technology (BHU), Varanasi, India  
shashi.rs.apm13@itbhu.ac.in

### Abstract

The present study is concerned with a recently proposed heat conduction model: an exact heat conduction model with a single delay term weakened by a finite linear Mode-I crack. The material of the medium is considered to be homogeneous and isotropic. The boundary of the crack is subjected to a prescribed stress distribution and temperature. The thermoelasticity theory with a single delay term developed by Quintanilla, is employed and integral transforms are used to obtain the solution of which is shown to be equivalent to the solution of a Fredholm's integral equation of the first kind. This integral equation is solved numerically by regularization method. The inversion of Laplace transform is also carried out numerically and numerical values of the displacement components, temperature and stresses in the physical domain are computed for copper material by considering different particular case. The results are also presented graphically.

**Keywords:** Generalized Thermoelasticity; Mode-I crack; Thermoelasticity with a single delay; Dual integral equations; Fredholm's integral equation

### REFERENCES

1. Ramon Quintanilla, Racke Rein Hard, A note on stability in three phase-lag heat conduction, International Journal of Heat and Mass transfer, Vol:51, 24-29, 2008.
2. Sadek Hossain Mallik, M. Kanoria, A unified generalized thermoelasticity formulataion: application to penny-shaped crack anal, Journal of TheramalStresses, Vol:32, 943-965, 2009.

## **DISCUSSION OF ADVECTION-DIFFUSION PROCESS IN FINITE ELEMENT TECHNIQUES**

<sup>1</sup>Murat Sari, <sup>2</sup>Huseyin Tunc

<sup>1</sup>Department of Mathematics, Faculty of Arts and Science, Yildiz Technical University,  
Istanbul, Turkey

<sup>2</sup>Department of Mathematical Engineering, Faculty of Chemistry and Metallurgy, Yildiz  
Technical University, Istanbul, Turkey

sarim@yildiz.edu.tr

### **Abstract**

The aim of this study is to discover numerical behaviour of the advection-diffusion processes using various finite element techniques based on B-splines. These methods are applied for the spatial derivatives and an optimization technique is suggested for the time integration of the resulting system. Note that the optimization technique has also been compared with the Runge-Kutta method. The proposed methods have been shown to be unconditionally stable. Two illustrative examples have also been presented. The computed results are seen to be highly accurate and in very good agreement with the literature.

**Keywords:** Advection-diffusion process; finite element method; B-splines; Runge-Kutta method; Mathematical modelling

### **REFERENCES**

1. D. Irk, I. Dag, M. Tombul, Extended cubic B-spline solution of the advection-diffusion equation, KSCE Journal of Civil Engineering, 19 (2015) 929-934.
2. J. Goh, A. A. Majid, A. I. Md. Ismail, Cubic B-spline collocation method for one-dimensional heat and advection-diffusion equations, Journal of Applied Mathematics, 37 (2012) 1-8.
3. C. V. Ramakrishnan, An upwind finite element scheme for the unsteady convective diffusive transport equation, Applied Mathematical Modelling, 3 (1979) 280-284.
4. A. Korkmaz, I. Dag, Quartic and quintic B-spline methods for advection-diffusion equation, Applied Mathematics and Computation, 274 (2016) 208-219.
5. M. Sari, G. Gurarslan, A. Zeytinoglu, High-order finite difference schemes for solving the advection-diffusion equation, Mathematical and Computational Applications 15 (2010) 449-460.

## **EVOLUTION PROBLEM GOVERNED BY THE SUBDIFFERENTIAL OPERATOR WITH DELAY**

**Soumia Saïdi**

LMPA Laboratory, Department of Mathematics, University of Jijel, Jijel, Algeria  
soumia\_ss@hotmail.fr

### **Abstract**

We deal in the present work, with the existence of solutions for differential inclusions governed by the subdifferential operators with time delay, in a separable Hilbert space. The set-valued perturbation which contains the delay is scalarly upper semicontinuous. We prove under a compactness condition on the perturbation, that there exists at least one absolutely continuous solution. Our existence result is obtained thanks to the one proved recently in [1] concerning a perturbed problem governed by the subdifferential operator whose perturbation is a set-valued map without delay and via a discretization method (see [2]).

**Keywords:** Differential inclusions, subdifferential operator, set-valued map, finite delay, perturbation, scalarly upper semicontinuous, integrable function, absolutely continuous map

### **REFERENCES**

1. Soumia Saïdi and Mustapha Yarou, Set-valued perturbation for time dependent subdifferential operator, *Topol. Methods Nonlinear Anal.*, Vol :46 No :1, 447–470, 2015.
2. Soumia Saïdi and Mustapha Yarou, Delay perturbation of an evolution problem involving subdifferential operator, *J. Nonlinear Convex Anal.*, Vol :17 No:7, 1363–1379, 2016.

## **COMBINING CRYPTOGRAPHY WITH STEGANOGRAPHY**

**Muharrem Tuncay GENÇOĞLU**

Vocational School of Technical Sciences, Firat University, Elazig, Turkey  
mtgencoglu23@gmail.com

### **Abstract**

In this study, a different cryptographic method is introduced by using Power series transform, codes of ASCII and science of steganographi. Here, we produce a new algorithm for cryptology, we use Expanded Laplace transformation of the exponential function for encrypting the plain text and we use codes of ASCII for support to the confidentiality of the chipertext. After, Chipertext have embedded by steganographic method in another plaintext to hide the existence of chipertext. We show corresponding inverse of Power Series transform for decryption.

**Keywords:** Cryptology, Encryption, Decryption, Laplace Transform, ASCII, Steganograph

### **REFERENCES**

1. Aydın, M., Gökmen, G., Kuryel, B., Gündüz, G. Diferansiyel Denklemler ve Uygulamaları(1990), Barış Yayınları. SS 332-349.
2. Koç, Ç.K., CryptographicEngineering (2009), Springer. PP 125-128.
3. Belgacem, F.B.M., Karaballi, A.A., Kalla, L.S. Analytical Investigations of the Sumudu Transform and Applications to Integral Productions Equations, Mathematical Problems in Engineering (2003), No: 3,103-118.
4. Gençoğlu, M.T., Use of Integral Transform in Cryptology.Science and Eng. J of Firat Univ. (2016), 28(2), 217-220.
6. <https://tr.wikipedia.org/wiki/ASCII>
- 7.Martin, K.M., Everyday Cryptography Fundamental Principles and Applications (2012), Oxford University Press.

## **MISTAKES AND MISCONCEPTION ABOUT “ZERO” IN SOME TOPICS OF MATHEMATICS FOR 8TH GRADERS IN YENIMAHALLE, ANKARA**

**Sebahat Yetim Karaca and Özgür Altoğ**

Department of Mathematics, University of Gazi, Ankara, Turkey  
sebahat@gazi.edu.tr , ozguraltug06@gmail.com

### **Abstract**

In this investigation, we targetted to take attention to the number ‘zero’ that differs in many topics throughout the primary education period and tried to determine the mistakes and misconceptions that the 8th graders make about the concept of ‘zero’. This research aims to identify if students make mistakes and misconceptions regarding the number zero, i.e. its’ being a natural, rational number, if it is a positive or negative number. Mistakes and misconceptions of students in solution of equations in cases where the variable on each side of the equation is eliminated have been examined. Mistakes and misconceptions of students for “zero” such as “ $a^0$ ”, “ $1/0$ ” on which even the teacher candidates make mistakes in the previous researches, have been studied. In the investigation, the students have been found to have many mistakes and misconceptions about the number ‘zero’ and some suggestions have been made on these mistakes and misconceptions by researchers.

**Keywords:** Zero, numbers, mistakes, misconceptions, mistakes and misconceptions about the number ‘zero’.

### **REFERENCES**

1. Ifrah, G. (1985). Rakamların evrensel tarihi v : sıfırın gücü. (K. Dinçer, Ed.). 5. Baskı. İstanbul: TÜBİTAK.
2. MEB. (2009). İlköğretim matematik dersi 1-5. sınıflar öğretim programı ve kılavuzu. Ankara: MEB.
3. MEB. (2009). İlköğretim matematik dersi 6-8. sınıflar öğretim programı ve kılavuzu. Ankara: MEB.





# ON THE EXACT SOLUTIONS OF THE FRACTIONAL (2+1)- DIMENSIONAL DAVEY-STEWARTSON EQUATION SYSTEM

Gülnur Yel<sup>1</sup>, Zeynep Fidan Koçak<sup>2</sup>

<sup>1</sup> Department of Mathematics Education, Final International University, Kyrenia, TRNC

<sup>2</sup> Department of Mathematics, University of Mugla Sıtkı Koçman, Mugla, Turkey,

gulnuryel33@gmail.com, zkocak@mu.edu.tr

## Abstract

In this study, we construct the exact traveling wave solutions of the fractional (2+1)-dimensional Davey-Stewartson equation system (D-S) that is complex equation system using the Modified Trial Equation Method (MTEM). We obtained trigonometric function solutions by this method that are newly in literature.

**Keywords:** Modified trial equation method, The fractional (2+1)-dimensional Davey-Stewartson equation system, Trigonometric function solutions.

## REFERENCES

1. Kocak, Z. F., Bulut, H., and Yel, G. (2014) The solution of fractional wave equation by using modified trial equation method and homotopy analysis method, AIP Conference Proceedings, Vol. 1637, 504-512.
2. Bulut, H., Baskonus, H. M., and Pandir, Y. (2013) The modified trial equation method for fractional wave equation and time fractional generalized Burgers equation, Abstract and Applied Analysis, 1-8.
3. Bulut, H., and Pandir, Y. (2013) Modified trial equation method to the non-linear fractional Sharma–Tasso–Oleiver equation, International Journal of Modeling and Optimization, 3(4), 353-357.
4. Atangana, A., (2016), On the new fractional derivative and application to nonlinear Fisher's reaction-diffusion equation, Applied Mathematics and Computation, **273**, 948-956.
5. Atangana, A., Baleanu, D., (2016), New fractional derivatives with nonlocal and non-singular kernel: Theory and application to heat transfer model, Thermal Science, **1**,763–769.

## **EMULATE ARTIFICIAL NEURAL NETWORK TO MAKE A DECISION IN WIRELESS SENSOR**

**Fouad ESSAHLAOUI, Ahmed EL ABBASSI, Rachid SKOURI**  
Department of Physics, My Ismail University, Morocco.  
essahlaouifouad@gmail.com

### **Abstract**

This study presents an Artificial Neural Network Implementation in Arduino Board, simulated Network with Proteus ISIS. Artificial Neurons Network (ANN) is used in the decision and control of dynamic systems which can be with a lack of superfluous information which forces the use of fuzzy logic. The network presents a feed-forward Backpropagation Network. It is the best general purpose network for either supervised or unsupervised learning. The back-propagation algorithm generates a weight for all nodes in the networks, to minimize absolute error committed in fusion data, As the structure used by human being able to reason and not repeat errors. The write-up provided here gives an overview of artificial neural networks, details of the sketch, it's an introduction to some of the basic concepts employed in feed forward networks and the backpropagation algorithm. Its main applications include temperature, humidity, gas sensor and other types of data monitoring, factory automation, home automation, remote monitoring and home device control or surrounding environment to make an exact decision in short time.

**Keywords:** Multi-Sensor, Wireless Signal, Embedded Systems, Emulate, Arduino, Neral Network, Backpropagation.

### **REFERENCES**

1. M. Bouamar and M. Ladjal, "Système multicapteur utilisant les réseaux de neurones artificiels pour la surveillance des eaux potables," in 4th International Conference: Sciences of Electronic, Technologies of Information and Telecommunications, LASS, Laboratoire d'Analyse des Signaux et Systèmes, Université de Msila, Algérie, 2007, pp. 25–29.
2. M. D. Abdellah, "Répartition économique de l'énergie électrique utilisant les techniques d'intelligence artificielle," Université Mentouri de Constantine, 2010. [Online]. Available: <http://bu.umc.edu.dz/theses/electrotec/DRA5240.pdf>

## **GAIN SCHEDULING LINEAR MODEL OF AN ELECTRO-HYDRAULIC ACTUATOR**

**Cem Onat, Mahmut Daskin, Abdullah Turan**

Department of Mechanical Engineering, Inonu University, Malatya, Turkey

cem.onat@inonu.edu.tr, mahmut.daskin@inonu.edu.tr, abduallah.turan@inonu.edu.tr

### **Abstract**

In different industrial processes where position and force control are desired, electro-hydraulic systems have a widespread area of utilization. Models of the electro-hydraulic systems include high order nonlinearity. In this study, a gain scheduling linear model corresponded with nonlinear model of a hydraulic force actuator system is developed. The proposed model is constituted in two distinct and consecutive stages. In first step, nonlinear terms caused to nonlinearity are described by means of measurable or observable system parameters and embedded in a nonlinear scheduling parameter. Thus, the scheduling parameter is continuously extracted from real system. In second step, the nonlinear system equation is rearranged by the scheduling parameter and, parameter varying linear model is obtained. The simulations which are performed by using of Matlab-Simulink computer program show that the proposed model rightly fits to the nonlinear system model.

**Keywords:** Nonlinear model; Electro-Hydraulic System; Parameter varying, Gain scheduling.

### **REFERENCES**

1. Anthony Esposito, Fluid Power with Application. Prentice Hall International, Englewood Cliffs Editions Ltd.,1994.
2. Garret A. Sohl, James E. Bobrow, Experiments and Simulations On the Nonlinear Control of a Hydraulic System, IEEE Trans. Control Syst. Technol., Vol: 7, No:2, 238–247, 1999.
3. Ali Volkan Akkaya , Saban Çetin, Self tuning fuzzy logic control of a hydraulically actuating system, Proceedings of 2nd International Conference on Intelligent Knowledge Systems, 154–158 2005.

## **MATHEMATICAL MODELING OF THE SYNTHESIS OF NEW MATERIALS**

**Valery Antonov<sup>1</sup>, Roman Davidov<sup>1</sup>, Nikolay Kalinin<sup>2</sup>, Alexey Rjahovski<sup>2</sup>**

<sup>1</sup> Department of Mathematics, Peter the Great St. Petersburg Polytechnic University, Russia  
antonovvi@mail.ru, romanvproze@gmail.com

<sup>2</sup> Joffe Physical-Technical Institution Russian Academy of Science, Saint-Petersburg, Russia  
nvkalinin@rambler.ru, alexey.i.ryakhovskiy@mail.ioffe.ru

### **Abstract**

The aim of this work is developing a mathematical model of the sharp changes in the phase state of a substance. To construct a mathematical model, a phenomenological method of thermal dynamics, magnetic hydrodynamics (MHD) and statistical physics has been created. This approach allows developing a model which can be efficiently used to describe the processes of heat and mass transfer during the inelastic deformation of materials. An important step in the work is an application of the above models to describe the processes of phase formation during certain transformations of the solid phase of materials.

It is equally important to determine the role of the chemical reactions as one of the most effective methods of phase formation control in polycrystalline systems. Given the above, it is believed that the use of this approach can create models adequately describing the process of changing the state of matter as a result of the high-energy supply in a short period of time.

An important step in modelling is to create the equation of state. The most promising for this class of problems is to use the free energy of the system, taking into account various interaction factors between the particles.

**Keywords:** Mathematical model, inelastic deformation of materials, equation of state.

### **REFERENCES**

1. V. Antonov. Mathematical models of thermal energy processes. Lambert Academic Publishing. 2012.
2. R. V. Davydov, V. I. Antonov, T. I. Davydova. Simulation of laser ablation of metals for nanoparticles production. International Journal of Modern Physics: Conference Series, Vol. 41 (2016).

## A NEW APPROACH TO INTERVAL MATHEMATICAL MODEL AND APPLICATIONS

Obaid Algahtani

Department of Mathematics, King Saud University, Saudi Arabia

obalgahtani@ksu.edu.sa,

### Abstract

An interval may be defined as a convex combination as follows:

$$I = [a, b] = \{x_\alpha = (1 - \alpha)a + \alpha b : \alpha \in [0, 1]\}.$$

Consequently, we may adopt interval operations by applying the scalar operation point-wise to the corresponding interval points:

$$I \cdot J = \{x_\alpha \cdot y_\alpha : \alpha \in [0, 1], x_\alpha \in I, y_\alpha \in J\},$$

with the usual restriction  $0 \notin J$  if  $\cdot = \div$ . These operations are associative:

$$I + (J + K) = (I + J) + K,$$

$$I * (J * K) = (I * J) * K.$$

These two properties, which are missing in the usual interval operations, will enable the extension of the usual linear system concepts to the interval setting in a seamless manner. The arithmetic introduced here avoids such vague terms as "interval extension", "inclusion function", determinants which we encounter in the engineering literature that deal with interval linear systems. On the other hand, these definitions were motivated by our attempt to arrive at a definition of interval random variables and investigate the corresponding statistical properties. We feel that they are the natural ones to handle interval systems.

We will enable the extension of many results from usual state space models to interval state space models.

**Keywords:** Interval Analysis, Interval Matrices, State Space Model, Kalman Filter.

### REFERENCES

1. O. Al-Gahtani, J. Al-Mutawa, M. El-Gebeily, R. Agarwal, The interval versions of the Kalman Filter and the EM algorithm, *Advanced in Difference Equations*, 2012.

## **SOME WAVE SIMULATION PROPERTIES OF THE (2+1) DIMENSIONAL BREAKING SOLUTION EQUATION**

**Emine Nesligül Aksan<sup>1</sup>, Hasan Bulut<sup>2</sup>, Miraç Kayhan<sup>3</sup>**

<sup>1,3</sup> Department of Mathematics, University of İnönü, Malatya, Turkey

<sup>2</sup> Department of Mathematics, University of Fırat, Elâzığ, Turkey

mirackayhan@yandex.com, nesligul.aksan@inonu.edu.tr, hbulut@firat.edu.tr

### **Abstract**

In this study, we apply an effective method which is improved Bernoulli sub-equation function method (IBSEFM) to (2+1) dimensional Breaking Solution equation. It gives some new wave simulations such as complex and exponential structures. We check up whether all structures verify the (2+1) dimensional Breaking Solution model. Then, we plot three and two dimensional surfaces to obtained solutions by using Wolfram Mathematica 9.

**Keywords:** Improved Bernoulli function method; Breaking Solution; Complex exponential; wave simulate.

### **REFERENCES**

1. M. T. Darvishi, M. Najafi, Some exact solutions of the (2+1)-dimensional breaking soliton equation using the three-wave method. World Academy of Science, Engineering and Technology, Volume 55, 919–922, 2011.
2. M. T. Darvishi, M. Najafi, He's variational method for a (2 +1)-dimensional soliton equation. International Journal of Applied Mathematical Research, Volume 1, Issue 1, 1-7, 2012.
3. A. Giese, R. Bjerkving, M. Westphal, J. Clin. Oncol, 21(8), 1624, 2003.
4. A. H. Bhrawy, M. A. Abdelkawy, A. Biswas, Topological soli-tons and cnoidal waves to a few nonlinear wave equations in the-oretical physics. Indian Journal of Physics, Volume 87, Issue 11, 1125–1131, 2013.

## **REVIEW AND CLASSIFICATIONS OF THE RIDGE PARAMETER ESTIMATION TECHNIQUES**

**Adewale F. Lukman, Kayode Ayinde**

Department of Statistics, Ladoké Akintola University of Technology, Nigeria

wale3005@yahoo.com, kayinde@lautech.edu.ng

### **Abstract**

Ridge parameter estimation techniques under the influence of multicollinearity in linear regression model were reviewed and classified into different forms and various types. The different forms are Fixed Maximum (FM), Varying Maximum (VM), Arithmetic Mean (AM), Geometric Mean (GM), Harmonic Mean (HM) and Median (M) and the various types are Original (O), Reciprocal (R), Square Root (SR) and Reciprocal of Square Root (RSR). These classifications resulted into proposing some other techniques of Ridge parameter estimation. Investigation of the existing and proposed ones were done by conducting 1000 Monte-Carlo experiments under five (5) levels of multicollinearity ( $\rho = 0.8, 0.9, 0.95, 0.99, 0.999$ ), three (3) levels of error variance ( $\sigma^2 = 0.25, 1, 25$ ) and five levels of sample size ( $n = 10, 20, 30, 40, 50$ ). The relative efficiency ( $RF \leq 0.75$ ) of the techniques resulting from the ratio of their mean square error and that of the ordinary least square was used to compare the techniques. Results show that the proposed techniques perform better than the existing ones in some situations; and that the best technique is generally the ridge parameter in the form of Harmonic Mean, Fixed Maximum and Varying Maximum in their Original and Square Root types.

**Keywords:** Linear Regression Model, Multicollinearity, Ridge Parameter Estimation Techniques, Relative, Efficiency.

### **REFERENCES**

1. Alkhamisi, M., Khalaf, G. and Shukur, G. Some modifications for choosing ridge parameters. Communications in Statistics- Theory and Methods, 35(11), 2005-2020, 2006.
2. Gibbons, D. G. A simulation study of some ridge estimators. Journal of the American Statistical Association, 76, 131-139, 1981.

# INVESTIGATION OF INDUCTION MOTORS MEDIUM VOLTAGE GRID CONNECTED POWER SYSTEM STABILITY ANALYSIS

**Samet KOYUNCU, Gökhan BAHADIR**

Department of Electricity, University of Kastamonu, Kastamonu, Turkey

skoyuncu@kastamonu.edu.tr, gbahadir@kastamonu.edu.tr

## **Abstract**

Package software that can view power systems from many aspects and meet the needs are developed and made ready for personal use. For example, the analysis of power systems according to their different operating and working types can be made by such programs like Matlab/Simulink, Neplan, Pscad, Etap, and Digsilent. Nearly all of these programs, results are either shown visually or just numeric results are delivered to users without showing the process. These results provide preliminary information about the system in analyzing the complex power systems to operators, operating engineers, and working crafts.

In this research, stability analysis of medium voltage, on grid, induction motor at the takeoff time is viewed with Etap program. Some charts are created such as voltage-time, power-time, moment-time according to dynamic and statical analysis mentioned the engineering system analysis. It is impossible to make these analyses with classic calculation methods. And that makes developing computer based solution methods necessary in analyzing power systems

**Keywords:** Motor Starting Analysis, Etap, System Stability

## **REFERENCES**

1. TÜRKER, T., Güç Sistem Analizlerinin Enerji Verimliliğe Etkileri 6. Enerji Verimliliği, Kalitesi Sempozyumu, Kocaeli: EMO (2015)



## NUMERICAL BEHAVIOR OF SINGULAR TWO- POINT BOUNDARY VALUE PROBLEMS IN A COMPARATIVE WAY

**Selmahan Selim, Gozde Elver, Murat Sari**

Department of Mathematics, Faculty of Arts and Science, Yildiz Technical University,  
Istanbul, Turkey  
sarim@yildiz.edu.tr

### **Abstract**

This study concentrates on discovering numerical behavior of the singular two-point boundary value problems through various numerical techniques. This is carried out in a comparative way by mainly using differential quadrature and finite element methods. Also a discussion has been done by means of advantages and disadvantages of the numerical methods of interest. To properly understand the behavior of the physical processes represented by the model equation, the calculated solutions have been discussed in detail.

**Keywords:** Singular two-point boundary value problems, differential quadrature method, finite element method, physical behavior

### **REFERENCES**

1. U. Yucel, M. Sari, Differential quadrature method for a class of singular two-point boundary value problems, *International Journal of Computer Mathematics*, 86 (209) 465-475.
2. C. Shu, *Differential Quadrature and its Application in Engineering*, Springer-Verlag, London, 2000.
3. M. Kumar, A three-point finite difference method for a class of singular two-point boundary value problems, *J. Comput. Appl. Math.* 145 (2002) 89-97.
4. M. Bayraktar, Solution of Burgers equation using Petrov-Galerkin Finite element method, M.Sc. Thesis, Pamukkale University, 2017.

# **ROBUST SPEED OBSERVER FOR MECHANICAL SYSTEMS WITH NON-HOLONOMIC CONSTRAINTS**

**Ammar Touati Brahim, Madjid Kidouche**

Department of automation, University of Bumerdes, Bumerdes, Algeria

ammartouati@yahoo.fr

## **Abstract**

A robust speed observer for unconstrained perturbed mechanical systems has recently developed in [1]. It ensures the global convergence in spite of the presence of unknown disturbances. The observer has high dimension and requires the solution to certain integrals which cannot be derived explicitly a priori. We present in this study a globally convergent robust observer for perturbed mechanical systems with non-holonomic constraints. The mechanical model considered is more general which contains the systems with k-nonholonomic constraints. The observer derived is uniformly globally asymptotically stable with only two states in excess of full order which means that one half of the observer states in [1] are removed. Observer is given by explicit expressions and does not require any solutions of integrals. The effectiveness of this approach is demonstrated through the resultants simulations.

**Keywords:** Speed observer, immersion and invariance; unknown disturbances; robust observer.

## **REFERENCES**

1. Jose Guadalupe Romero, Romero Ortega, Two Globally Convergent Adaptive Speed Observers for Mechanical Systems, Automatica, doi: 10.1016/j.2015.06.032.

# SOLUTIONS OF DIFFERENTIAL EQUATIONS THROUGH MONTE CARLO ALGORITHMS

**Hande Uslu, Murat Sari**

Department of Mathematics, Faculty of Arts and Science, Yildiz Technical University,  
Istanbul, Turkey  
sarim@yildiz.edu.tr

## **Abstract**

This study aims at effectively producing solutions of ordinary differential equations through the Monte Carlo simulation algorithms. The Monte Carlo simulation is an approach analysing problems encountered in broad range of science. The simulation algorithm is considered to find out solutions of some optional equations. In the light of those issues, we also have opportunity to discuss what a stochastic model is. For the corresponding model, we will have a chance to figure out the ability and efficiency of the algorithm.

**Keywords:** Boundary value problem, Monte Carlo algorithm, differential equation, stochastic model

## **REFERENCES**

1. Akhtar, M.N., Durad, M.H., Ahmed, A., Solving Initial Value Ordinary Differential Equations by Monte Carlo Method, Proceedings of IAM, V.4, N.2, 2015, pp.149-174.
2. Farlow, Stanley J., Partial Differential Equations for Scientists and Engineers, Dover Publications, New York, 1993.
3. Glasserman, P., Monte Carlo Methods in Financial Engineering, Applications of Mathematics, Springer, 2003.
4. Rubinstein, R.Y., Simulation and the Monte Carlo Method, John Wiley and Sons, New York, 1981.
5. Zhong W., Z. Tian, Solving initial value problem of ordinary differential equations by Monte Carlo method in Multimedia Technology (ICMT), International Conference on 2011, IEEE.

# **TRANSIENT ANALYSIS WITH THE FOUR-STEP RUNGE-KUTTA METHOD OF INDUCTION MOTOR WITH MATLAB**

**Gökhan BAHADIR, Samet KOYUNCU**

Department of Electricity, University of Kastamonu, Kastamonu, Turkey

gbahadir@kastamonu.edu.tr, skoyuncu@kastamonu.edu.tr

## **Abstract**

In this study, Asynchronous Motor equations are converted to DQ axis equations. A state space model was constructed with these equations. State equations were analyzed using the Matlab m. file software using the Four-Step Runge Kutta Method. In this way, the asynchronous motor transients are displayed on the graph screen and their behavior is analyzed.

**Keywords:** Induction Motor, Four Step Runge Kutta Method, Matlab m-file

## **REFERENCES**

1. Arifoğlu, U. (2012), MATLAB 7.14 Simulink ve Mühendislik Uygulamaları, İstanbul, Alfa Basım Yayım Dağıtım.
2. Sarıoğlu, K (1995), Asenkron Makinalar ve Kontrolü, İstanbul, Birsen Yayınevi.

# **ELASTO-DYNAMIC RESPONSE OF CRACKED INFINITE ORTHOTROPIC ELASTIC STRIP UNDER IMPACT LOADING CONDITIONS**

**P. K. Mishra and S. Das**

Department of Mathematical Sciences, IIT(BHU), Varanasi, India

prshntmsr58@gmail.com

## **Abstract**

This study deals with the investigation of elasto-dynamic response of a finite crack embedded in an infinite orthotropic strip under suddenly applied stress. The crack is situated symmetrically and oriented in a direction normal to the edges of the strip. Integral transforms are employed to reduce the transient problem to a pair of dual integral equations in the Laplace transformed plane which are solved by iterations in the low frequency domain. To determine time dependence of the parameters, these equations are inverted to yield the analytical expressions of the dynamic stress intensity factor and crack opening displacement (COD). These physical quantities are calculated for different point loading given on the surface of the crack for the composite materials graphite epoxy and glass epoxy. The numerical values thus obtained are depicted through graphs for different particular cases.

**Keywords:** Orthotropic elastic strip; Impact response; Dynamic stress intensity factor.

## **REFERENCES**

1. Freund L. B., The stress intensity factor due to normal impact loading on the faces of a crack, *Int. J. Eng. Sci.*, 12, 179-189, 1974.
2. Kassir, M.K. and Bandopadhyay, K.K., Impact response of a cracked orthotropic medium, *ASME Journal of Applied Mechanics* 50, 630-636, 1983.
3. S. Itou, Dynamic stress intensity factors around two coplanar Griffith cracks in an orthotropic layer sandwiched between two isotropic elastic half planes, *Engng. Fract. Mech.* 34 (1989) 1085–1095.
4. Rubio-Gonzalez, C. and Mason, J. J., “Mixed mode dynamic stress intensity factor due to applied point loads”, *Computers and Structures* 76, 237-245, 2000.

# **SIMULATION OF TWO DIMENSIONAL SHALLOW WATER EQUATIONS WITH VARIABLE BOTTOM GEOMETRY USING FORCE METHOD**

**R. K. Gupta and L. P. Singh**

Department of Mathematical Sciences, Indian Institute of Technology, Banaras Hindu  
University, Varanasi, India

rkgupta.rs.apm12@itbhu.ac.in

## **Abstract**

In the present study, the FORCE scheme has been used for the numerical solution of two dimensional shallow water equations with variable bottom geometry. Firstly, the one dimensional equations are solved and the source term is treated using time operator splitting. The method is then extended to two dimensional problem using space operator splitting. The method is applied to the various test problems in one and two dimensions. The results obtained are validated with the earlier works. It was observed that the FORCE method works faithfully to the real life problems but the treatment of source term depends upon the geometry of the problem.

**Keywords:**Force Method; Shallow Water Equations;Bottom Geometry.

## **REFERENCES**

1. S K Godunov, A finite difference method for the computation of discontinuous solutions of the equations of fluid dynamics, *Mater Sb*1959;47:357–393.
2. J Murillo, P García-Navarro, Augmented versions of the HLL and HLLC Riemann solvers including source terms in one and two dimensions for shallow flow applications. *Journal of Computational Physics*, 2012;231:6861–6906
3. Himanshu Gupta, L P Singh, Simulation of Dam-Break Problem using Random Choice Method, *Computers & Fluids* 2015;111:187–196.
4. Phillip Collela, Glimm's Method For Gas Dynamics, *SIAM J Sci STAT COMPUT* 1982;3(1):76-110.

## ON A NONLINEAR EIGENVALUE PROBLEM IN MUSIELAK-ORLICZ SPACES

M. Rhoudaf and H. Sabiki

Annaysis laboratory, Geometry and Applications, Faculty of Sciences, BP 133 Kenitra 14000,  
Morocco

sabikihajar@gmail.com

### Abstract

We consider the eigenvalue problem in an arbitrary Musielak-Orlicz space. We show that the existence of an eigenvalue can be derived from a generalized version of Lagrange multiplier rule.

**Keywords:** Eigenvalue problem, Musielak Orlicz spaces, Nonlinear elliptic problems

### REFERENCES

1. J. Musielak, Orlicz Spaces and Modular Spaces, Lecture Notes in Mathematics, Vol. 1034, Springer, Berlin, 1983.
2. J. P. Gossez and R. Mansevich, On a nonlinear eigenvalue problem in Orlicz-Sobolev spaces, Proceedings of the Royal Society of Edinburgh: Section A Mathematics, 132(4), pp. 891-909.
3. M. Tienari, Ljusternik-Schnirelman theorem for the generalized laplacian, J. Diff. Equat., 161 (2000), 174-190.

## **CRYPTANALYSIS OF APPLICATION OF LAPLACE TRANSFORM FOR CRYPTOGRAPHY**

**M.Tuncay GENÇOĞLU**

Vocational School of Technical Sciences, University of Firat, Elazig, Turkey

mt.gencoglu@firat.edu.tr

### **Abstract**

Although Laplace Transform is a good application field in the design of cryptosystems, many encryption algorithm proposals become unsatisfactory for secure communication since cryptanalysis studies are not sufficient. One of the important factors resulting in poor proposals is the fact that security analysis of the proposed encryption algorithms is performed with only statistical tests and experimental results. In this study, a general attack scenario was given in order to conduct security analyses of Laplace Transform based cryptosystems. The application of proposed general attack scenario was shown on recently proposed Laplace Transform based encryption scheme.

**Keywords:**Laplace Transform; Cryptography; Cryptanalysis; A general attack scenario.

### **REFERENCES**

1. Bodkhe D.S, Panchal S.K. Use of Sumudu Transform in Cryptography, Bulletin of the Marathwada Mathematical society, 16/2: 1-6,2015.
2. Hiwarekar A.P. A new method of cryptography using Laplace transform, International Journal of Mathematical Archive, 3/3: 1193-1197,2012.
3. Hiwarekar A.P. Application of Laplace Transform for Cryptography, International Journal of Engineering and Science, 5/4: 129-135,2015.
4. Lakshmi G.N, Kumar B.R, Sekhar A.C. A cryptographic scheme of Laplace transforms, International Journal of Mathematical Archive, 2/12: 2515-2519,2011.



## A NEW RELIABLE TREATMENT OF THE LANE-EMDEN TYPE EQUATIONS

Necdet Bildik, Sinan Deniz

Department of Mathematics, Manisa Celal Bayar University, Manisa, Turkey

necdet.bildik@cbu.edu.tr, sinan.deniz@cbu.edu.tr

### Abstract

In this study, a new analytic approximate technique, namely the optimal perturbation iteration method, is presented. We applied this technique to singular initial value Lane-Emden type problems, which are nonlinear differential equations which represent many scientific phenomena in astrophysics and mathematical physics, to verify the effectuality and productivity of the method. This technique ensures us to control the convergence regions when necessary. Comparing different methods discovers that the proposed method is highly accurate and has great potential to be a new kind of powerful analytical tool for nonlinear differential equations.

**Keywords:** Optimal perturbation iteration method, delay differential equations, approximates solutions.

### REFERENCES

1. Yiğit Aksoy and Mehmet Pakdemirli. New perturbation–iteration solutions for bratu-type equations. *Computers & Mathematics with Applications*, 59(8):2802–2808, 2010
2. N. Herişanu and Vasile Marinca. Accurate analytical solutions to oscillators with discontinuities and fractional-power restoring force by means of the optimal homotopy asymptotic method. *Computers & Mathematics with Applications*, 60(6):1607{1615, 2010.
3. Deniz, Sinan, and Necdet Bildik. "Comparison of adomian decomposition method and Taylor matrix method in solving different kinds of partial differential equations." *International Journal of Modeling and Optimization* 4.4 (2014): 292.

# CERTAIN FRACTIONAL INTEGRALS AND SOLUTIONS OF FRACTIONAL KINETIC EQUATIONS INVOLVING THE PRODUCT OF S- FUNCTION

Mehar Chand<sup>1</sup>, Zakia Hammouch<sup>2</sup>, And Joshua Kiddy K. Asamoah<sup>3</sup>

<sup>1</sup>Department of Applied Sciences, Guru Kashi University, Bathinda-1513002 (India)

<sup>2</sup>Department of Mathematics Faculty of Sciences and Techniques,  
Moulay Ismail University Errachidia 52000, Morocco

<sup>3</sup>African Institute for Mathematical Sciences, Biriwa-Ghana.

mehar.jallandhra@gmail.com

## Abstract

In this study, our main objective is to establish certain new fractional integral by applying the Saigo hypergeometric fractional integral operators and by employing some integral transforms on the resulting formulas, we presented their image formulas involving the product of S-function. Furthermore, We develop a new and further generalized form of the fractional kinetic equation involving the product of S-function. The manifold generality of the S-function is discussed in terms of the solution of the fractional kinetic equation and their graphical interpretation is interpreted in the present study. The results obtained here are quite general in nature and capable of yielding a very large number of known and (presumably) new results.

**Keywords:** Saigo hypergeometric fractional integral operators, fractional kinetic equation, S-function.

## REFERENCES

1. Wang, Guotao, Praveen Agarwal, and Mehar Chand. "Certain Grüss type inequalities involving the generalized fractional integral operator." *Journal of Inequalities and Applications* 2014.1 (2014): 147.
2. Agarwal, Praveen, et al. "Certain integrals involving the generalized hypergeometric function and the Laguerre polynomials. *Journal of Computational and Applied Mathematics* 313 (2017): 307-317.



# COMBINATION OF LIE TRANSFORMATIONS AND AUXILIARY EQUATION METHOD FOR A CLASS OF NEW KDV-BURGERS-KURAMOTO TYPE EQUATION

Zehra Pinar

Department of Mathematics, Namık Kemal University, Tekirdağ, Turkey

zpinar@nku.edu.tr

## Abstract

For engineering and science, the analytical solutions of nonlinear partial differential equations are important. Therefore, transformations are the most important tools. Generally, the wave transformation, which is also one of the group transformations, is used for the analytical methods. In this work, we consider a class of new KdV-Burgers-Kuramoto type equation and the solutions of the equation are obtained via based on analytical methods where instead of wave transformations, group transformations are proposed. With the group transformations, analytic solutions can be obtained via Auxiliary equation method.

**Keywords:**A class of new KdV-Burgers-Kuramoto type equation; group transformations; Auxiliary equation method.

## REFERENCES

1. Wazwaz, A.M., The tanh and the sine-cosine methods for a reliable treatment of the modified equal width equation and its variants, Commun Non-linear Sci. Numer. Simul., 11:148-160, 2006.
2. Ma, S. H., Peng, J. and Zhang, C., New exact solutions of the (2+1)-dimensional breaking soliton system via an extended mapping method, Chaos, Solitons and Fractals, 46:210-214,2009.
3. Z. Pinar, T. Ozis, An Observation on the Periodic Solutions to nonlinear Physical models by means of the auxiliary equation with a sixth-degree nonlinear term, Commun Nonlinear Sci Numer Simulat, 18, 2177-2187,2013.

## **HIDDEN SYMMETRIES WITHIN SOME NEW DERIVATIVES**

**Ozlem Defterli**

Department of Mathematics, Çankaya University, Ankara, Turkey

defterli@cankaya.edu.tr

### **Abstract**

In this study, the generic (standard) and non-generic (hidden) symmetries of the extended Lagrangians are investigated for the geometries induced by the extended Lagrangian belonging to the motion of a one-dimensional free particle. The standard and hidden symmetries of the induced two-dimensional manifolds within conformable derivative are reported.

**Keywords:** Killing vectors; Killing-Yano tensors; Conformable derivative; Lagrangian.

### **REFERENCES**

1. Dumitru Baleanu, Ozlem Defterli, Killing-Yano tensors and angular momentum, Czechoslovak Journal of Physics, Vol: 54, Issue: 2, 157-165, 2004.
2. Ozlem Defterli, Dumitru Baleanu, Killing-Yano tensors and superintegrable systems, Czechoslovak Journal of Physics, Vol: 54, Issue: 11, 1215-1221, 2004.
3. Dumitru Baleanu, Ozlem Defterli, Killing-Yano tensors, surface terms and superintegrable systems, Global Analysis and Applied Mathematics, AIP Conference Proceedings, 729, 99-105, 2004.
4. Ehab Malkawi, Dumitru Baleanu, Fractional Killing-Yano Tensors and Killing Vectors Using the Caputo Derivative in Some One- and Two-Dimensional Curved Space, Abstract and Applied Analysis, Article Number: 290694, 2014.
5. Thabet Abdeljawad, On conformable fractional calculus, Journal of Computational and Applied Mathematics, Vol: 279, 57-66, 2015.
6. Douglas R. Anderson, Darin J. Ulness, Newly Defined Conformable Derivatives, Advances in Dynamical Systems and Applications, Vol: 10, No: 2, 109-137, 2015.

## A NOTE ON STURM-LIOUVILLE PROBLEM FOR DIFFERENCE EQUATIONS

Erdal Bas, Ramazan Ozarslan

Department of Mathematics, University of Firat, Elazig, Turkey

erdalmat@yahoo.com

### Abstract

In this study, Sturm-Liouville problem, with variable potential function  $q(n)$ , for difference equations is taken into consideration as follows

$$\Delta^2 x(n-1) + q(n)x(n) + \lambda x(n) = 0, n = a, \dots, b, \quad (1)$$

$$x(a-1) + hx(a) = 0, \quad (2)$$

$$x(b-1) + kx(b) = 0, \quad (3)$$

where  $a, b$  are finite integers with  $a \geq 0$ ;  $a \leq b$ ,  $h$  is a real number,  $\Delta$  is the forward difference operator,  $\Delta x(n) = x(n+1) - x(n)$ ,  $\lambda$  is the spectral parameter,  $q(n)$  is a real valued potential function for  $n \in [a, b]$ ;  $n$  is a finite integer. The sum representations of solutions are found. It is shown that these results satisfy the equation by using summation by parts. Asymptotic formulas for eigenfunctions are given.

**Keywords:** Sturm-Liouville, Casoratian, difference equation, eigenfunction, asymptotic formula.

### REFERENCES

1. W.G. Kelley, A.C. Peterson, Difference Equations: An Introduction with Applications, Academic Press, San Diego (2001).
2. B.M. Levitan, I.S. Sargsjan, Introduction to Spectral Theory: Selfadjoint Ordinary Differential Operators, American Mathematical Society, Providence Rhode Island 5-8, 1975.
3. E.S. Panakhov, E. Bas, A New Approximation For Singular Inverse Sturm-Liouville Problem, Thai Journal of Mathematics, 58,147-154, 2012.
4. M. Adivar, E. Bairamov Spectral Properties of Non-selfadjoint Difference Operators, Journal of Mathematical Analysis and Applications 261, 461-478, 2001.
5. F.V. Atkinson, Discrete and Continuous Boundary Value Problems, Academic Press Newyork (1964).

## NOVEL HYPERBOLIC BEHAVIORS TO SOME IMPORTANT MODELS ARISING IN QUANTUM SCIENCE

Hasan Bulut<sup>1</sup>, Tukur Abdulkadir Sulaiman<sup>2</sup>, Hacı Mehmet Baskonus<sup>3</sup>, Tugba Yazgan<sup>4</sup>

<sup>1, 2, 4</sup> Department of Mathematics, University of Firat, Elazig, Turkey

<sup>2</sup> Department of Mathematics, Federal University, Dutse, Jigawa, Nigeria

<sup>3</sup> Department of Computer Engineering, Munzur University, Tunceli, Turkey

<sup>1</sup>hbulut@firat.edu.tr, <sup>2</sup>sulaiman.tukur@fud.edu.ng

<sup>3</sup>hmbaskonus@gmail.com, <sup>4</sup>tubayzgn01@gmail.com

### Abstract

In this study, with the help of Wolfram Mathematica 9, sine-Gordon expansion method is used in constructing new hyperbolic function solutions to the two-well-known nonlinear differential equations that arises in nonlinear science, namely; the modified Zakharov-Kuznetsov (mZK) and the (2+1)-dimensional cubic Klein-Gordon (cKG) equations. We also plot the two- and three-dimensional graphics using the same computer program in the Wolfram Mathematica 9.

**Keywords:** The sine-Gordon expansion method; modified Zakharov-Kuznetsov equation; (2+1)-dimensional cubic Klein-Gordon equation; hyperbolic function solution

### REFERENCES

1. F. Tascan, A. Bekir and M. Koprان, Travelling Wave Solutions of Nonlinear Evolution Equations by Using the First Integral Method, Commun. Nonlinear Sci. Numer. Simulat., 14, 1810-1815, 2009.
2. H.M. Baskonus and H. Bulut, New Hyperbolic Function Solutions for Some Nonlinear Partial Differential Equations Arising in Mathematical Physics, Entropy, 17, 4255-4270, 2015.
3. H. Bulut, T.A. Sulaiman and H.M. Baskonus, New Solitary and Optical Wave Structures to the Korteweg-de Vries Equation with Dual-Power Law Nonlinearity, Opt. Quant. Electron, 48(564), 1-14, 2016.

# GENERALIZED CESÀRO SUMMABLE DIFFERENCE SEQUENCE SPACES AND THEIR DUAL SPACES

Mikail Et

Department of Mathematics, Firat University, Elazig, Turkey

mikaillet68@gmail.com

## Abstract

Et [3] introduced some type Cesàro difference sequence spaces  $C_p(\Delta^m)$  ( $1 \leq p < \infty$ ),  $C_\infty(\Delta^m)$  and determined their Köthe-Toeplitz duals. In this study we continue to examine others relations with related the the sequence spaces  $C_1(\Delta^m)$  and  $C_p(\Delta^m)$  and determine the  $\alpha$ -duals of the sequence space  $C_1(\Delta^m)$ .

**Keywords:** Difference Sequence, Cesàro Summability, Dual Spaces.

## REFERENCES

1. Bhardwaj V. K. and Gupta, S. Cesàro summable difference sequence space, J. Inequal. Appl. 2013, 2013:315, 9 pp.
2. Bhardwaj V. K. and Gupta, S. and Karan, R. Köthe-Toeplitz duals and matrix transformations of Cesàro difference sequence spaces of second order, J. Math. Anal. 5(2) (2014), 1-11.
3. Et, M. On some generalized Cesàro difference sequence spaces, İstanbul Üniv. Fen Fak. Mat. Derg. 55/56 (1996/97), 221-229.
4. Et, M. and Colak, R. On generalized difference sequence spaces, Soochow J. Math., 21(4) (1995), 377-386.
5. Ng, P. N. and Lee, P. Y. Cesàro sequence spaces of non-absolute type, Comment Math. 20 (1978), 429-433.
6. B.C. Tripathy, A. Esi and B. K. Tripathy, On a new type of generalized difference Cesaro Sequence spaces, Soochow J. Math. 31:3 (2005), 333-340.

# TRIGONOMETRIC FUNCTION SOLUTIONS OF FRACTIONAL DRINFELD'S SOKOLOV -WILSON SYSTEM

ZeynepFidan Koçak<sup>1</sup>, Gülnur Yel<sup>2</sup>

<sup>1</sup>Department of Mathematics, University of Mugla Sıtkı Koçman, Mugla, Turkey

<sup>2</sup>Department of Mathematics Education, Final International University, Kyrenia, TRNC

zfkocakt@gmail.com, gulnuryel33@gmail.com

## Abstract

In this study, we construct exact trigonometric solutions of the space-time fractional classical Drinfeld's Sokolov-Wilson system by Modified Trial Equation Method (MTEM). These solutions may explain some physical phenomena and lead to researchers in physics and engineering.

**Keywords:** Modified trial equation method, Fractional Drinfeld's Sokolov-Wilson system.

## REFERENCES

1. Shehata, A. R, Kamal, E. M and Kareem, H. A (2015) Solutions of the space-Time fractional of some nonlinear systems of partial differential equations using modified Kudryashov method, International Journal of Pure and Applied Mathematics, 101(4),477-487.
2. Drinfel'd, V.G., and Sokolov, V.V. (1981) Equations of Kortweg-de Vries type and simple lie algebras, Sov. Math. Dokl. 23, 457-462.
3. Koçak, Z. F., Bulut, H. and Yel, G. (2014) The Solution of Fractional Wave Equation by using Modified Trial Equation Method and Homotopy Analysis Method, AIP Conference Proceedings 1637, 504
4. Bulut, H., Baskonus, H. M., and Pandir, Y. (2013) The modified trial equation method for fractional wave equation and time fractional generalized Burgers equation, Abstract and Applied Analysis, vol. pp. 1-8.
5. Yel, G. (2016) On The Analytical and Numerical Solutions of Nonlinear Fractional Differential Equations, Ph. D Thesis, Mugla Sıtkı Koçman University, Mugla, 95 p.



## FRACTIONAL PROBLEM FOR DIFFUSION OPERATOR WITH IMPULSIVE CONDITION

Erdal BAS, Funda Metin TURK

Department of Mathematics, University of Firat, Elazig, Turkey

erdalmat@yahoo.com, fnd-44@hotmail.com

### Abstract

We consider fractional Sturm-Liouville problem for diffusion operator of order  $\alpha \in (1, 2]$  with impulsive boundary conditions,

$$-D^\alpha h(x) {}^c D^\alpha y(t) + (2\lambda p(t) + q(t))y(t) = 0$$

$$\Delta y|_{t=t_k} = I_k(y(t_k)), \quad \Delta y'|_{t=t_k} = I_k^*(y(t_k)), \quad t_k \in [0, \pi], \quad k = 1, \dots, n$$

$$\alpha_1 y(0) + \beta_1 y'(0) = 0, \quad \alpha_2 y(\pi) + \beta_2 y'(\pi) = 0$$

where  $I_k, I_k^* : \mathbb{R} \rightarrow \mathbb{R}$ ,  $\Delta y(t_k) = y(t_k^+) - y(t_k^-)$ ,  $y(t_k^+) = \lim_{h \rightarrow 0} y(t_k + h)$ . We provide representation of solution for this problem. By means of a fixed point theorem, the existence of solution for this problem is obtained. Our results are based on Schaefer fixed point theorem.

**Keywords.** Fractional; Sturm-Liouville; Impulsive.

### REFERENCES

1. P. Agarwal Ravi, Benchohra Mouffak, Attou Slimani Boualem, Existence Results for Differential Equations with Fractional Order and Impulses, *Memoirs on Differential Equations and Mathematical Physics*, Vol:44, 1-21, 2008.
2. Ahmad Bashir and J. Nicto Juan, Existence of Solutions for Impulsive Anti-Periodic Boudary Value Problems of Fractional Order, *Taiwanese Journal of Mathematics*, Vol:15, No:3, 981-993, 2011.
3. Erdal Bas, Funda Metin, Spectral Analysis for Fractional Hydrogen Atom Equation, *Advances in Pure Mathematics*, Vol:5, 767-773, 2015.

## **MODELING DISTRIBUTED WORKFLOW PROCESSES USING EXTENDED PETRI NETS**

**Mehmet Karay**

Department of Computer Engineering, Final International University, Kyrenia, TRNC

mehmet.karay@ufu.university

### **Abstract**

A manufacturing cell is a component of a distributed flexible manufacturing system at some factory. This component is itself a distributed subsystem. The contribution introduces modelling distributed workflow processes using extended Petri nets with the new construction which is the interruption routing. Petri nets notation is used for representation of the four main routing constructs as well as for the workflow process. In this study, four main routing construct and the new construct interruption explained and modeled by using extended Petri nets.

**Keywords:** Workflow, Workflow Building Blocks, Process Modelling, Routing Constructs; extended Petri nets.

### **REFERENCES**

1. Workflow Management Coalition: Workflow Management Coalition – Terminology & Glossary. Technical Report. Document Number WFMC-TC-1011 (1999).
2. W. M. P. van der Aalst, K. M van Hee: Workflow Management – Models, Methods, and Systems, The MIT Press, Cambridge, Massachusetts, London, England, 2002.
3. Hollingsworth, D.: Workflow Reference Model. Technical Report. The Workflow Management Coalition, Document Number WFMC-TC-1003 (1995).
4. Desrochers, A., and R. Ai-Jaar. 1995. *Applications of Petri Nets in Manufacturing Systems: Modeling, Control and Performance Analysis*. IEEE Press.
5. A. Kostin and Ilushechkina L, “Modeling and simulation of distributed systems”, *World Scientific Publ. Co.*, 2010.
6. T. Murata, Petri nets: Properties, Analysis and Applications, Proc. IEEE, vol. 77, no. 4, pp. 541 – 580, 1989.

## **NEW MULTIPLE SOLITON SOLUTIONS OF MODIFIED KDV-KP EQUATION**

**Yusuf Ali Tandogan, Yusuf Pandir**

Department of Mathematics, Bozok University, Yozgat, Turkey

yali.tandogan@bozok.edu.tr, yusuf.pandir@bozok.edu.tr

### **Abstract**

Many studies have been carried out on the creation of mathematical models of real life problems in the field of applied sciences. New solution functions have been tried to be obtained by means of methods developed for these nonlinear physical problems.

In this study, new generalized F-expansion method is used to obtain multiple soliton solutions of modified KdV-KP equation. With this proposed method, new combined and multiple soliton solutions have been found.

**Keywords:** New generalized F-expansion method; modified KdV-KP equation; multiple soliton solutions.

### **REFERENCES**

1. S. Zhang, T. Xia, A generalized F-expansion method with symbolic computation exactly solving Broer–Kaup equations, *Applied Mathematics and Computation*, 189, 949-955, 2007.
2. Yusuf Pandir, Nail Turhan, A new version of the generalized F-expansion method and its applications, *AIP Conference Proceedings*, 1798, 020122, 1-5, 2017.
3. A. M. Wazwaz, Solitons and singular solitons for the Gardner-KP equation, *Applied Mathematics and Computation*, 204, 162-169, 2008.
4. N. Taghizadeh, M. Mirzazadeh, F. Farahrooz, Exact soliton solutions of the modified KdV–KP equation and the Burgers–KP equation by using the first integral method, *Applied Mathematical Modelling*, 35(8), 3991-3997, 2011.
5. A. S. Al-Fhaid, New Exact Solutions for the Modified KdV-KP Equation Using the Extended F-Expansion Method, *Applied Mathematical Sciences*, 6(107), 5315 – 5332, 2012.

# OPTIMAL PERTURBATION ITERATION METHOD FOR SOLVING DELAY DIFFERENTIAL EQUATIONS

Sinan Deniz, Necdet Bildik

Department of Mathematics, Manisa Celal Bayar University, Manisa, Turkey

sinan.deniz@cbu.edu.tr, necdet.bildik@cbu.edu.tr

## Abstract

In this research, we have presented a new analytical technique, namely the optimal perturbation iteration method and have implemented this technique to delay differential equations to carry out an efficient algorithm for the new approximate solutions. We have also tested the accuracy and effectiveness of this method by various examples of linear and nonlinear problems of delay differential equations. Obtained results expose that optimal perturbation iteration algorithm is very effective, reliable, easy to use and simple to perform.

**Keywords:**Optimal perturbation iteration method, delay differential equations, approximate solutions

## REFERENCES

1. M. Khalid, Mariam Sultana, Faheem Zaidi, and Fareeha Sami Khan. Solving polluted lakes system by using perturbation-iteration method. *International Journal of Computer Applications*, 114(4), 2015.
2. N. Herişanu and Vasile Marinca. Accurate analytical solutions to oscillators with discontinuities and fractional-power restoring force by means of the optimal homotopy asymptotic method. *Computers & Mathematics with Applications*, 60(6):1607-1615, 2010.
3. N Bildik and S Deniz. Comparison of solutions of systems of delay differential equations using taylor collocation method, lambert w function and variational iteration method. *Scientia Iranica. Transaction D, Computer Science & Engineering, Electrical*, 22(3):1052, 2015.

# AN APPLICATION OF WEIERSTRASS TRANSFORMATION METHOD TO SOME NONLINEAR PHYSICAL PROBLEMS

Latife Gizem Kambur, Yusuf Gurefe

Department of Econometrics, Usak University, Usak, Turkey

latife.gizem.kambur@gmail.com, ygurefe@gmail.com

## Abstract

In this study, the extended Weierstrass transformation method, that is applied to construct the new wave solutions of some nonlinear partial differential equations such that Tzidzeica-Dodd-Bullough and Liouville equations, is considered. Thus, some new traveling wave solutions including the Weierstrass elliptic functions are obtained by using this novel method. So, these results can't be found in literature. Also, the behaviour of solutions is determined by two and three-dimensional graphics.

**Keywords:** Nonlinear problems; Soliton; Weierstrass elliptic functions, Exact solution.

## REFERENCES

1. Alfred Huber, The Calculation of Novel Class of Solutions of a Non-linear Fourth Order Evolution Equation by the Weierstrass Transform Method, Applied Mathematics and Computation, Vol:(1-2), No:201, 668–677, 2001.
2. Alfred Huber, A Novel Class of Solutions for a Non-linear Third Order Wave Equation Generated by the Weierstrass Transformation, Chaos, Solitons and Fractals, Vol:4, No:28, 972–978, 2006.
3. El-Said A. El-Wakil, Essam M. Abulwafa, Mohammed A. Abdou, Extended Weierstrass Transformation Method for Nonlinear Evolution Equations, Nonlinear Science Letters A: Mathematics, Physics and Mechanics, Vol:1, No:3, 253–262, 2010.
4. Yusuf Gurefe, Emine Misirli, Yusuf Pandir, Abdullah Sonmezoglu, Mehmet Ekici, New Exact Solutions of the Davey-Stewartson Equation with Power-Law Nonlinearity, Bulletin of the Malaysian Mathematical Sciences Society Vol:38, 1223–1234, 2015.

# **SPEED SENSORLESS VECTOR CONTROL WITH A STRATEGY OF LINEARIZATION BY STATE FEEDBACK OF INDUCTION MOTOR APPLIED MODEL REFERENCE ADAPTIVE SYSTEM**

A. Amrane<sup>1</sup>, A. Larabi<sup>1</sup>, M.S. Boucherit<sup>2</sup>

<sup>1</sup> Machines Drives Control Laboratory, USTHB BP. 32 El-Alia, Bab-Ezzouar, Algiers,  
Algeria

amraneahmed@gmail.com; larabiabdelkader@yahoo.fr

<sup>2</sup> Process Control Laboratory, ENP, BP. 182, 16200. El-Harrach, Algiers, Algeria  
ms\_boucherit@yahoo.fr

## **Abstract**

In this study, we show that the association of the fuzzy logic regulators with a control strategy using the linearization by return of state feedback by using fuzzy regulators for an induction machine without speed sensor, and with adaptation of the rotor resistance. The rotor speed is estimated by using the model reference adaptive system approach (MRAS). This method consists of using two models. The first one is the reference model and the second is an adjustable one in which two components of the stator flux, obtained from the measurement of the currents and stator voltages, are estimated. The estimated rotor speed is then obtained by canceling the difference between stator-flux of the model of reference and those of the adjustable model. This technique lends itself very well to the adjustment and has the badly controllable command of process by conventional traditional methods, and makes it possible to obtain a powerful and robust command with respect to uncertainties on the external parameters and disturbances.

**Keywords:** Asynchronous actuator, Fuzzy Logic Control, adaptive method with model of reference, Vector control.

## **REFERENCES**

1. Y. Kumsuwana, S. Premrudeepreechacharna, and H.A. Toliyat, Modified direct torque control method for induction motor drives based on amplitude and angle control of stator flux, *Electric Power Systems Research* 78 (2008) 1712–1718.
2. Mohammed T. Lazim, Muthanna J. M. Al-khishali, Ahmed Isa. Al-Shawi, Space Vector Modulation Direct Torque Speed Control of Induction Motor, *The 2nd International Conference on Ambient Systems, Networks and Technologies, Procedia Computer Science* 5, 2011, pp.505–512.
3. R. Toufouti, H. Benalla and S. Meziane, New Direct Torque Neuro-fuzzy Control Based SVM-Three Level Inverter-Fed Induction Motor, *International Journal of Control Automation, and System* (2010) 8(2):425-432.
4. A. Amrane, A. Larabi, A. Hamzaoui, 2014, Robust sensorless control of an induction machine based on a fuzzy MRAS, *International Conference on Electrical and Electronics Engineering (ICEEE 2014)* du 21-23 April, Antalya, Turquie.

## **STOCHASTIC RUNGE-KUTTA METHODS IN A GOMPERTZIAN STOCHASTIC MODEL**

**Tugcem PARTAL<sup>1</sup> , Mustafa BAYRAM<sup>2</sup>**

<sup>1</sup> Department of Mathematical Engineering, Yildiz Technical University, Istanbul, Turkey

<sup>2</sup> Department of Computer Engineering, University of Gelisim, Istanbul, Turkey

tpartal@yildiz.edu.tr, mbayram@gelisim.edu.tr

### **Abstract**

In this study, a Gompertzian stochastic model is introduced to describe the solid tumour growth. Explicit Runge-Kutta scheme of second order in the weak sense for the Gompertzian stochastic model is considered. Finally we demonstrate the accuracy by computing the errors in approximate solution for our model which have known exact solutions.

**Keywords:** Stochastic Runge-Kutta scheme, Stochastic differential equations

### **REFERENCES**

1. Folkman, J., The vascularization of tumors. *Scientific American*, 234(5), 58. 1976.
2. Ferrante, L., Bompadre, S., Possati, L., & Leone, L., Parameter estimation in a Gompertzian stochastic model for tumor growth. *Biometrics*, 56(4), 1076-1081, 2000.
3. Bassukas, I. D., Comparative Gompertzian analysis of alterations of tumor growth patterns. *Cancer research*, 54(16), 4385-4392, 1994.
4. Tocino, A., and Ardanuy, R., Runge–Kutta methods for numerical solution of stochastic differential equations. *Journal of Computational and Applied Mathematics*, 138(2), 219-241, 2002.
5. Rößler, A., Second order Runge–Kutta methods for Itô stochastic differential equations. *SIAM Journal on Numerical Analysis*, 47(3), 1713-1738, 2009.

# TAN (F(xi)/2) -EXPANSION METHOD FOR EXACT SOLUTIONS OF THE (2+1)-DIMENSIONAL POTENTIAL CALOGERO–BOGOYAVLENSKII–SCHIFF EQUATION

Rabar Mohammed Rasul<sup>1</sup>, Hasan Bulut<sup>2</sup>

<sup>1</sup> Raparin University, Faculty of Basic Education, Department of Mathematics, Iraq

<sup>2</sup> Firat University, Faculty of Science, Department of Mathematics, Turkey

math.rabar@gmail.com, hbulut@firat.edu.tr

## Abstract

In this study, with help of Wolfram Mathematica 9, we consider the  $\tan\left(\frac{F(\xi)}{2}\right)$ -expansion method for investigating the traveling wave solutions of the (2+1)-dimensional Calogero–Bogoyavlenskii–Schiff equation. We find some traveling wave solutions such as trigonometric, hyperbolic, exponential and rational function solutions. Then, we also plot the two- and three-dimensional graphics for some traveling wave solutions obtained in this study by using the same program in Wolfram Mathematica 9.

**Keywords:** (2+1)-dimensional Calogero–Bogoyavlenskii–Schiff equation;  $\tan\left(\frac{F(\xi)}{2}\right)$ -Expansion Method; exact solutions

## REFERENCES

1. Debnath, L., Nonlinear Partial Differential Equations for Scientist and Engineers, Birkhauser, Boston, MA, 1997.
2. Wazwaz, A.M., Partial Differential Equations: Methods and Applications, Balkema, Rotterdam, 2002.
3. Shang, Y., Bäcklund transformation, Lax pairs and explicit exact solutions for the shallow water waves equation, Applied Mathematics and Computation, 187 (2007) 1286–1297.
4. Bock, T.L., Kruskal, M.D., 1979. A two-parameter Miura transformation of the Benjamin-Ono equation, Physics Letters A, 74, 173-176.
5. Matveev, V.B., Salle, M.A., Darboux transformations and solitons, Springer, Berlin, 1991.



## ON LACUNARY STATISTICAL CONVERGENCE OF ORDER $\beta$ FOR SEQUENCES OF FUZZY NUMBERS

Hıfı ALTINOK, Damla BARLAK

Department of Mathematics, University of Firat, Elazig, Turkey

hifsialtinok@gmail.com, dyagdiran@hotmail.com

### Abstract

In this study, we generalize some lacunary statistically convergent sequence classes of order  $\beta$  using the Orlicz function  $M$  and generalized difference operator  $\Delta^m$  in fuzzy sequences and give some inclusion relations.

**Keywords:**Fuzzy number, sequence of fuzzy numbers, statistical convergence, lacunary sequence, Orlicz function, difference sequence.

### REFERENCES

1. Altınok, H. and Yağdıran, D. Lacunary statistical convergence of order  $\beta$  in difference sequences of fuzzy numbers, *Journal of Intelligent&Fuzzy Systems*, 31 (2016) 227--235.
2. Çolak, R. Statistical convergence of order  $\alpha$ , *Modern Methods in Analysis and Its Applications*, New Delhi, India: Anamaya Pub, (2010), 121--129.
3. Connor, J. S. The statistical and strong  $p$ -Cesaro convergence of sequences, *Analysis* 8 (1988), 47-63.
4. Et, M. Generalized Cesàro difference sequence spaces of non-absolute type involving lacunary sequences. *Appl. Math. Comput.* 219(17) (2013), 9372--9376.
5. Et, M.; Şengül, H. Some Cesaro-type summability spaces of order  $\alpha$  and lacunary statistical convergence of order  $\alpha$ . *Filomat* 28(8) (2014), 1593--1602.
6. Fast, H. Sur la convergence statistique, *Colloq. Math.* 2 (1951), 241-244.
7. Fridy, J. On statistical convergence, *Analysis* 5 (1985), 301-313.
8. Freedman, A. R. ; Sember J. J. and Raphael, M. Some Cesaro-type summability spaces, *Proc. Lond. Math. Soc.* 37(3) (1978), 508-520.

## **UNSTEADY FREE-CONVECTIVE EXOTHERMIC FLUID FLOW IN VERTICAL CHANNEL FILLED WITH POROUS MATERIAL**

**Basant K. Jha<sup>1</sup>, Muhammad L. Kaurangini<sup>2</sup>**

<sup>1</sup>Department of Mathematics, Ahmadu Bello University, Zaria, NIGERIA

<sup>2</sup>Department of Mathematics, Kano University of Science and Technology, Wudil, NIGERIA  
kaurangini@yahoo.com

### **Abstract**

Numerical and analytical solutions for the unsteady and steady free-convective flow in a vertical channel formed by vertical parallel plates with exothermic fluid filled with uniform porous material are presented. The flow is described by Brinkman-extended Darcy and energy equations. In the course of numerical computations to study the effect of the parameters involved, it is found that there is an excellent agreement between the analytical solution and numerical solution at a large value of time. It was also noted that the time required reaching steady-state velocity and temperature field depends on Frank-Kamenetskii parameter.

**Keywords:** Exothermic, Brinkman-extended, Porous material

### **REFERENCES**

1. Frank Kamenetskii, D.A., (1969) Diffusion and Heat transfer in chemical Kinetics, Plenum Press, New York.
2. Yang J. W., Scaccia, C and Goodman, (1974) laminar natural convection about vertical plates with oscillatory surface temperature Trans. ASME J. Heat Transf. 96, 9-14.
3. Wang C.Y, (1988) Free convection between vertical plates with periodic heat input, Trans ASME J. Heat Transfer 110 508-511

## THEORETICAL STUDY OF THE ELECTRON AND PHOTOVOLTAIC PROPERTIES OF CARBAZOLE-BASED OLIGOMERS

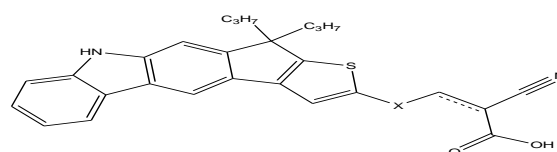
M. JABHA<sup>1,2</sup>, A. ELALAOU<sup>1</sup>, A. JARID<sup>2</sup>

<sup>1</sup> Equipe de recherche ressource naturelles et environnement (RN&E), Faculté des sciences et techniques d'Er-Rachidia, Maroc

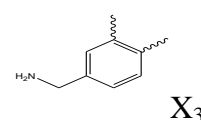
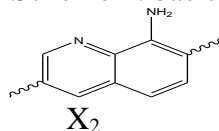
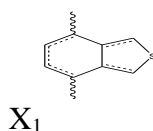
<sup>2</sup> Université Cadi Ayyad, Faculté des Sciences Semlalia, Département de Chimie, Av. My Abdellah, BP 2390 Marrakech, Maroc  
aelalaoui1@gmail.com

### Abstract

Carbazole oligomers (Scheme 1) have been widely studied in recent years thanks to their optoelectronic and photovoltaic properties and their industrial applications. In this work, we were interested in the theoretical study and quantum calculations of the structural, electronic, optical and photovoltaic properties of six conjugated systems. We have grafted three different X groups (Scheme 2) to study the variation of the optoelectronic and photovoltaic properties of these oligomers. We have also added the chromophore (2-Cyanoacrylic acid -CHCCNCO<sub>2</sub>H), to these oligomers and found that the energy gap decreases. On another hand, the optoelectronic and photovoltaic properties are improved when some donor and acceptor blocs are alternated on the oligomer skeleton since slight band gaps are noticed especially for X2 and X3 molecules with chromophore (average value 2.59eV). Indeed, some higher values of  $\lambda_{\max}$  (wave-length absorbed) are obtained and the HOMO and LUMO orbitales are correctly located than their homologs semi-conductors as the Bis-PC60BM. All these allow us to propose such materials as good candidate for some applications in the solar organic cells field. The study was undertaken using the DFT quantum method at B3LYP/6-31G (d, p) levels. To evaluate the carbazole-base systems properties, we have performed the structural optimization without geometrical restrictions on the total potential energy surface (TPES). The nature of extrema was identified by vibrational frequencies computations, all our structures are minima (all frequencies are positive) on the TPESs.



Scheme 1: basic molecule



Scheme 2: Xi groups

**Keywords:** oligomers; electronic structures, photovoltaic, gap energy

### REFERENCE

1. T.A. PhungHai, R. Sugimoto, Synthetic Metals 220 (2016) 59–71
2. M.A. Green, K. Emery, D.L. King, S. Progress inPhotovoltaics, 13, 1 (2005) 49.
3. M. J Frisch et al., gaussian, Inc., Wallingford CT, (2009).

**INFLUENCE OF ALIGNED MAGNETIC FIELD AND CNTS IN TWO DIFFERENT  
BASE FLUIDS OVER A MOVING SURFACE WITH SLIP EFFECTS**

**Rizwan Ul Haq**

Department of Engineering, Bahria University, Islamabad, Pakistan

ideal\_riz@hotmail.com, r.haq.qau@gmail.com

**Abstract**

In this study, combine impacts of the inclined magnetic field; velocity slip boundary condition and thermal radiation are analyzed for nanofluid flow moving over a flat surface. Two different kind of Carbon nanotubes are also incorporated, namely: Single wall carbon nanotubes (SWCNTs) and multiple wall carbon nanotubes (MWCNTs). Rheological characteristics of CNT-Water and CNT-Kerosene are studied under the influence of inclined applied magnetic field between  $0 \leq \gamma \leq \pi/2$ . Exact solutions are obtained for both momentum and energy equation in the form of hypergeometric function. These results are compared with the numerical technique. The course objective of aligned angle of the magnetic field is to use the governing magnetic intensity on the nanofluid and the extending appraisals of aligned angle of the magnetic field produce to upgrade the local skin friction and decline the local Nusselt number. Significant consequences of inclined magnetic field with rest of the physical parameters including radiation parameter, velocity slip and solid volume fraction nanoparticles are presented and analyzed via numerical and graphical illustrations.

**Keywords:** Carbon nanotubes, aligned magnetic field, moving surface, exact solution.

**REFERENCE**

1. S.U.S. Choi, Enhancing thermal conductivity of fluids with nanoparticles, International Mechanical Engineering Congress and Exposition, San Francisco, USA, ASME, FED 231/MD, 66 (1995), 99-105.
2. H. Masuda, A. Ebata, K. Teramae, N. Hishinuma, Alteration of thermal conductivity and viscosity of liquid by dispersed ultra-fine particles (dispersion of Al<sub>2</sub>O<sub>3</sub>, SiO<sub>2</sub>, and TiO<sub>2</sub> ultra-fine particles), Netsu Bussei (Japan) 4 (1993) 227–233.
3. Q. Li, Y. Xuan, Convective heat transfer and flow characteristics of Cu–water nanofluid, Sci. China E 45 (4) (2002) 408.

## **FLOW OF UNSTEADY SECONG GRADE NANOFUID PAST A PERMEABLE SURFACE**

**M. Ramzan<sup>1</sup>, M. Bilal<sup>2</sup>**

<sup>1</sup>Department of Computer Science, Bahria University, Islamabad Campus, Islamabad, 44000,  
Pakistan.

<sup>2</sup>Department of Mathematics, Faculty of Computing, Capital University of Science  
and Technology, Islamabad, Pakistan.  
mramzan@bahria.edu.pk

### **Abstract**

This investigation studies time dependent flow of second grade nanofluid near a stagnation point past a linearly stretched permeable surface. Analysis is performed in attendance of Thermophoresis and Borwnian motion effects. Series solutions of the system of nonlinear equations are obtained by employing Homotopy Analysis method (HAM). Graphical illustrations depicting influence of dominant parameters on all involved distributions are also given. It is observed that velocity field decreases for increasing values of suction/injection parameter.

**Keywords:** Impermeable stretched surface; Nanofluid; Stagnation point; Homotopy analysis method.

### **REFERENCES**

1. M. Ramzan, M. Bilal, J. D. Chung, Radiative flow of Powell-Eyring magneto-nanofluid over a stretching cylinder with chemical reaction and double stratification near a stagnation point, PLoS ONE, Vol: 12, No.1, e0170790, 2017.
2. M. Ramzan, M. Bilal, J. D. Chung, A. B. Mann, On MHD radiative Jeffery nanofluid flow with convective heat and mass boundary conditions, Neural Computing and Applications, 1-10, 2017.
3. M. Ramzan, M. Bilal, J. D. Chung, MHD stagnation point Cattaneo--Christov heat flux in Williamson fluid flow with homogeneous--heterogeneous reactions and convective boundary condition-A numerical approach, Journal of Molecular Liquids, Vol: 225, 856-862, 2017.

## ON THE NEW SOLUTIONS OF (3+1)-DIMENSIONAL MODIFIED KdV-ZAKHAROV-KUZNETSEV EQUATION

Onur Alp Ilhan<sup>1</sup>, Tukur Abdulkadir Sulaiman<sup>2</sup> and Hasan Bulut<sup>3</sup>

<sup>1</sup>Erciyes University, Department of Mathematics, Kayseri, Turkey

<sup>2,3</sup>Firat University, Department of Mathematics, Elazig, Turkey

oailhan@erciyes.edu.tr, sulaiman.tukur@fud.edu.ng, hbulut@firat.edu.tr

### Abstract

Using the powerful sine-Gordon expansion method with aid of Wolfram Mathematica 9, we succeed in constructing new travelling wave solutions to the (3+1)-dimensional modified KdV-Zakharov-Kuznetsev equation such as trigonometric function solutions and hyperbolic function solutions, with some solutions complex in nature. We test all the obtained solutions in this study by using program in Wolfram Mathematica 9 and they all satisfy the (3+1)-dimensional modified KdV-Zakharov-Kuznetsev equation. We also plot the 2- and 3-dimensional graphics of the obtained solutions using the same program in Wolfram Mathematica 9. We finally give a comprehensive conclusion to this study.

**Keywords:** The sine-Gordon expansion method; the (3+1)-dimensional modified KdV-Zakharov-Kuznetsev equation; hyperbolic function solution; trigonometric function solution

### REFERENCES

1. M. Matinfar, M. Eslami, S. Roshandel, The First Integral Method to Study the (2+1)-Dimensional Jaulent-Miodek Equations, *Pramana-J Phys*, 85(4) (2015), 593-603.
2. Z. Zhang, J. Zhong, S.S. Dou, J. Liu, D. Peng, T. Gao, First Integral Method and Exact Solutions to Nonlinear Partial Differential Equations Arising in Mathematical Physics, *Romanian Report in Physics*, 65(4) (2013), 1155-1169.
3. N. Taghizadeh, M. Mirzazadeh, A.S. Paghaleh, The First Integral Method to Nonlinear Partial Differential Equations, *Applications and Applied Mathematics*, 7(1) (2012), 117-132.

# **THE DISCRETE HOMOTOPY PERTURBATION SUMUDU TRANSFORM METHOD FOR SOLVING PARTIAL DIFFERENCE EQUATIONS**

**Figen Özpınar<sup>1</sup>, Fethi Bin Muhammed Belgacem<sup>2</sup>**

<sup>1</sup> Bolvadin Vocational School, Afyon Kocatepe University, Afyonkarahisar, Turkey

<sup>2</sup> Department of Mathematics, Faculty of Basic Education PAAET, Shaamyia, Kuwait

fozpinar@aku.edu.tr, fbmbelgacem@gmail.com

## **Abstract**

In this study, a discrete version of homotopy perturbation Sumudu transform method(DHPSTM) is introduced to solve the linear and nonlinear partial difference equations.

**Keywords:**Discrete homotopy perturbation method; Discrete Sumudu transform method; Partial difference equations.

## **REFERENCES**

1. R.R. Agarwal, Difference Equations and Inequalities, Marcel Dekker, Newyork, 1992.
2. M.A. Asiru, Further properties of the Sumudu transform and its applications, International Journal of Mathematical Education in Science and Technology Vol:33, No:3, 441-449, 2002.
3. M.A. Asiru, Clasroom note: application of the Sumudu to discrete dynamic systems, International Journal of Mathematical Education in Science and Technology Vol:34, No:6, 944-949, 2003.
4. F.B.M. Belgacem, A. Karaballi, Sumudu transform fundamental properties investigations and applications, Journal of Applied Mathematics and Stochastic Analysis, Article ID 91083, 23 pages, 2006.

## **SOME PROTOTYPE RESULTS OF THE SYMMETRIC REGULARIZED LONG WAVE EQUATION ARISING IN NONLINEAR ION ACOUSTIC WAVES**

**Erdem Isik<sup>1</sup>, Hasan Bulut<sup>2</sup>, Sibel Sehriban Atas<sup>2</sup>**

<sup>1</sup>Tunceli Vocational School, Munzur University, Tunceli, Turkey

<sup>2</sup> Faculty of Science, Department of Mathematics, Firat University, Elazig, Turkey  
erdem023@gmail.com, hbulut@firat.edu.tr, suzundag90@gmail.com

### **Abstract**

In this study, we consider the Bernoulli sub-equation function method for obtaining new exponential prototype structures to the Symmetric Regularized Long Wave mathematical model. We obtain new results by using this technique. We plot two- and three-dimensional surfaces of the results by using Wolfram Mathematica 9. At the end of this manuscript, we submit a conclusion in the comprehensive manner.

**Keywords:** Symmetric Regularized Long Wave Equation, Bernoulli sub-equation function method, Exponential function solution, Rational function solution, Hyperbolic function solution.

### **REFERENCES**

1. R. Hirota, The Direct Method in Soliton Theory, Cambridge Univ. Press, 2004.
2. M.J. Ablowitz, P.A. Clarkson, Solitons, nonlinear evolution equations and inverse scattering, Cambridge: Cambridge University Press, 1991.
3. A. M. Wazwaz, Travelling wave solutions for combined and double combined sine-cosineGordon equations by the variable separated ODE method, Appl. Math. Comput, 177 (2006) 755-760.
4. M. Dehghan, J. Manafian, A. Saadatmandi, The solution of the linear fractional partial differential equations using the homotopy analysis method, Z. Naturforsch, 65a (2010) 935949.
5. M. Dehghan, J. Manafian, A. Saadatmandi, Solving nonlinear fractional partial differential equations using the homotopy analysis method, Num. Meth. Partial Differential Eq. J, 26 (2010) 448-479.



**A NEW DONOR- $\pi$ -ACCEPTOR COMPOUNDS BASED ON CARBAZOLE,  
THIOPHENE AND BENZOTHIADIAZOLE FOR PHOTOVOLTAIC APPLICATION  
AS DYE-SENSITIZED SOLAR CELLS: THEORETICAL STUDY**

**Z. El Malki <sup>1\*</sup>, M. Bouachrine <sup>1</sup>, M. Hamidi <sup>2</sup>, F. Serein-Spirau <sup>3</sup>,  
J. P. Lère-Porte <sup>3</sup>, J. Marc Sotiropoulos <sup>4</sup>**

<sup>1</sup> MEM, ESTM, Université Moulay Ismail, Meknès, Maroc.

<sup>2</sup> FST Errachidia, Université Moulay Ismaïl, Errachidia, Maroc.

<sup>3</sup> Hétérochimie Moléculaire et Macromoléculaire, ENSCM, Montpellier, France.

<sup>4</sup> Université de Pau et des Pays de l'Adour, UMR5254 – IPREM, Hélioparc –PAU, France.

Corresponding authors: zelmalki@yahoo.fr

**Abstract**

A large amount of research interest has been devoted to Dye-sensitized solar cells (DSSCs) in the past two decades. Within the donor- $\pi$ -conjugated spacer-acceptor (D- $\pi$ -A) architecture [1, 2]. The electron-donating and accepting strengths have been proven to be major control variables for increasing the energy conversion efficiency [3]. In this study, we have designed a series of novel double organic D- $\pi$ -A (electron donor- $\pi$ -conjugated-acceptor) based on Carbazole, Thiophene and Benzothiadiazole. The optimized structures and optoelectronic properties of these dyes have been investigated by using the Density Functional Theory DFT/B3LYP/6-31G(d,p) method and Time Dependant Density Functional Theory (TD/DFT) calculations. The trend of the calculated HOMO-LUMO (E<sub>gap</sub>) gaps nicely compares with the spectral optical data. A low band gap will be expected in polymers containing double donor-acceptor (D-A) repeating units. The bridging effect by C=C(CN)<sub>2</sub> on the optoelectronic properties of the studied compounds is investigated. The calculated HOMO-LUMO (E<sub>gap</sub>) gaps and the wavelength of absorption spectrum ( $\lambda_{max}$ ) were compared with the experimental data. The calculated results of these dyes demonstrate that these compounds can be used as potential sensitizers for TiO<sub>2</sub> nanocrystalline solar cells. These properties suggest these materials as a good candidate for organic solar cells.

**Keywords:** Benzothiadiazole; Carbazole; Thiophene; TD/DFT calculations; Donor-Acceptor;

**REFERENCES**

1. M. Gratzel, Nature 414, 338-344 (2001).
2. M. Gratzel, J. Photochem. Photobiol. C 4, 145-153 (2003).
3. K. Tanaka, K. Takimiya, T. Otsubo, K. Kawabuchi, S. Kajihara, Y. Harima. Chem Lett. 35, 592-3 (2006).

## **EFFECTIVE PAIR-POTENTIAL BETWEEN DROPLETS WITH END-GRAFTED POLYMERS WITHIN PICKERING EMULSIONS VERSUS GRAFTING-DENSITY, SOLVENT QUALITY AND MONOMER CONCENTRATION**

**M. Benhamou<sup>1</sup>, H. Kaidi<sup>2</sup>**

<sup>1</sup> Physics Department, Faculty of Sciences, P.O. Box 11201, Moulay Ismail University, Meknes, Morocco

<sup>2</sup> CRMEF, P.O. Box 255, Meknes, Morocco  
m.benhamou@ensam-umi.ac.ma

### **Abstract**

The aim is a quantitative determination of the effective pair-potential between droplets within Pickering emulsions of (oil-in-water or water-in-oil types), which are protected by end-grafted polymer chains via (uncharged) solid particles. This strong and irreversible grafting mode plays a fundamental role and rend the emulsions more stable, even in the absence of charges. The droplets stabilization is very sensitive to the bath temperature that controls the solvent quality, the number of grafted-polymers per droplet (or grafting-density), and the concentration of monomers that float in the continuous phase (water or oil). The effective interaction between hairy-droplets is a sum of two parts: the steric interaction coming from the excluded-volume forces, and the second is simply the usual van der Waals attraction. Using the Renormalization Theory techniques, we determine the expression of the repulsive part of the overall pair-potential, upon the center-to-centre distance between adjacent hairy-droplets. First, we study all analytic properties of the obtained overall pair-potential, taking into account the solvent quality, the values of the bulk monomer concentration and the grafting-density. Second, these analytic properties enable us to classify the various shapes of the pair-potential in space of the pertinent parameters. In particular, in any case (good and theta-solvents), we observe that for high-grafting-densities (above some critical value) or small monomer concentration (below some critical value), the potentials exhibit a barrier that prevents the coalescence of hairy-droplets. As remark, incidentally, the determined potential expression is very similar to that of the DLVO one. Finally, the discussion is extended to quantify the effects of a chemical mismatch on the mutual interactions between unlike-hairy-droplets.

**Keywords:** Pickering emulsions, Solid particles, Grafted-polymers, Effective pair-potential, Renormalization Theory, Solvent quality, Monomer concentration effects, Grafting-density effects, Chemical mismatch role.

### **REFERENCES**

1. W. Ramsden, Separation of solids in the surface-layers of solutions and suspensions, Proc. Royal Soc. London 72 (1903) 156-164.
2. S.U. Pickering, CXCVI.-Emulsions, J. Chem. Soc. 91 (1907) 2001-2021.



## **BENEFITS OF REVERSE ENGINEERING TECHNOLOGIES IN SOFTWARE DEVELOPMENT MAKERSPACE**

**M.H Aabidi<sup>1</sup>, C. Baidada<sup>1</sup>, B. El Mahi<sup>1</sup>, A. Jakimi<sup>1</sup>, Hany Ammar<sup>2</sup>**

<sup>1</sup>Software Engineering & Information Systems, Engineering Team, Computer Sciences  
Department, Moulay Ismail University, FST Errachidia, Morocco

<sup>2</sup>West Virginia University, Lane Department of Computer Science and Electrical Engineering  
Morgantown, USA

ajakimi@yahoo.fr, myhafidaabidi@yahoo.fr, ammar.hany@gmail.com

### **Abstract**

In the recent decades, the amount of data produced by scientific, engineering, and life science applications has increased with several orders of magnitude. In parallel with this development, the applications themselves have become increasingly complex in terms of functionality, structure, and behavior. In the same time, development and production cycles of such applications exhibit a tendency of becoming increasingly shorter, due to factors such as market pressure and rapid evolution of supporting and enabling technologies. As a consequence, an increasing fraction of the cost of creating new applications and manufacturing processes shifts from the creation of new artifacts to the adaption of existing ones. A key component of this activity is the understanding of the design, operation, and behavior of existing manufactured artifacts, such as software code bases, hardware systems, and mechanical assemblies. For instance, in the software industry, it is estimated that maintenance costs exceed 80% of the total costs of a software product's lifecycle, and software understanding accounts for as much as half of these maintenance costs. To facilitate the software development process, it would be ideal to have tools that automatically generate or help to generate UML (Unified Modeling Language) models from source code. Reverse engineering the software architecture from source code provides a valuable service to software practitioners. Case tools implementing MDA and reverse-engineering constitute an important opportunity of software development engineers. So MDA and reverse engineering is an important key witch make makerspace more productive and more efficient.

**Keywords:**Software development; Reverse Engineering; UML behavior; MDA, makerspace;

### **REFERENCES**

1. MDA (2005). The Model Driven Architecture. Retrieved October 2011 from [www.omg.org/mda](http://www.omg.org/mda).
2. UML (2010). Unified Modeling Language: Infrastructure. Version 2.3. OMG Specification formal/ 2010-05-03. Retrieved October 2011 from [www.omg.org](http://www.omg.org).

## **INVARIANT SUBSPACE METHOD: APPLICATION TO NONLINEAR DISPERSIVE EQUATION WITH TIME- CAPUTO-FABRIZIO FRACTIONAL DERIVATIVE**

**E. H. El Kinani<sup>1</sup> and A. Ouhadan<sup>2</sup>**

<sup>1</sup>Equipe Modélisation Mathématique et Calcul Scientifique, Ecole Nationale Supérieure des Arts et Métiers, Université Moulay Ismaïl, Marjane 2, B.P. 15290, Meknès, Morocco

<sup>2</sup>Centre Régional des Métiers de l'Education et de la Formation, Meknès, BP 255, Morocco  
elkinani\_67@yahoo.com

### **Abstract:**

In this study, the method of invariant subspace is used to study nonlinear fifth order dispersive equation with time-Caputo Fabrizio fractional derivative is discussed. To solve the obtained system of ordinary fractional equations, some useful news properties of Laplace transform of Caputo Fabrizio fractional derivative are used. Consequently, a non trivial exact solution of nonlinear fifth order dispersive equation with time-Caputo-Fabrizio fractional derivative is obtained.

**Keywords:** Invariance subspace method, Caputo-Fabrizio Fractional Derivative, Nonlinear fifth Order Dispersive Equation

### **REFERENCES:**

1. R. Gazizov and A. Kasatkin, "Construction of exact solutions for fractional order differential equations by the invariant subspace method", Computers and Mathematics with Applications, Vol. 66, no. 5, 2013, 576-584.
2. V. Galaktionov and S. Svirshchevskii, "Exact solutions and invariant sub-spaces of nonlinear partial differential equations in mechanics and physics". Chapman and Hall/CRC applied mathematics and nonlinear science series, 2007.
3. T. Hoherman and P. Rosenau," On KS-type equations describing the evolution and rupture of a liquid interface", Phys. D, 67, 113-125, 1993
4. Pietro Artale Harris, Roberto Garra, Nonlinear time-fractional dispersive equations, Communications in Applied and Industrial Mathematics (2015), DOI: 10.1685, arXiv:1410.8085v1 [math-ph] 29 Oct 2014

## **THE NUMERICAL SOLUTION OF FRACTIONAL BRATU-TYPE DIFFERENTIAL EQUATIONS**

**Duygu Dönmez Demir, Aylin Zeybek**

Department of Mathematics, Manisa Celal Bayar University, Manisa, Turkey  
duygu.donmez@cbu.edu.tr

### **Abstract**

This study introduces the differential transform method (DTM) to solve the fractional Bratu-type differential equation modelling a combustion in numerical slab. For the definition of fractional derivative, the Caputo sense is used. The result corresponds to the exact solution when obtained solution is constructed as power series for some values of fractional order. Finally, some examples are presented to indicate the efficiency of applied method. Comparison of the results obtained by DTM with those obtained by other methods is given.

**Keywords:** Fractional Bratu-type differential equation; DTM; Caputo sense fractional derivative.

### **REFERENCES**

1. Bahman Ghazanfari, Amaneh Sepahvandzadeh, Homotopy Perturbation Method for Solving Fractional Bratu-Type Equation, *Journal of Mathematical Modeling*, 2 (2), 143-155, 2015.
2. Bahman Ghazanfari, Amaneh Sepahvandzadeh, Adomian Decomposition Method for Solving Fractional Bratu-type Equations, *Journal of Mathematics and Computer Science*, 8, 236-244, 2014.
3. Esmail Babolian, Shahnam Javadi and Eslam Moradi, RKM for solving Bratu-type differential equations of fractional order, *Math. Meth. Appl. Sci.*, 39, 1548-1557, 2016.
4. Zaid Odibat, Shaher Momani, Vedat Suat Erturk, Generalized differential transform method: Application to differential equations of fractional order, *Applied Mathematics and Computation*, 197, 467-477, 2008.

## **INCREASING THE CAPACITY OF O-MIMO SYSTEMS USING MGDM TECHNIQUE**

**EL OUTASSI Omar<sup>1</sup>, EL HAJRAT Nourddne<sup>2</sup>, ZOUINE Younes<sup>3</sup>**

<sup>1</sup> Laboratory of Optoélectronique et Techniques Energétiques Appliquées, Dept. of Physics, FST, B.P. 509, Boutalamine, Errachidia, My Ismail University, Morocco.

<sup>2</sup> Laboratory of Optoélectronique et Techniques Energétiques Appliquées, Dept. Of Physics, FST, B.P. 509, Boutalamine, Errachidia, My Ismail University, Morocco.

<sup>3</sup> ENSA Kenitra, Morocco, IbnTofail University, Morocco.

elhajratssi@gmail.com, eloutassiomar@gmail.com, yszouine@gmail.com

### **Abstract**

The MGDM (Group Mode Division Multiplexing) is a multiplexing technique, which aims to improve the multimode optical fiber's performance by spatially multiplexing the data streams to be transmitted. In this work we study optical MIMO transmission systems (Multi-input Multi-output) optical fiber on an MMF, rimarily graded in-dex (GI) MMFs, specifically adapting the architecture of optical MIMO transmission systems. In this context we studied he optimization of launching and detection conditions in order to increase the capacity of an optical MIMO link using the MGDM technique.

**Keyword:** MGDM, GI-MMF, Optical MIMO capacity of transmission

### **REFERENCES**

1. G.D. Golden et al "Detection algorithm and initial laboratory results using V-BLAST space-time communication architecture" Electronics Letters, Vol. 35, No. 1, pp. 14-16, 1999.
2. T. Koonen, H. Van den Boom, F. Willems, J. Bergmans, and G.-D. Khoe, "Broadband multi-service in house networks using mode group diversity multiplexing," in Proc. Int. Plastic Opt. Fibers Conf., Tokyo, Japan, 2002, pp. 87-90
3. M. Awad, I. Dayoub, W. Hamouda, and J. M. Rouvaen, "Adaptation of the mode group diversity multiplexing technique for radio signal transmission over MMF," IEEE/OSA J. Opt. Commun. Netw, vol. 3, no. 1, pp. 1-9, Dec. 2011.
4. E. Telatar, "Capacity of multi-antenna Gaussian channels," Eur. Trans. Telecommun, vol. 10, no. 6, pp.585-595, Nov/Dec.1999.
5. L. Raddatz, I. H. White, D. G. Cunningham, and M. C. Nowell, "An experimental and theoretical study of the offset launch technique for the enhancement of the bandwidth of multimode fiber links," J. Lightw. Technol., vol. 16, no. 3, pp. 324-331, Mar. 1998.
6. M. Calzavara, R. Caponi, and F. Cisternino, "Selective excitation of annular zones in graded index multimode fiber," J. Opt. Commun., vol. 5, no. 3, pp. 82-86, 1984.

# MHD MIXED CONVECTION IN A LID-DRIVEN TRIANGULAR CAVITY FOR VARIOUS ELECTRICAL CONDUCTIVITY MODELS

Fatih Selimefendigil<sup>1</sup>, Hakan F. Öztop<sup>2</sup>

<sup>1</sup>Department of Mechanical Engineering, Celal Bayar University, Manisa, Turkey

<sup>2</sup>Department of Mechanical Engineering, Technology Faculty, Firat Univeristy, Elazig, Turkey

fthsel@yahoo.com, hfoztop1@gmail.com

## Abstract

In this study, effects of different electrical conductivity models for magneto-hydrodynamic mixed convection of nanofluids in a lid-driven triangular cavity was numerically investigated with finite element method. Effects of Richardson number, Hartmann number on the convective heat transfer characteristics were analyzed for various electrical conductivity models of nanofluids. Average Nusselt number decreases for higher Hartmann and Richardson numbers. Discrepancies in the local and average heat transfer exist between different electrical conductivity models which is higher for higher values of Richardson number and Hartmann number.

**Keywords:** Magneto-hydrodynamic; Mixed Convection; Electrical Conductivity; Finite Element Method.

## REFERENCES

1. B. Ghasemi, S. Aminossadati, Mixed convection in a lid-driven triangular enclosure filled with nanouids, International Communications in Heat and Mass Transfer 37 (2010) 1142-1148.
2. Y. Varol, A. Koca, H. F. Oztop, Natural convection in a triangle enclosure with flush mounted heater on the wall, Int. Comm. Heat Mass Transfer 33(2006) 951-958.
3. F. Selimefendigil, H. F. Oztop, Natural convection in a flexible sided triangular cavity with internal heat generation under the effect of inclined magnetic field, Journal of Magnetism and Magnetic Materials 417 (2016) 327-337.

## NUMERICAL SOLUTIONS OF VECTOR STOCHASTIC DIFFERENTIAL EQUATIONS

Gülşen ORUCOVA BÜYÜKÖZ<sup>1</sup>, Mustafa BAYRAM<sup>2</sup>

<sup>1</sup> Department of Mathematics, Yildiz Technical University, İstanbul, Turkey

<sup>2</sup> Department of Computer Engineering, University of Gelisim, İstanbul, Turkey  
mbayram@gelisim.edu.tr, gbuyukoz@yildiz.edu.tr,

### Abstract

In this study, we consider systems of stochastic differential equations. We mention about general form of vector stochastic differential equations. Then using numerical methods we obtain approximation solutions. The efficiency of these methods we compare the exact solutions and numerical solutions of our model.

**Keywords:** Systems of stochastic differential equations; Numerical solutions

### REFERENCES

1. Kloeden, Peter Eris, Eckhard Platen, and Henri Schurz. Numerical solution of SDE through computer experiments. Springer Science & Business Media, 2012.
2. Kloeden, P. E., and Platen, E. (1992). Higher-order implicit strong numerical schemes for stochastic differential equations. Journal of statistical physics, 66(1), 283-314.
3. Allen, E. (2007). Modeling with Itô stochastic differential equations (Vol. 22). Springer Science & Business Media.
4. San Martín, J., and Torres, S. (2001). Euler scheme for solutions of a countable system of stochastic differential equations. Statistics & probability letters, 54(3), 251-259.
5. Higham, D. J., and Kloeden, P. E. (2002). MAPLE and MATLAB for stochastic differential equations in finance. In Programming Languages and Systems in Computational Economics and Finance (pp. 233-269). Springer US.



## NUMERICAL APPROACH FOR SOLVING TIME FRACTIONAL DIFFUSION EQUATION

Dilara ALTAN KOÇ, Mustafa GÜLSU

Department of Mathematics, Faculty of Science, Mugla Sıtkı Kocman University, Mugla,  
Turkey.

dilaraaltan@mu.edu.tr, mgulsu@mu.edu.tr

### Abstract

In this study one of the fractional partial differential equations was solved by finite difference scheme based on five point and three point central space method with discretization in time. We use between the Caputo and the Riemann-Liouville derivative definition and the Grünwald-Letnikov operator for the fractional calculus. The stability analysis of this scheme is examined by using von-Neumann method. A comparison between exact solutions and numerical solutions is made. Some figures and tables are included.

**Keywords:** Fractional diffusion equation, finite difference schemes, explicit method.

### REFERENCES

1. Ciesielski M., Leszczynski J. Numerical simulations of anomalous diffusion, Computer Methods in Mechanics, Gliwice, Poland, June 3-6, 2003.
2. Berkowitz B.; Scher H., Anomalous transport in random fracture networks, Phys. Rev. Lett., 79, 4038-4041, 1997.
3. He J. H., Approximate analytical solution for seepage flow with fractional derivatives in porous media Comput. Method. Appl. M. 167, 57, 1998.
4. Yuste S. B., Acedo L., An explicit finite difference method and a new Von Neumann-type stability analysis for fractional diffusion equations, Society for Industrial and Applied Mathematics, Vol. 42(5), 1862-1874, 2005.
5. Murillo J. Q., Yuste S. B., An Explicit Numerical Method for the Fractional Cable Equation, Hindawi Publishing Corporation International Journal of Differential Equations, 2011.

# STABILITY ANALYSIS OF DECOUPLED TIME- STEPPING SCHEMES FOR THE SPECIALIZED CONDUCTION SYSTEM/MYOCARDIUM COUPLED PROBLEM IN CARDIOLOGY

Mbarki Wajih <sup>1</sup> Aouadi Saloua <sup>1</sup> Zemzemi Nejib <sup>2</sup>

<sup>1</sup>Faculté des Sciences de Tunis, Université de Tunis El Manr

<sup>2</sup>INRIA Bordeaux Sud-Ouest 200 avenue de la vieille tour, 33405 Talence, France.

mbarki\_wajih@live.fr

## Abstract

The Purkinje network is the rapid conduction system in the heart. It ensures the physiological spread of the electrical wave in the ventricles. In this work, we first prove the stability of the space semi-discretized problem. Then we present four different strategies for solving the Purkinje/ myocardium coupled. The strategies are based on different time discretization of the coupling terms. The first scheme is fully coupled, where the coupling terms are considered implicit. The second and the third schemes are based on Gauss-Seidel time-splitting schemes where one coupling term is considered explicit and the other is implicit. The last is a Jacobi-like time-splitting scheme where both coupling terms are considered explicit. Our main result is the proof of the stability of the three considered schemes under the same restriction on the time step. Moreover, we show that the energy of the problem is slightly affected by the time-splitting schemes. We illustrate the theoretical result by different numerical simulations in 2D. We also conduct 3D simulations using physiologically detailed ionic models.

**Keywords:** Cardiac electrophysiology, reaction-diffusion, Purkinje network, myocardium, stability analysis, monodomain model, finite element, coupling problem.

## REFERENCES

1. C. D'Angelo and A. Quarteroni. On the coupling of 1D and 3D diffusion reaction equations. Application to tissue perfusion problems. MOX, Dipartimento di Matematica "F. Brioschi" Politecnico di Milano, Via Bonardi 29- 20133 Milano (Italy)2-C.

## **THE CREATIVITY DIMENSION OF INSTRUCTIONAL MATERIALS DESIGNED BY PROSPECTIVE TEACHERS: THE COMPARISON ACROSS DOMAINS**

**Esen Ersoy<sup>1</sup>, Emine Şendurur<sup>2</sup>, İsmail Çetin<sup>3</sup>**

<sup>1</sup> Programme of Elementary Mathematics Teaching, University of Ondokuz Mayıs, Samsun, Turkey

<sup>2,3</sup> Computer Education and Instructional Technologies Teacher Education, University of Ondokuz Mayıs, Samsun, Turkey  
eminesendurur@gmail.com , ismail.cetin@omu.edu.tr, esene@omu.edu.tr

### **Abstract**

This study aims at revealing the creativity dimension of the materials designed and developed by the second year students studying at the department of Computer Education and Instructional Technology. A part of the participants has completed the process by designing materials in their own field, information technologies; while some of them have done so by designing materials in the field of mathematics. The data have been retrieved from an experimental study of 13 weeks. "Teaching Material Creativity Rubric" developed by the researchers, has been used as the data collection tool. The rubric has been developed in order to evaluate the creativity dimensions of products. While developing the rubric, the creative product evaluation dimensions of Finke et al. (1996) have been a source of inspiration. The products developed by the students have been evaluated through the retrieved data, in terms of their creativity. The rubric developed includes Originality, Practicality & Sensibility, Productivity & Flexibility, Feasibility, Inclusiveness, and Insightfulness dimensions. In this research, the data of the aforementioned dimensions and sub-dimensions have been evaluated. The results present that the creativity level of the products on teaching information technologies, which have been developed by Computer Education and Instructional Technology (CEIT) students, is high. It has been argued that the creativity of domain-specifically developed materials is higher, through literature.

**Keywords:** Material Design in Computers, Mathematics Teaching, Originality, Applicability, Creativity, Creativity and Domains.

### **REFERENCES**

1. Finke, R.A., Ward, T.B., & Smith, S.M. (1996). Creative Cognition: Theory, Research, and Applications, Cambridge, MA: MIT Press.

**PERSONALIZATION OF LEARNING SITUATIONS WITHIN A VIRTUAL  
ENVIRONMENT FOR TRAINING BASED ON FUZZY CLUSTERING**

**FAHIM Mohamed<sup>1</sup>, JAKIMI Abdeslam<sup>1</sup>, EL BERMI Lahcen<sup>1</sup>, E. H. EL KINANI<sup>2</sup>**

<sup>1</sup>Software Engineering & Information Systems, Engineering Team, Computer Sciences  
Department, Moulay Ismail University, FST Errachidia, Morocco

<sup>2</sup>Mathematical Modeling and Scientific Computation Team, ENSAM, Moulay Ismail  
University, Meknès, Morocco

fahim.mohamed89@gmail.com , ajakimi@yahoo.fr, elbermi.lahcen@gmail.com,  
elkinani\_67@yahoo.com

**Abstract**

Advances in networks, computers and multimedia technology have changed traditional methods for learning and skills training. Today, Virtual Environments for Training (VET) has been popular, it can provide an environment where virtual reality can be used to create interactive interfaces and real-time software that can control every response and action made by the user. VET have proven to be advantageous to put learners into varied training situations to acquire knowledge and competencies, especially when these situations are taking place in uncontrolled circumstances, or those situations are dangerous, unrealizable, expensive to establish in reality. However individual learners find it difficult to select suitable learning activities for their particular situation because often, there is no personalized service to response to the user needs. Personalization of learning in a VET is a very important way of improving the effectiveness and the quality of the training, yet it also a complex process that requires consideration of several factors such as learner's profiles. The goal is to associate suitable learning activities, pedagogical resources, etc, to each learner based on his profile. However, personalization of learning becomes an issue with the uncertainty and imprecision of data that may contains a learner profile. To address this issue, this study is an attempt to integrate a fuzzy clustering into the process of the personalization of learning.

**Keywords:** Virtual Environments for Training; personalization of learning; fuzzy clustering.

**REFERENCES**

1. P. Fuchs, G. Moreau, Le traité de la réalité virtuelle (Les Presses de l'Ecole des Mines de Paris, 2006).
2. N. Mollet, B. Arnaldi, Storytelling in Virtual Reality for Training, Proceedings of the First international conference on Technologies for E-Learning and Digital Entertainment (Page: 334-347 Year of Publication: 2006 ISBN: 3-540-33423-8 978-3-540-33423-1).

## **THE WEAK SOLUTION OF ANTIPLANE ELECTRO- VISCOELASTIC CONTACT PROBLEM WITH REGULARIZED FRICTION LAW**

**Hacene Chaouche Soumeiya and Mohamed Dalah**

Department of Mathematics, Faculty of Sciences: FES University of Constantine 1: UPMC,  
Algeria  
dalah.mohamed@yahoo.fr

### **Abstract**

In this work, we study the unique weak solution of the antiplane electro-viscoelastic problem with regularized friction law. In first time, we derive the variational formulation of continuous problem. Finally, we prove that the weak solution of the antiplane electro-viscoelastic problem with regularized friction law converge to the solution of the antiplane electro-viscoelastic problem when the parameter  $\rho$  is very small.

**Keywords:** Friction law; formulation variationnelle, electro-visco-elasticity.

### **REFERENCES**

1. M. Sofonea, M. Dalah, Antiplane Frictional Contact of ElectroViscoelastic Cylinders, Electronic Journal of Differential Equations, Vol. 18, No. 161, pp. 114, 2007.
2. M. Dalah, Analysis of electro-viscoelastic antiplane contact problem with total slip rate dependent friction, Vol. 2009, No. 118, pp. 1-15, 2009.
3. Lerguet, Zhor, A frictional contact problem for an electro-viscoelastic body, Vol. 2007 (2007), No. 170, pp. 1-16, 2007.

## **DEVELOPING AN ACHIEVEMENT TEST FOR FRACTION TEACHING: VALIDITY AND RELIABILITY ANALYSIS**

**Belgin Bal-İncebacak<sup>1</sup> Esen Ersoy<sup>2</sup>**

<sup>1</sup> Department of Primary Education, University of Ondokuz Mayıs, Samsun, Turkey

<sup>2</sup> Department of Mathematics, University of Ondokuz Mayıs, Samsun, Turkey

esene@omu.edu.tr, belginbal33@gmail.com

### **Abstract**

The aim of the study is to develop an achievement test that can be used to measure the achievement status of elementary school 4th grader students in terms of their fractions learning in mathematics courses. Examining the literature, it is visible that there are 8 development stages of the achievement test. According to Atilgan (2013), these stages include determining the area to be used for test scores, determining the behaviors representing the area or the statement, writing test items, reviewing the test items, preparing the test form, putting the test on a trial implementation, selecting materials by analyzing them according to the trial implementation, and prognosis of the selected items that generate the statistics of the final test. The "Academic Achievement Test for Fractional Teaching (KÖYABT)", which has been developed in the study, aims at measuring students' status of learning acquisitions included in the elementary school curriculum after fraction teaching. Throughout the development of the achievement test, 16 expert opinions were obtained including those of 5 teachers and 11 academicians. ITEMAN 3.5 package software was employed to analyze the validity and reliability of the test. Statistical analysis of the test reveals that KR-20 Internal Consistency and KR-21 Internal Consistency are 0.90. This value indicates that the consistency of the test is high. The average discrimination of the test is 0.80, which indicates that the test is highly distinctive among students. The average strength of the test has been calculated as 0.67. Therefore, it has been determined that the test should be both easy and distinctive when it comes to measuring the effectiveness of the teaching method. The result of the analysis suggest that when consistency and distinctiveness values are considered, the developed test is not only easy to use but also highly distinctive. Finally, it has been discovered that the academic achievement test for fraction teaching is valid and reliable.

**Keywords:** Achievement Test, Reliability, Validity, Fraction teaching.

### **REFERENCES**

1. Atilgan, H., Kan, A., Doğan N., Eğitimde Ölçme ve Değerlendirme. Ankara: Anı Yayıncılık, 2006.

## **THE EVALUATION OF THE PROBLEM SOLVING IN MATHEMATICS COURSE ACCORDING TO STUDENT VIEWS**

**Esen Ersoy<sup>1</sup> Belgin Bal-İncebacak<sup>2</sup>**

<sup>1</sup> Department of Mathematics, University of Ondokuz Mayıs, Samsun, Turkey

<sup>2</sup> Department of Primary Education, University of Ondokuz Mayıs, Samsun, Turkey  
belginbal33@gmail.com, esene@omu.edu.tr

### **Abstract**

This study was conducted to determine the problem solving skills of the third grade students studying at the department of elementary school mathematics teaching. The study was conducted in the second semester of the academic year of 2015-2016. The study group consists of 47 third year student who study at Ondokuz Mayıs University, Faculty of Education Elementary School Mathematics Teaching and take the selective course of Problem Solving in Mathematics. Within the scope of this course, the researchers explained subjects related to problem and problem solving, problem solving skills and solved problems during the first 4 weeks of the course. For the rest of the weeks, the students were divided into groups. They have solved two non-routine problems each week for 8 weeks. At the end of each course the problems solved were discussed and the problem situations were dealt within the scope of Polya's problem solving stages. At the end of the process, the students were interviewed through a semi-structured interview form. Two interviews were conducted: before and after the implementation. The method of study is the interview method, which is one of the qualitative research methods. The data of the study were comparatively analyzed via content analysis. In order to check the validity of the scope, the percentage of compliance was calculated via Miles & Huberman's (1996) compliance percentage formula. In light of the retrieved findings, the answers given by the students have been thematized as the stages of problem solving, understanding the problem, implementing the problem, evaluation of the problem, reasons for taking the courses, association problems, ways of finding different solutions, development of procedural skills, creating formulas, mathematical thinking, use of mathematical language, suitability of the course, views on problem solving, and the contribution of the course. When the answers of the students who took the course are examined under these themes, it becomes apparent that they enjoyed and the course very much and obtained a lot of information, moreover; their perspective on mathematics course has changed and they got the chance to implement the stages of problem solving.

**Keywords:** Problem, Problem solving, Mathematics, Polya

### **REFERENCES**

1. Bal-İncebacak, B., Ersoy, E. 7. sınıf öğrencilerinin matematiksel muhakeme becerilerinin TIMSS'e göre analizi. Uluslararası Sosyal Araştırmalar Dergisi, Vol:9, No:46, 474- 481, 2016a.

## PISA QUESTION AND REASONING SKILL

Esen Ersoy<sup>1</sup> Belgin Bal-İncebacak<sup>2</sup>

<sup>1</sup> Department of Mathematics, University of Ondokuz Mayıs, Samsun, Turkey

<sup>2</sup> Department of Primary Education, University of Ondokuz Mayıs, Samsun, Turkey  
belginbal33@gmail.com, esene@omu.edu.tr,

### Abstract

The ability of thinking allows students to make reasonable decisions and make sense of the events they experience throughout their lives (Liu Po-Hung, 2003). In making reasonable decisions, the students have to reason the possibilities that exist in the events for the process of thinking. Harel and Lim (2004); Lesh and Zawojewski (2007) point out that students must be able to think deeply and carefully and make reasonable assumptions for reasoning. It is believed that increasing the reasoning skills enables students to improve their rational and sound decision-making. Therefore, revealing students' mathematical reasoning skills gains significance. The objective of the study is to determine the level of the reasoning skills of the secondary school students. This research has been conducted during the academic year of 2015-2016 with the participation of 51 students in total, from a province in the Black Sea region of Turkey by using random sampling method. Case study method has been used in this study, since it explains an existing situation. In this study, content analysis from the qualitative research methods was carried out. In order to ensure the validity of the scope, agreement percentage formula was used and expert opinions were sought.

The problem named Holiday from the Chapter 1 of the normal units in Problem Solving Questions from PISA (Program for International Student Assessments) (2015), are used as the data collection tool for the study. The problem named Holiday consists of two questions. Applied problems were evaluated according to the mathematical reasoning stages of TIMSS (2003). The findings suggest that the students use proportional reasoning while solving the problems and use the geometric shapes to facilitate the solution of the problem. When they come across problems related to each other, it is observed that they create connections between the problems based on the results of the previous problem. In conclusion, the students perform crosscheck to ensure that their solutions to the problems are accurate.

**Keywords:** Mathematics, Secondary School, Reasoning

### REFERENCES

1. TIMSS, IEA's TIMSS 2003 International Report on Achievement in the Mathematics Cognitive Domains: Findings from a Developmental Project International Association for the Evaluation of Educational Achievement. TIMSS & PIRLS International Study Lynch School of Education, Boston College, 2003.



## **TECHNOLOGIES OF A CONTINUOUS ULTRASONIC THICKNESS MEASURING**

**Vitaliy Pronin<sup>1</sup>, Petr Shkatov<sup>1</sup>, Anna Sandulyak<sup>1</sup>, Haci Mehmet  
Baskonus<sup>2</sup>**

<sup>1</sup>Moscow technological university, Moscow, RF,  
<sup>2</sup>Department of Computer Engineering, Munzur University, Tunceli, Turkey  
pronin@echoplus.ru, petr\_shkatov@mail.ru, anna.sandulyak@mail.ru,  
hmbaskonus@gmail.com

### **Abstract**

In present work, technologies and means of an ultrasonic thickness measuring of the main metal and welded connections of pipelines with application of the phased antenna lattices with linear scanning and TOFD methods are described. According to a thickness measuring with application of the specialized software the cards of thickness of controlled subjects are received. Results of measurement with use of these technologies, and also the prospects of development of these methods are given.

**Keywords:** Antenna lattice, digital focusing of the antenna, ultrasonic thickness measuring of welded connections, TOFD method, linear scanning

### **REFERENCES**

1. Way of ultrasonic control of a profile of an internal surface of a product with uneven surfaces. Patent RF № 2560754, 2014.
2. E.G. Basulin, S.A. Kokolev, A.S. Golubev. Application of an ultrasonic antenna lattice for registration of echo signals by method of double scanning for obtaining images of defects. Defektoskopiya, 7, 2009.

## **TWO-EXPONENTIAL MODEL MAGNETIC CONTROL OF FERROIMPURITIES IN VARIOUS ENVIRONMENTS**

**Anna Sandulyak, Alexander Sandulyak, Maria Polismakova, Darya Sandulyak**  
Moscow technological university, Moscow, RF,  
anna.sandulyak@mail.ru, a.sandulyak@mail.ru, m.polismakova@mail.ru, d.sandulyak@mail.ru

### **Abstract**

Indicative examples of technological environments for which mass-operational characteristics of magnetic control of ferroimpurities not corresponds to the basic exponential model are given and analyzed. The concept of two-exponential model assuming the piecewise and functional description of the key characteristic of control is stated and realized. Possibilities of calculations performance of the actual and potential masses of ferroimpurities, allocated from the technological environment, and the corresponding values of their concentration in this environment are shown.

**Keywords:** Ferroimpurity, magnetic control, exponential model, mass of ferroimpurities, concentration of ferroimpurities.

### **REFERENCES**

1. A.A. Sandulyak, M.N. Polismakova, D.V. Ershov, A.V. Sandulyak, V.A. Ershova, D.A. Sandulyak, Functional extrapolation of the mass-operational characteristic of magnetophoresis as a basis for a precision method of monitoring ferroparticles, Meas. Tech. 53 (8) (2010) 914–918.
2. A.A. Sandulyak, A.V. Sandulyak, V.A. Ershova, M.N. Polismakova, D.A. Sandulyak. Use of the Magnetic Test-filter for Magnetic Control of Ferroimpurities of Fuels, Oils, and Other Liquids (Phenomenological and Physical Models) Journal of Magnetism and Magnetic Materials 426 (2017) 714–720.
3. A. A. Sandulyak, A.V. Sandulyak, H. Bulut, H.M. Baskonus, M.N. Polismakova, D.A. Sandulyak. Some characteristic properties of analytical method of magnetic control of ferroimpurities in various primary and technological media. MATEC Web of Conferences 76 (2016)

## **MEASUREMENT OF DEPTH OF CLOSE LOCATED SUPERFICIAL CRACKS BY ELECTROPOTENTIAL METHOD**

**Petr Shkatov<sup>1</sup>, Irina Lisitsyna<sup>1</sup>, Anna Sandulyak<sup>1</sup>, Hasan Bulut<sup>2</sup>**

<sup>1</sup> Moscow technological university, Moscow, RF,

<sup>2</sup>Department of Mathematics, University of Firat, Elazig, Turkey

petr\_shkatov@mail.ru, lisicina-irina@yandex.ru, anna.sandulyak@mail.ru,  
hbulut@firat.edu.tr

### **Abstract**

The researches of signals of the electropotential converter interacting with two close located superficial cracks parallel each other are conducted. The scheme of measurement with the converter electrodes placed in rectangle tops was investigated. Results of the research are important for measurement of depth of superficial cracks of stress-corrosion origin.

**Keywords:** Electropotential method, measurement of depth of superficial cracks, corrosion cracking energized (stress corrosion), grid of cracks.

### **REFERENCES**

1. V.P. Vavilov, K.V. Podmasteriev, F.R. Sosnin at all. Nondestructive control. The reference book in 8 volumes /Under redaction of V.V. Kliuev/ Moscow, 2006.
2. E.I. Brainin. Control of elements of electrical machines and devices by an electropotential method, Moscow, Energiya, 1980.
3. P.N. Shkatov. Research of an error of measurement of depth of cracks by an electropotential method. Proceedings of the 14<sup>th</sup> Russian science conference « Nondestructive control and diagnostics », Moscow, 1996.
4. P.N. Shkatov. Increased preciseness of deep defects defecting through electropotential method// 7<sup>th</sup> European Conference on NDT, Copenhagen, 1998.
5. P.N. Shkatov. The solution of the return problem of an electropotential defektometry for a superficial crack of final length. Proceedings of the 3<sup>rd</sup> international science conference "Computer methods and the return tasks in nondestructive control and diagnostics", Moscow, 2002.
6. P.N. Shkatov. The computerized measuring instrument of depth of cracks «ZOND IGT-98». «Control.Diagnostics» Mechanical engineering, 1998.

# **A THREE FACTOR REMOTE USER AUTHENTICATION SCHEME USING COLLISION RESIST FUZZY EXTRACTOR IN SINGLE SERVER ENVIRONMENT**

**Debasis Giri<sup>1</sup> and Tanmoy Maitra<sup>2</sup>**

<sup>1</sup>Department of Computer Science and Engineering, Haldia Institute of Technology, Haldia-  
721657, India

<sup>2</sup>Department of Computer Science and Engineering, Jadavpur University,  
Kolkata-700032, India  
debasis\_giri@hotmail.com, tanmoy.maitra@live.com

## **Abstract**

Due to rapid growth of online applications, it is needed to provide such a facility by which communicators can get the services by applying the applications in a secure way. As communications are done through an insecure channel like Internet, any adversary can trap and modify the communication messages. Only authentication procedure can overcome the aforementioned problem. Many researchers have proposed so many authentication schemes in this literature. But, this study has shown that many of them are not usable in real world application scenarios because, the existing schemes cannot resist all the possible attacks. Therefore, this study has proposed a three factor authentication scheme using hash function and fuzzy extractor. This study has further analyzed the security of the proposed scheme using random oracle model. The analysis shows that the proposed scheme can resist all the possible attacks. Furthermore, comparison between proposed scheme and related existing schemes shows that the proposed scheme has better trade-off among storage, computational and communication costs.

**Keywords:** Attack; Authentication; Biometric; Password; Smart card.

## **REFERENCES**

1. Leslie Lamport. Password authentication with insecure communication. Commun. ACM, Vol. 24, No: 11, 770-772, 1981.

# CLASSIFICATIONS ON THE TRAVELLING WAVE SOLUTIONS TO THE (3+1)-DIMENSIONAL GENERALIZED KP AND JIMBO-MIWA EQUATIONS

Ozlem ISIK<sup>1</sup>, Ozge IRMAK DEGIRMENCI<sup>2</sup>, Hasan BULUT<sup>2</sup>

<sup>1</sup> Department of Mathematics, Kirklareli University, Kirklareli, Turkey

<sup>2</sup> Department of Mathematics, Firat University, Elazig, Turkey

ozlem.isik@klu.edu.tr, ozgeirmak@firat.edu.tr, hbulut@firat.edu.tr

## Abstract

In this study, we use the powerful  $\tan\left(\frac{F(\xi)}{2}\right)$ -expansion method with the help of Wolfram Mathematica 9 in investigating the solution structures of three well known nonlinear evolution equations, namely; the (3+1)-dimensional generalized KP and (3+1)-dimensional Jimbo-Miwa equations. We obtain new solutions such as hyperbolic function, exponential function and rational function solutions. We plot two- and three-dimensional graphics of some obtained results using the same program, Wolfram Mathematica 9.

**Keywords:**  $\tan\left(\frac{F(\xi)}{2}\right)$ -expansion method; the (3+1)-dimensional generalized KP equation; the (3+1)-dimensional Jimbo-Miwa equation; trigonometric function solutions; hyperbolic function solution; exponential function solution; rational function solution

## REFERENCES

1. A.J.M. Jawad, The sine-cosine function method for the exact solutions of nonlinear partial differential equations, International Journal of Research and Reviews in Applied Sciences, 13(1), 186–191, 2012.
2. W. Ma, J. Lee, A transformed rational function method and exact solutions to the (3+1)-dimensional Jimbo-Miwa equation, Chaos, Solitons and Fractals, 42, 1356-1363, 2009.
3. A.M. Wazwaz, Multiple-soliton solutions for a (3+1)-dimensional generalized KP equation, Commun. Nonlinear Sci. Numer. Simulat., 17, 491-495, 2012.
4. M. Eslami, Solitary Wave solutions to the (3+1)-dimensional Jimbo-Miwa equation, Caspian Journal of Mathematical Sciences, 2(2), 115-122, 2014.

## **GAIN SCHEDULING PI CONTROL OF AN ELECTRO-HYDRAULIC ACTUATOR FOR ACTIVE SUSPENSION SYSTEMS**

**Cem Onat, Mahmut Daskin, Abdullah Turan**

Department of Mechanical Engineering, Inonu University, Malatya, Turkey  
cem.onat@inonu.edu.tr, mahmut.daskin@inonu.edu.tr

### **Abstract**

The controller structure of the active suspension system is generally decomposed into two loops namely outer loop and inner loop controllers. Outer loop controller is used to calculate the optimum target force to reject the effects of road disturbances, while, the inner loop controller is used to keep the actual force close to this desired force. The inner loop controller design is challenge because models of the electro-hydraulic systems include high order nonlinearity. In this study, a gain scheduling linear model corresponded with nonlinear model of a hydraulic force actuator system is based. Next, gain scheduling PI controller for the inner loop is designed by using of weighted geometrical center method. The proposed controller structure comprises a feed forward loop. The gain scheduling model is constituted in two distinct and consecutive stages. In first step, nonlinear terms caused nonlinearity are described by measurable or observable system parameters and embedded in a nonlinear scheduling parameter. In this way, the scheduling parameter is continuously extracted from real system. In second step, the nonlinear system equation is rearranged by the scheduling parameter and, parameter varying linear model is obtained. The simulation which is performed by using of Matlab-Simulink computer program show that the proposed gain scheduling controller structure overcomes nonlinear actuator dynamics, and desired force is smoothly traced to the nonlinear system model.

**Keywords:** Electro-Hydraulic; Nonlinear model; Parameter varying model; PI controller

### **REFERENCES**

1. Hrovat D., Survey of Advanced Suspension Developments and Related Optimal Control Applications. *Automatica*. 33(10), 1781-1817, 1997.
2. Shen X., Peng H., Analysis of Active Suspension Systems with Hydraulic Actuators, Proceedings of the 2003 IAVSD Conference, Atsugi, Japan, August, 2003.
3. Zhang Y., Alleyne A., A Practical and Effective Approach to Active Suspension Control, Proceedings of the 6th International Symposium on Advanced Vehicle Control, Hiroshima, Japan September, 2002.

## HALF INVERSE PROBLEM FOR HILL'S EQUATION

Ahu ERCAN<sup>1</sup>, Etibar S. PANAKHOV<sup>1,2</sup>

<sup>1</sup>Department of Mathematics, University of Firat, Elazig, Turkey

<sup>2</sup> Institute of Applied Mathematics, University of Baku State, Baku, Azerbaijan  
ahuduman24@gmail.com, epenahov@hotmail.com,

### Abstract

In this study, half inverse problem for Hill equation is considered. It's shown by Hochstadt–Lieberman's method that if the potential function is prescribed  $q(x)$  on the interval  $(\frac{\pi}{2}, \pi)$ , then a single spectrum suffices to determine  $q(x)$  on the whole interval  $(0, \pi)$ . However, half inverse problem for Hill equation is to construct of the operator in a whole interval by using two spectrum and potential known in a semi interval.

**Keywords:** Half inverse problem; Hill equation; Inverse spectral problem.

### REFERENCES

1. H. Hochstadt, On the determination of a Hill's equation from its spectrum, Arch. Rational Mech. Anal., Vol:19, 353–3622, 1965.
2. H. Hochstadt, An inverse problem for a Hill's equation, Journal of Differential Equations, Vol:20, 53–60, 1976.
3. H. Hochstadt, B. Lieberman, An inverse Sturm–Liouville problem with mixed given data, SIAM J. Appl. Math. Vol:34, 676–680, 1978.
4. H. Koyunbakan, E.S Panakhov, Half-inverse problem for diffusion operators on the finite interval, J. Math. Anal. Appl., Vol:326, 1024–1030, 2007.

## HALF INVERSE PROBLEM FOR A DISCONTINUOUS INTEGRO DIFFERENTIAL OPERATOR

Etibar Panakhov<sup>1,2</sup>, Ahu Ercan<sup>2</sup>

<sup>1</sup> Institute of Applied Mathematics, University of Baku State, Baku, Azerbaijan

<sup>2</sup> Department of Mathematics, University of Firat, Elazig, Turkey  
epenahov@hotmail.com, ahuduman24@gmail.com

### Abstract

In this study, we solve a half inverse problem for discontinuous integro differential operator by using Hochstadt-Lieberman's method. Half- inverse problem for a Sturm-Liouville operator consist in reconstruction of the operator from its spectrum and half of the potential.

**Keywords:** Integro-differential equation; Discontinuity; Half inverse problem.

### REFERENCES

1. H. Hochstadt, B. Lieberman, An inverse Sturm–Liouville problem with mixed given data, SIAM J. Appl. Math. Vol:34, 676–680, 1978.
2. H. Koyunbakan, E.S Panakhov, Half-inverse problem for diffusion operators on the finite interval, J. Math. Anal. Appl., Vol:326, 1024–1030, 2007.
3. B. Keskin, A.S. Ozkan, Spectral problem for a discontinuous Integro-Differential operator, Ukrainian Mathematical Journal, Vol:64, No:2, 309-315, 2012.
4. A.S. Ozkan, Half-inverse Sturm-Liouville problem with boundary and discontinuity conditions dependent on the spectral parameter, Inv.Probl. Sci. Eng., Vol:22, No:5, 848-859, 2013.



## NEW FUNCTION METHOD TO SOLVE THE ZHIBER-SHABAT EQUATION

Yusuf Gurefe<sup>1</sup>, Tolga Akturk<sup>2</sup>, Yusuf Pandir<sup>3</sup>

<sup>1</sup>Department of Econometrics, Usak University, Usak, Turkey

<sup>2</sup>Department of Mathematics and Science Education, Ordu University, Ordu, Turkey

<sup>3</sup>Department of Mathematics, Bozok University, Yozgat, Turkey  
ygurefe@gmail.com, tolgaakturk@gmail.com, yusufpandir@gmail.com

### Abstract

In this study, we use the new function method to find new exact solutions of the Zhiber-Shabat equation. This equation is very important for the mathematical modelling of the physical problems in real world applications. From this point of view, we obtain traveling wave solution including Jacobi elliptic function by the new function method. So, it can be easily seen that the obtained results for the Zhiber-Shabat equation give us a new behaviour in physical sense.

**Keywords:** New functionmethod; Zhiber-Shabatequation; Jacobiellipticfunctionsolutions.

### REFERENCES

1. Guicheng Shen, Yunchuan Sun, Yongping Xiong, New travelling-wavesolutionsforDodd-Bullough equation, Journal of Applied Mathematics, Vol:2013, 5pages, 2013.
2. Yunchuan Sun, New travellingwavesolutionsfor Sine-Gordon equation, Journal of Applied Mathematics, Vol:2014, 4 pages, 2014.
3. Hasan Bulut, Tolga, Akturk, Yusuf Gurefe, Travelingwavesolutions of the (N+1)-dimensional sine-cosine-Gordon equation, AIP Conference Proceedings, Vol:1637, No:1, 145–149, 2014.
4. Hasan Bulut, Tolga, Akturk, Yusuf Gurefe, An application of thenewfunctionmethodtothegeneralizeddoublesinh-Gordon equation, AIP Conference Proceedings, Vol:1648, 4 Pages,2015.
5. Yaning Tang, Wei Xu, Jianwei Shen, Liang Gao, Bifurcations of travelingwavesolutionsfor Zhiber-Shabat equation, Nonlinear Analysis: Theory, Methods and Applications, Vol:67, No:2, 648–656, 2007.

## **ANALYSIS OF KELLER-SEGEL MODEL WITH CAPUTO AND CAPUTO-FABRIZIO DERIVATIVES**

**Mustafa Ali Dokuyucu<sup>1</sup>, Ercan Çelik<sup>2</sup>**

<sup>1</sup>Department of Mathematics, Faculty of Science and Arts, Ağrı İbrahim Çeçen University,  
Ağrı, Turkey

<sup>2</sup>Department of Mathematics, Faculty of Science, Atatürk University, Erzurum, Turkey  
madokuyucu@agri.edu.tr, ercelik@atauni.edu.tr

### **Abstract**

In this work, we analysed the Keller-Segel model with Caputo and Caputo-Fabrizio fractional derivatives. Using the fixed-point theorem, we present the existence and uniqueness of the coupled solutions for both definitions of fractional derivatives. We also analysed uniqueness of the solutions. A comparison of the results obtained is given using *Mathematica*.

**Keywords:** Keller-Segel model, Caputo fractional derivative, Caputo-Fabrizio fractional derivative.

### **REFERENCES**

1. M. Caputo, Linear model of dissipation whose Q is almost frequency independent -II. Geophys J R Astr Soc, 13, 529-539, 1967
2. M. Caputo, Geophys. J. Int. 13, 529 (1967) reprinted in Fract. Calculus Appl. Anal. 11, 3, 2008.
3. I. Podlubny, Fractional Differential Equations, Academic Press, San Diego, 1999.
4. M. Caputo, M. Fabrizio, A new definition of fractional derivative without singular kernel, Progr. Fract. Differ. Apply.,1,73-85, 2015.
5. J. Losada, J.J. Nieto, Properties of a New Fractional Derivative without singular kernel, Progr. Fract. Differ. Apply.,1,87-92, 2015.
6. A. Atangana, S. Badr, Analysis of the Keller-Segel model with a fractional derivative without singular kernel, Entropy, 17, 4439-4453, 2015.
7. Atangana A, Baleanu D., New fractional derivatives with nonlocal and non-singular kernel: theory and application to heat transfer model. Therm. Sci. 2016. OnLine-First (00). 18. 10.2298/TSCI160111018A).

## **REGARDING ON THE NOVEL FORMS OF THE (3+1)- DIMENSIONAL KADOMTSEV-PETVIASHVILI EQUATION**

**Hasan Bulut<sup>1</sup>, Betül Demirdağ<sup>2</sup>, Hacı Mehmet Baskonus<sup>3</sup>**

<sup>1,2</sup>Department of Mathematics, University of Firat, Elazig, Turkey

<sup>3</sup>Department of Computer Engineering, University of Munzur, Tunceli, Turkey  
hbulut@firat.edu.tr, betuldenizd@gmail.com, hmbaskonus@gmail.com

### **Abstract**

In this study, we have applied the Bernoulli Sub-Equation method to the (3+1)-Dimensional Kadomtsev-Petviashvili equation. We have obtained some new analytical solutions such as exponential function and rational solutions by using this technique. We have observed that two analytical solutions have been verified the (3+1)-Dimensional Kadomtsev-Petviashvili equations by using Wolfram Mathematica 9. At the end of this manuscript, we submitted a conclusion in a comprehensive manner.

**Keywords:** Bernoulli function method; (3+1)-Dimensional Kadomtsev-Petviashvili equation; Exponential function solution; rational function solution.

### **REFERENCES**

1. Ahmet Bekir, Ferhat Uygun, Exact travelling wave solutions of nonlinear evolution equations by using the  $(\frac{G'}{G})$ - expansion method, Arab Journal of Mathematical Sciences, Vol:18, 73–85, 2012.
2. H. Bulut, S. S. Atas and H. M. Baskonus, Some Novel Exponential Function Structures to the Cahn-Allen Equation, Cogent Physics, 3:1240886, 2016.
3. H. Bulut, G. Yel, H.M. Baskonus, An Application Of Improved Bernoulli Sub-Equation Function Method To The Nonlinear Time-Fractional Burgers Equation, Turkish Journal of Mathematics and Computer Science, Vol:5, 1-7, 2016.
4. H. Zhao, C. Bai, New doubly periodic and multiple soliton solutions of the generalized (3+1)-dimensional Kadomtsev-Petviashvili equation with variable coefficients, Chaos, Solitons & Fractals, 30 (2006) 217.

## **DISCRETE FRACTIONAL SOLUTIONS OF A CHEBYSHEV EQUATION**

**Resat Yilmazer**

Department of Mathematics, University of Firat, Elazig, Turkey  
rstyilmazer@gmail.com,

### **Abstract**

Fractional calculus is a field of applied mathematics that deals with derivatives and integrals of arbitrary orders, and their applications appear in various fields in science, engineering, applied mathematics, economics, such as, viscoelasticity, diffusion, neurology, control theory, and statistics [1-3]. Therefore it has achieved significance during the past three decades. The similar theory for discrete fractional calculus was begun and features of the theory of fractional sums and differences were constituted. Many papers related to this topic have seemed recently [4-5].

In this work, we acquire some new particular solutions of the homogeneous and nonhomogeneous Chebyshev's equations by using discrete fractional nabla operator.

**Keywords:** Discrete fractional calculus; Chebyshev equation; Nabla operator.

### **REFERENCES**

1. K.S. Miller, B. Ross, An Introduction to the Fractional Calculus and Fractional Differential Equations, John Wiley and Sons, Inc., New York, 1993.
2. I. Podlubny, Fractional differential equations, Academic Press, New York, London, Tokyo and Toronto, 1999.
3. K., Nishimoto, Fractional Calculus, Descartes Press, vol. I 1984, vol. II 1987, vol. III 1989, vol. IV 1991, vol. V, 1996.
4. F.M. Atıcı, P.W. Eloe, Discrete fractional calculus with the nabla operator, Electronic Journal of Qualitative Theory of Differential Equations, Spec. Ed I, 3 1-12, 2009.
5. G.A. Anastassiou, Right nabla discrete fractional calculus, Int. J. Difference Equations 6 91-104, 2011.

## AN APPLICATION OF THE NISHIMOTO'S OPERATOR FOR THE RADIALSCHRÖDINGER EQUATION

Resat Yilmazer<sup>1</sup> and Okkes Ozturk<sup>2</sup>

<sup>1</sup> Department of Mathematics, University of Firat, Elazig, Turkey

<sup>2</sup> Department of Mathematics, University of Bitlis Eren, Bitlis, Turkey  
rstyilmazer@gmail.com, oozturk27@gmail.com

### Abstract

Fractional calculus and its generalizations are used for the solutions of some classes of differential equations and fractional differential equations. Fractional calculus techniques contribute to many fields of science and engineering such as applied mathematics, control theory, economy, nuclear magnetic resonance, geometric mechanics, optics, robot technology, heat transfer and so on [1-4]. In this study, our aim is to obtain fractional solutions of the radial Schrödinger equation via the Nishimoto's operator  $N^\mu$ .

**Keywords:** Fractional calculus, The Nishimoto's Operator, Radial Schrödinger equation.

### REFERENCES

1. Podlubny, I., Fractional differential equations: an Introduction to fractional derivatives, fractional differential equations, methods of their solution and some of their applications, mathematics in science and engineering, vol. 198, Academic Press, New York, London, Tokyo and Toronto, 1999.
2. Yilmazer, R., Ozturk, O., Explicit solutions of singular differential equation by means of fractional calculus operators, Abstract and Applied Analysis, 2013, 6 pages, 2013.
3. Nishimoto, K., Fractional Calculus, Descartes Press, vol. I 1984, vol. II 1987, vol. III 1989, vol. IV 1991, vol. V, 1996.
4. Ortigueira, M. D., Fractional Calculus for Scientists and Engineers, Springer, Heidelberg, 2011.

## A 3-SCALE HAAR WAVELET COLLOCATION METHOD FOR SOLVING PDEs

Fatih Bulut<sup>1</sup>, Ömer Oruç<sup>2</sup>, Alaattin Esen<sup>3</sup>

<sup>1</sup> Department of Physics, Inonu University, Malatya, Turkey

<sup>2</sup> Aralik Anatlia High School, Iğdır, Turkey

<sup>3</sup> Department of Mathematics, Inonu University, Malatya, Turkey

fatih.bulut@inonu.edu.tr

### Abstract

In this study, we analyze the performance of a numerical scheme based on 3-scale Haar wavelets for solving PDEs. For solution process firstly we rewrite the time dependent partial differential equation as a system of partial differential equations by introducing a new variable and then we use finite difference approximation for discretization of time dependent variables and for discretization of spatial variables we use 3-scale Haar wavelets. By doing so, we obtain a system of algebraic equations whose solution gives wavelet coefficients for constructing numerical solution of partial differential equation. To test the accuracy and reliability of the numerical scheme based on 3-scale Haar wavelets, we applied it on various test problems which consist of variable and constant coefficient, homogeneous and non-homogeneous partial differential equations. The obtained results are compared wherever possible with those from previous studies. Numerical results are tabulated and depicted graphically.

**Keywords:** 3-Scale Haar wavelets, PDEs, Numerical solution

### REFERENCES

1. R.C. Mittal, R.K. Jain, B-splines methods with redefined basis functions for solving fourth order parabolic partial differential equations, *Appl. Math. Comput.* 217 (2011) 9741–9755.
2. C.H. Hsiao, W.J. Wang State analysis of time-varying singular bilinear systems via Haar wavelets. *Math. Comput. Simul.*, 52 (2000) 11–20.
3. U. Lepik, Numerical solution of differential equations using Haar wavelets, *Math. Comput. Simul.* 68 (2005) 127–143
4. Ö. Oruç, F. Bulut, A. Esen, A Haar wavelet-finite difference hybrid method for the numerical solution of the modified Burgers' equation, *Journal of Mathematical Chemistry*, 53 (7) (2015) 1592–1607.

## **DOUBLE DIFFUSIVE MIXED CONVECTION IN A NANOFUID FILLED CONFINED CAVITY HEATED FROM BOTTOM WALL**

**S. Hussain<sup>1,2</sup>, H. F. Oztop<sup>3</sup>**

Department of Mathematics, Capital University of Science and Technology, Islamabad,  
Pakistan<sup>1</sup>

Institut für Angewandte Mathematik (LS III), Technische Universität, Dortmund, Germany<sup>2</sup>

Department of Mechanical Engineering, Technology Faculty, Firat University, 23119 Elazig,  
Turkey<sup>3</sup>

shafqat.hussain@cust.edu.pk, hfoztop1@gmail.com

### **Abstract**

A computational solution has been performed to analysis heat and fluid flow double diffusive mixed convection in a nanofluid filled confined enclosure heater from the bottom side. Vertical walls are chosen as adiabatic. Governing parameters are solved via Galerkin finite element method in space and the Crank-Nicolson in time. The study is performed in the range of parameters with different Lewis number, Reynolds number, Richardson number and buoyancy ratio. It is found that all parameters are effective on number of cells inside the cavity. It is observed that heat transfer increases with increasing of nanoparticle volume fraction and decreases with Hartmann number.

### **REFERENCES**

1. A. Kumar, A. K. Singh, P. Chandran, and N. C. Sacheti, \Effect of perpendicular magnetic field on free convection in a rectangular cavity," Sultan Qaboos University Journal for Science, vol. 20(2), pp. 49-59, 2015.
2. M. Sheikholeslami, M. G. Bandy, and D. Ganji, \Numerical investigation of MHD effects on Al<sub>2</sub>O<sub>3</sub>-water nanofluid flow and heat transfer in a semi-annulus enclosure using LBM," Energy, vol. 60, pp. 501-510, 2013.
3. S. Das, A. S. Banu, R. N. Jana, and O. D. Makinde, \Entropy analysis on MHD pseudo-plastic nanofluid flow through a vertical porous channel with convective heating," Alexandria Engineering Journal, vol. 54, pp. 325-337, 2015.
4. S. Das, R. N. Jana, and O. D. Makinde, \Mixed convective magnetohydrodynamic flow in a vertical channel filled with nanofluids," Engineering Science and Technology, an International Journal, vol. 18, pp. 244-255, 2015.

## **CAPTURING THE BEHAVIOR OF ADVECTION- DIFFUSION PROCESS THROUGH MONTE CARLO SIMULATION**

**Murat Sari, Arshed A. Ahmad, Lamyaa Almashhadani**

Department of Mathematics, Faculty of Arts and Science, Yildiz Technical University,  
Istanbul, Turkey  
sarim@yildiz.edu.tr

### **Abstract**

This study investigates physical behavior of the advection-diffusion process using Monte Carlo simulation approaches. This is carried out by walking randomly in the solution region and then the solution is recorded at the end of each random walk at one point at a specified time. Simultaneously solving the model equation has advantages comparison to the numerical methods. For computational purposes, the simulated results are compared with the finite difference results. To properly understand the behavior of the physical processes, the calculated solutions have been discussed in detail. The considered techniques are seen to be promising in realizing the processes.

**Keywords:** Advection-diffusion process, Monte Carlo simulation, physical behavior, mathematical modelling

### **REFERENCES**

1. D. Irk, I. Dag, M. Tombul, Extended cubic B-spline solution of the advection-diffusion equation, KSCE Journal of Civil Engineering, 19 (2015) 929-934.
2. A. Korkmaz, I. Dag, Quartic and quintic B-spline methods for advection-diffusion equation, Applied Mathematics and Computation, 274 (2016) 208-219.
3. M. Sari, G. Gurasrslan, A. Zeytinoglu, High-order finite difference schemes for solving the advection-diffusion equation, Mathematical and Computational Applications 15 (2010) 449-460.
4. S.J. Farlow, Partial Differential Equations for Scientists and Engineers, John Wiley & Sons, New York, 1982.
5. M.N.O. Sadiku, Monte Carlo Methods for Electromagnetics, USA, 2009.



# NUMERICAL INVESTIGATION ON MHD FLOW AND HEAT TRANSFER OVER AN EXPONENTIALLY STRETCHING SHEET WITH VISCOUS DISSIPATION AND RADIATION EFFECTS

**İnci ÇİLİNGİR SÜNGÜ**

Department of Mathematics, University of Ondokuz Mayıs, Samsun, Turkey  
incicilingir@gmail.com

## **Abstract**

This study is to examine the steady two-dimensional laminar flow of a viscous incompressible electrically conducting fluid over a continuous surface. In this study DTM-Padé method is used to solve which is a combination of differential transform method (DTM) and Padé approximant. Comparisons between the solutions obtained by DTM and DTM-Padé and are shown that DTM-Padé is the completely powerful method for solving the problems in which boundary conditions at infinity. Also in this study, the effect of Magnetic and Radiation parameters, Prandtl number and Eckert number for velocity and temperature distributions are investigated.

**Keywords:**DTM, DTM-Padé, MHD, Exponentially Stretching Sheet, Boundary layer flow

## **REFERENCES**

1. A. Ishak, MHD boundary layer flow due to an exponentially stretching sheet with radiation effect, *Sains Malaysiana*, 40(2011), 391-395.
2. B. Bidin and R. Nazar, Numerical solution of the boundary layer flow over an exponentially stretching sheet with thermal radiation, *European journal of scientific research*, 33(2009), 710-717.
3. R. N. Jat and Gopi Chand, MHD Flow and Heat Transfer over an Exponentially Stretching Sheet with Viscous Dissipation and Radiation Effects *Applied Mathematical Sciences*, Vol. 7, 2013, no. 4, 167 – 180.
4. M.M. Rashidi, T. Hayat, M. Keimanesh, and H. Yousefian, A Study on Heat Transfer in a Second-Grade Fluid Through a Porous Medium with the Modified Differential Transform Method, *Heat Transfer—Asian Research*, 42 (1), 2013.
5. M. Azimi, D. D. Ganji, F. Abbassi, Study on MHD Viscous Flow over a Stretching Sheet Using DTM-Padé' Technique *Modern Mechanical Engineering*, 2012, 2, 126-129.

## VARIOUS METHODS FOR THE BURGERS EQUATION

**Murat Sari, Eren Dincer**

Department of Mathematics, Faculty of Arts and Science, Yildiz Technical University,  
Istanbul, Turkey  
sarim@yildiz.edu.tr

### **Abstract**

This study aims at numerically solving the one-dimensional Burgers equations using up to sixth-order finite difference and sixth-order compact finite difference schemes. These methods are applied for discretizing spatial derivatives and strong stability-preserving third-order (SSP3) time discretization method for the time integration of the resulting system. In addition, the Lax-Wendroff and MacCormack method are adapted to numerically approximate Burgers equation. The proposed methods are demonstrated by two test problems. The produced results are in very good agreement with the exact solution and the literature.

**Key Words:** Burgers equation; High-order finite difference scheme; Compact finite difference scheme; Lax-Wendroff method; MacCormack method

### **REFERENCES**

1. J.M. Burgers, A mathematical model illustrating the theory of turbulence, Adv. Appl. Mech. 1 (1948) 171-199.
2. R.C. Mittal, R.K. Jain, Numerical solutions of nonlinear Burgers' equation with modified cubic B-splines collocation method, Appl. Math. Comput. 218 (2012), 7839-7855.
3. A.A. Soliman, A Galerkin solution for Burgers' equation using cubic B-spline finite elements, Abstract Appl. Anal. doi: 10.1155/2012/527467.
4. B. Inan, A.R. Bahadir, A numerical solution of the Burgers' equation using a crank-nicolson exponential finite difference method, J. Math. Comput. Sci. 4 (2014) No.5 849-860.
5. M. Khan, A novel solution technique for two dimensional Burgers' equation, Alex. Engng. J. 53 (2014) 485-490.
6. M. Sari, G. Gürarlan, A sixth-order compact finite difference scheme to the numerical solutions of Burgers' equation, Appl. Math. Comput. 208 (2009) 475-483.

# ON SOME PROPERTIES OF SEQUENCE SPACES DEFINED BY A SEQUENCE OF MODULUS FUNCTION

Çiğdem A. BEKTAŞ, Sinan ERCAN

Department of Mathematics, University of Firat, Elazig, Turkey

cbektas@firat.edu.tr, sinanercan45@gmail.com

## Abstract

In this study, we introduce the generalized new sequence spaces defined by using a sequence of modulus function. We give some topological properties and inclusion relations between these spaces.

**Keywords:** Modulus function; Paranorm space.

## REFERENCES

1. I. J. Maddox, Elements of functional analysis, Cambridge Univ. Press, 1970.
2. M. Mursaleen, A. K. Noman, On the Spaces of  $\lambda$ -convergent and bounded sequences, Thai Journal of Mathematics, vol. 8, no. 2, pp. 311–329, 2010.
3. N. L. Braha, F. Başar, On the domain of triangle  $A(\lambda)$  on the spaces of null, convergent and bounded sequences, Abstract and Applied Analysis, Volume 2013, Article ID 476363, 9 pages.
4. S. K. Sharma, Generalized sequence spaces defined by a sequence of moduli, Journal of Egyptian Mathematical Society, 23, 73-77, 2015.

# ON STATISTICAL CONVERGENCE OF SEQUENCES GENERATED BY THE DIFFERENCE OPERATOR OF FRACTIONAL ORDER

Sinan ERCAN, Çiğdem A. BEKTAŞ

Department of Mathematics, University of Firat, Elazig, Turkey

sinanercan45@gmail.com, cbektas@firat.edu.tr

## Abstract

In this study, we introduce the concept of statistical convergence for difference sequences of fractional order. Some various properties of this concept of statistical convergence are examined.

**Keywords:** Sequences; Statistical convergence.

## REFERENCES

1. H. Fast, Sur la convergence statistique, Colloq. Math., 2, 241-244, 1951.
2. J. Fridy, On statistical convergence, Analysis, 5, 301-313, 1985.
3. T. Šalát, On statistically convergent sequences of real numbers, Math. Slovaca, 30, 139-150, 1980.
4. I. J. Schoenberg, The integrability of certain functions and related summability methods, Amer. Math. Monthly, 66, 361-375, 1959.
5. H. Steinhaus, Sur la convergence ordinaire et la convergence asymptotique, Colloquium Mathematicum, 2, 73-74, 1951.
6. A. Zygmund, Trigonometric series, Cambridge University Press, Cambridge, 1979.
7. P. Baliarsingh, Some new difference sequence spaces of fractional order and their dual spaces, Applied Mathematics and Computation, vol. 219, no. 18, pp. 9737–9742, 2013.

## **ON SOME COMPLEX ASPECTS OF THE (2+1)- DIMENSIONAL BROER-KAUP-KUPERSHMIDT SYSTEM**

**Hasan Bulut<sup>1</sup>, Hilal Arslanoglu Isik<sup>2</sup>, Tukur Abdulkadir Sulaiman<sup>3</sup>**

<sup>1,3</sup>Faculty of Science, Firat University of, Elazig, Turkey

<sup>2</sup>Faculty of Engineering, Munzur University, Tunceli, Turkey

<sup>3</sup>Faculty of Science, Federal University, Dutse, Jigawa, Nigeria

hbulut@firat.edu.tr, h\_arslanoglu@hotmail.com, sulaiman.tukur@fud.edu.ng

### **Abstract**

The improved Bernoulli sub-equation function method is used in extracting some new exponential function solutions to the (2+1)-dimensional Broer-Kaup-Kupershmidt system. It is of vital effort to look for more solutions of the (2+1)-dimensional Broer-Kaup-Kupershmidt system, which are very helpful for coastal and civil engineers to apply the nonlinear water models in a harbor and coastal design. All the obtained solutions satisfied the (2+1)-dimensional Broer-Kaup-Kupershmidt system. We also plot the two- and three-dimensional graphics of all the obtained solutions in this study. All the computations and the graphics plots in this study are carried out with the help of the Wolfram Mathematica 9.

**Keywords:**The improved Bernoulli sub-equation function method; the (2+1)-dimensional Broer-Kaup-Kupershmidt system; complex hyperbolic structure

### **REFERENCES**

1. H.M. Baskonus and H. Bulut, Exponential Prototype Structure for (2+1)-Dimensional Boiti-Leon-Pempinelli System in Mathematical Physics, Waves in Random and Complex Media, 26(2), 189-196, 2016.
2. M. Song, S. Li and J. Cao, New Exact Solutions for the (2+1)-dimensional Broer-Kaup-Kupershmidt Equations, Abstract and Applied Analysis, 2010, 652649, 2010.
3. H. Bulut, T.A. Sulaiman and H.M. Baskonus, New Solitary and Optical Wave Structures to the Korteweg-de Vries Equation with Dual-Power Law Nonlinearity, Opt. Quant. Electron, 48(564), 1-14, 2016.

## NEW GENERALIZATIONS OF EXTENDED GAMMA AND BETA FUNCTIONS

Recep Şahin<sup>1</sup>, M. Baki Yağbasan<sup>2</sup>, Ayşegül Çetinkaya<sup>2</sup>, İ. Onur Kıymaz<sup>2</sup>, Oğuz Yağcı<sup>1</sup>

<sup>1</sup> Department of Mathematics, University of Kırıkkale, Kırıkkale-Turkey

<sup>2</sup> Department of Mathematics, University of Ahi Evran, Kırşehir-Turkey  
receptsahin@kku.edu.tr

### Abstract

In this study, we introduce a new generalization of extended gamma and beta functions. We also define a new generalization of Pochhammer symbol and Macdonald function by using the new generalized gamma function. Then we investigate their properties.

**Keywords:** Gamma function; Beta function; Pochhammer symbol; Macdonald function.

### REFERENCES

1. Bailey W.N., Generalized Hypergeometric Series, Cambridge Tracts in Mathematics and Mathematical Physics, vol. 32, Cambridge University Press, Cambridge, 1935.
2. Chaudhry M. A., Qadir A., Rafique M., Zubair S. M., Extension of Euler's beta function, J. Comput. Appl. Math., 78, 19-32, 1997.
3. Chaudhry M. A., Qadir A., Srivastava H. M., Paris R. B., Extended hypergeometric and confluent hypergeometric functions, Appl. Math. Comput., 159 (2), 589-602, 2004.
4. Erdélyi A., Magnus M., Oberhettinger F., Tricomi F.G., Higher Transcendental Functions, vol. I, McGraw-Hill Book Company, New York, 1953.
5. Srivastava H. M., Çetinkaya A., Kıymaz İ. O., A certain generalized Pochhammer symbol and its applications to hypergeometric functions, Appl. Math. Comput., 226, 484-491, 2014.

## NEW GENERALIZATIONS OF GAUSS AND CONFLUENT HYPERGEOMETRIC FUNCTIONS

Oğuz Yağcı<sup>1</sup>, Recep Şahin<sup>1</sup>, M. Baki Yağbasan<sup>2</sup>, Ayşegül Çetinkaya<sup>2</sup>, İ. Onur Kıymaz<sup>2</sup>

<sup>1</sup>Department of Mathematics, University of Kırıkkale, Kırıkkale-Turkey

<sup>2</sup>Department of Mathematics, University of Ahi Evran, Kırşehir-Turkey

oguzyagci26@gmail.com

### Abstract

In this work, we introduce new generalizations of Gauss and confluent hypergeometric functions by using generalized extended beta functions. We also investigate their properties such as integral representations, summation and transformation formulas, Mellin transforms and difference operators.

**Keywords:** Beta function; Gauss hypergeometric functions; Confluent hypergeometric functions; Integral representations, Mellin transforms.

### REFERENCES

1. M. A. Chaudhry, A. Qadir, M. Raque, and S. M. Zubair, Extension of Euler's Beta function, J. Comput. Appl. Math. 78, 19-32, 1997.
2. M. A. Chaudhry, A. Qadir, H. M. Srivastava, and R. B. Paris, Extended hypergeometric and confluent hypergeometric functions, Appl. Math. Comput. 159, 589-602, 2004.
3. A. Erdelyi, W. Magnus, F. Oberhettinger and F. G. Tricomi, Tables of Integral Transforms, Vol. I, McGraw-Hill Book Company, New York, Toronto and London, 1954.
4. E. D. Rainville, Special Functions, Macmillan Company, New York, 1960; Reprinted by Chelsea Publishing Company, Bronx, New York, 1971.
5. L. J. Slater, Generalized Hypergeometric Functions, Cambridge University Press, Cambridge, London, and New York, 1966.
6. H. M. Srivastava and P. W. Karlsson, Multiple Gaussian Hypergeometric Series, Halsted Press (Ellis Horwood Limited, Chichester), John Wiley and Sons, New York, Chichester, Brisbane and Toronto, 1985.

## ON A NEW GENERALIZATION OF RIEMANN-LIOUVILLE FRACTIONAL DERIVATIVE OPERATOR

Ayşegül Çetinkaya<sup>1</sup>, İ. Onur Kıymaz<sup>1</sup>, Recep Şahin<sup>2</sup>, M. Baki Yağbasan<sup>1</sup>, Oğuz Yağcı<sup>2</sup>

<sup>1</sup> Department of Mathematics, University of Ahi Evran, Kırşehir-Turkey

<sup>2</sup> Department of Mathematics, University of Kırıkkale, Kırıkkale-Turkey

acetinkaya@ahievran.edu.tr

### Abstract

In this work, we introduced a new generalization of Riemann-Liouville fractional derivative operator and by using a new generalization of extended beta function we also defined generalizations of some hypergeometric functions. Then we obtained generalized Riemann-Liouville fractional derivatives of some functions and used them to determine linear and bilinear generating relations for these generalized hypergeometric functions.

**Keywords:** Beta function; Hypergeometric functions; Riemann-Liouville fractional derivative; Generating functions.

**Acknowledgement:** This work was supported by Ahi Evran University Scientific Research Projects Coordination Unit. Project Number: FEF.E2.17.027

### REFERENCES

1. Agarwal P., Choi J., Paris R. B., Extended Riemann-Liouville fractional derivative operator and its applications, *J. Nonlinear Sci. Appl.*, 8, 451-466, 2015.
2. Baleanu D., Parmar R. K., Agarwal P., Salahshour S., Extension of the fractional derivative operator of the Riemann-Liouville, *J. Nonlinear Sci. Appl.*, 2017. (accepted)
3. Chaudhry M. A., Qadir A., Rafique M., Zubair S. M., Extension of Euler's beta function, *J. Comput. Appl. Math.*, 78, 19-32, 1997.
4. Chaudhry M. A., Qadir A., Srivastava H. M., Paris R. B., Extended hypergeometric and confluent hypergeometric functions, *Appl. Math. Comput.*, 159 (2), 589-602, 2004.
5. Kıymaz İ. O., Çetinkaya A., Agarwal P., An extension of Caputo fractional derivative operator and its applications, *J. Nonlinear Sci. Appl.*, 9, 3611-3621, 2016.
6. Kilbas A. A., Srivastava H. M., Trujillo J. J., *Theory and Applications of Fractional Differential Equations*, Elsevier, Amsterdam etc., 2006.
7. Özarıslan M. A., Özergin E., Some generating relations for extended hypergeometric functions via generalized fractional derivative operator, *Mathematical and Computer Modelling*, 52, 1825-1833, 2010.



## ON A NEW GENERALIZATION OF CAPUTO FRACTIONAL DERIVATIVE OPERATOR

İ. Onur Kıymaz<sup>1</sup>, Ayşegül Çetinkaya<sup>1</sup>, M. Baki Yağbasan<sup>1</sup>, Recep Şahin<sup>2</sup>, Oğuz Yağcı<sup>2</sup>

<sup>1</sup> Department of Mathematics, University of Ahi Evran, Kırşehir-Turkey

<sup>2</sup> Department of Mathematics, University of Kırıkkale, Kırıkkale-Turkey

iokiymaz@ahievran.edu.tr

### Abstract

In this work, we introduced a new generalization of Caputo fractional derivative operator and by using a new generalization of extended beta function we also defined generalizations of some hypergeometric functions. Then we obtained generalized Caputo fractional derivatives of some functions and used them to determine linear and bilinear generating relations for these generalized hypergeometric functions.

**Keywords:** Beta function; Hypergeometric functions; Caputo fractional derivative; Generating functions.

**Acknowledgement:** This work was supported by Ahi Evran University Scientific Research Projects Coordination Unit. Project Number: FEF.E2.17.026

### REFERENCES

1. Agarwal P., Choi J., Paris R. B., Extended Riemann-Liouville fractional derivative operator and its applications, *J. Nonlinear Sci. Appl.*, 8, 451-466, 2015.
2. Baleanu D., Parmar R. K., Agarwal P., Salahshour S., Extension of the fractional derivative operator of the Riemann-Liouville, *J. Nonlinear Sci. Appl.*, 2017. (accepted)
3. Chaudhry M. A., Qadir A., Rafique M., Zubair S. M., Extension of Euler's beta function, *J. Comput. Appl. Math.*, 78, 19-32, 1997.
4. Chaudhry M. A., Qadir A., Srivastava H. M., Paris R. B., Extended hypergeometric and confluent hypergeometric functions, *Appl. Math. Comput.*, 159 (2), 589-602, 2004.
5. Kıymaz İ. O., Çetinkaya A., Agarwal P., An extension of Caputo fractional derivative operator and its applications, *J. Nonlinear Sci. Appl.*, 9, 3611-3621, 2016.
6. Kilbas A. A., Srivastava H. M., Trujillo J. J., *Theory and Applications of Fractional Differential Equations*, Elsevier, Amsterdam etc., 2006.
7. Özarlan M. A., Özergin E., Some generating relations for extended hypergeometric functions via generalized fractional derivative operator, *Mathematical and Computer Modelling*, 52, 1825-1833, 2010.

**NOVEL STRUCTURE TO THE COUPLED NONLINEAR MACCARI'S  
SYSTEM BY USING MODIFIED TRIAL EQUATION METHOD**

**Gülnur Yel<sup>1</sup>, Hacı Mehmet Baskonus<sup>2</sup>, Hasan Bulut<sup>3</sup>**

<sup>1</sup>Department of Mathematics Education, Final International University, Kyrenia, TRNC

<sup>2</sup>Department of Computer Engineering, Munzur University, Tunceli, Turkey

<sup>3</sup>Department of Mathematics, University of Firat, Elazig, Turkey

gulnuryel33@gmail.com, hmbaskonus@gmail.com, hbulut@firat.edu.tr

**Abstract**

In this study, we obtain some new travelling wave analytical solution of the coupled nonlinear Maccari's system. The purpose of this study is research new exact travelling wave solutions of the coupled nonlinear Maccari's system by apply to the Modified Trial Equation Method (MTEM). This method is very efficient and suitable for solving nonlinear differential equations and equation systems. The solutions that we find have not in the literature until recently.

**Keywords:** Modified trial equation method, Coupled nonlinear Maccari's system, Travelling wave solutions.

**REFERENCES**

1. Ahmad Neirameh, New analytical solutions for the coupled nonlinear Maccari's system, Alexandria Eng. J. Vol: 55, Issue:3,2839–2847, 2016.
2. Bouthina S. Ahmed., Anjan Biswas, Edamana Krishnan, Sachin Kumar, Solitons and other solutions to the generalized Maccari system. Romanian Reports in Physics, Vol:65, (4), 1138–1154, 2013.
3. Cheng -Shi Liu, Trial equation method and its applications to nonlinear evolution equations. Acta Physica Sinica Chinese Edition. Vol:54, Issue:6, 2505–2509,2005.
4. Cheng -Shi Liu, Trial equation method to nonlinear evolution equations with rank inhomogeneous: mathematical discussions and its applications, *Communications in Theoretical Physics*. Vol:45, Issue:2, 219–223,2013.
5. Davood Rostamy, Fatemeh Zabihi, Exact solutions for different coupled nonlinear Maccari's systems, *Nonlinear Studies*, Vol. 19, No. 2, pp. 291-301, 2012.

# ON EXPONENTIAL STABILITY OF NONLINEAR VOLTERRA INTEGRO-DIFFERENTIAL EQUATIONS WITH CONSTANT TIME-LAG

**Cemil Tunç**

Department of Mathematics, Faculty of Sciences, Yüzüncü Yıl University, Van, Turkey  
cemtunc@yahoo.com

## **Abstract**

In the present work, we pay attention to a number of nonlinear Volterra integro-differential equations (VIDEs) with constant time-lag. We define three new Lyapunov functionals (LFs) and employ them to get specific conditions guaranteeing the uniform exponential asymptotic stability (UEAS) of the trivial solutions of the (VIDEs) considered. The results obtained generalize, compliment and improve the results found in the literature from the cases of the without time-lag to the more general cases with time-lag.

**Keywords:** Non-linear, Volterra integro-differential equations, first order, time-lag, uniform exponential asymptotic stability

## **REFERENCES**

1. M. Adıvar, Y. N. Raffoul, Inequalities and exponential stability and instability in finite delay Volterra integro-differential equations. *Rend. Circ. Mat. Palermo* (2) 61 (2012), no. 3, 321–330.
2. L. C. Becker, Function bounds for solutions of Volterra equations and exponential asymptotic stability. *Nonlinear Anal.* 67 (2007), no. 2, 382–397.
3. G. S. Jordan, Asymptotic stability of a class of integro-differential systems. *J. Differential Equations* 31 (1979), no. 3, 359–365.
4. Y. Raffoul, Exponential stability and instability in finite delay nonlinear Volterra integro-differential equations. *Dyn. Contin. Discrete Impuls. Syst. Ser. A Math. Anal.* 20 (2013), no. 1, 95–106.
5. C. Tunç, A note on the qualitative behaviors of non-linear Volterra integro-differential equation. *J. Egyptian Math. Soc.* 24 (2016), no. 2, 187–192.
6. C. Tunç, On qualitative properties in Volterra integro-differential equations. *AIP Proceedings.* 1798 (1), (020164-1)- (020164-1), (2017).
7. C. Tunç, Stability and in Volterra-integro differential equations with delays. *Dynam. Systems Appl.* 26 (2017) 121-130.
8. Q. Wang, The stability of a class of functional differential equations with infinite delays. *Ann. Differential Equations*, 16 (2000), no. 1, 89–97.

## **ESTIMATION OF EARTHQUAKE PROBABILITIES WITH NON-PARAMETRIC METHODS IN SEMI- MARKOV MODEL**

Çiğdem Lazoğlu<sup>1</sup>, İsmail Gür<sup>2</sup>

<sup>1</sup>Department of Actuarial Sciences, University of Hacettepe, Ankara, Turkey

<sup>2</sup>Department of Actuarial Sciences, University of Hacettepe, Ankara, Turkey  
cigdemkoba1@hacettepe.edu.tr, cigdemkoba061@gmail.com,  
ismail.gur@hacettepe.edu.tr, igur44@gmail.com

### **Abstract**

In this study, it is assumed that the successive earthquakes can not be independent events and the magnitudes of earthquakes and the time of occurrence of earthquakes can not be independent from the time of between successive earthquakes. For this purpose, the usage of the Semi-Markov model has always been seen as appropriate. In addition, probability values are obtained by nonparametric methods. In this study, earthquakes of above 5 ML magnitude which occurred between January 1, 1950 and January 1, 2017 in and around the Marmara Region were examined. The earthquake is divided into 3 cases as low, medium and high severity according to their magnitudes. In this context, transition possibilities for semi-markov kernels, markov renewal functions, and semi-Markov processes are obtained. As a result of this study, the probability of occurrence of earthquake within the interval of the epicenter and the intensity of the earthquake is calculated at the end of any period. Rstudio, Matlab, ARCGIS programmes were used in this study.

**Keywords:** Semi markov renewal process; Embedded Markov Chain; Stability distribution; Nonparametric methods; Spatial k-means Clustering Algorithm.

### **REFERENCES**

1. Votsi, N. Limnios, G. Tsaklidis, and E. Papadimitriou, Estimation of the Expected Number of Earthquake Occurrences Based on Semi-Markov Models, *Methodol. Comput. Appl. Probab.*, vol. 14, no. 3, pp. 685–703, 2012.
2. Ouhbi B, Limnios N, The rate of occurrence of failures for semi-Markov processes and estimation, *Stat Probab Lett* 59, pp. 245-255, 2002.
3. V. Barbu, J. Bulla, and A. Maruotti, Estimation of the stationary distribution of a semi-Markov chain, *J. Reliab. Stat. Stud.*, vol. 5, pp. 15–26, 2012.
4. Altınok Y, Kolcak D, An application of the semi-Markov model for earthquake occurrences in North Anatolia, Turkey, *J Balkan Geophys. Soc*, vol. 2, pp. 90-99, 1999.

## **ON THE PROPERTIES OF SOLUTIONS TO NON-LINEAR VOLTERRA INTEGRO-DIFFERENTIAL EQUATIONS WITH MULTIPLE TIME-LAGS**

**Cemil Tunç, Osman Tunç**

Department of Mathematics, Faculty of Sciences, Yuzuncu Yıl University  
65080, Van - Turkey  
cemtunc@yahoo.com, agaosman@hotmail.com

### **Abstract**

This study is concerned with the non-linear Volterra integro-differential equation with multiple time-lags. We give some sufficient conditions so that solutions of the Volterra integro-differential equation given are absolutely Riemann integrable on  $[0, \infty)$  and have bounded derivatives by the Lyapunov-Krasovskii functional approach. The results obtained make improvements and extension of those the results can be found in literature. We give examples to verify the results obtained and for illustrations.

**Keywords:** Non-linear, Volterra integro-differential equations, first order, time-lag, stability, boundedness

### **REFERENCES**

1. L. C. Becker, Uniformly continuous  $L^1$  – solutions of Volterra equations and global asymptotic stability. *Cubo* 11 (2009), no. 3, 1–24.
2. T. A. Burton, Volterra integral and differential equations. Second edition. Mathematics in Science and Engineering, 202. Elsevier B. V., Amsterdam, 2005.
3. J. R. Graef, C. Tunç, Continuability and boundedness of multi-delay functional integro-differential equations of the second order. *Rev. R. Acad. Cienc. Exactas Fís. Nat. Ser. A Math. RACSAM* 109 (2015), no. 1, 169–173.
4. Y. Raffoul, Boundedness in nonlinear functional differential equations with applications to Volterra integrodifferential equations. *J. Integral Equations Appl.* 16 (2004), no. 4, 375–388
5. Y. Raffoul, Construction of Lyapunov functionals in functional differential equations with applications to exponential stability in Volterra integro-differential equations. *Aust. J. Math. Anal. Appl.* 4 (2007), no. 2, Art. 9, 13 pp.
6. C. Tunç, A note on the qualitative behaviors of non-linear Volterra integro-differential equation. *J. Egyptian Math. Soc.* 24 (2016), no. 2, 187–192.
7. C. Tunç, New stability and boundedness results to Volterra integro-differential equations with delay. *J. Egyptian Math. Soc.* 24 (2016), no. 2, 210–213.
8. C. Tunç, Properties of solutions to Volterra integro-differential equations with delay. *Appl. Math. Inf. Sci.* 10 (2016), no. 5, 1775–1780. 9. C. Tunç, Stability and in Volterra-integro differential equations with delays. *Dynam. Systems Appl.* 26 (2017) 121-130.
9. Bo Zhang, Necessary and sufficient conditions for stability in Volterra equations of non-convolution type. *Dynam. Systems Appl.* 14 (2005), no. 3-4, 525–549.

## **NON-UNIFORM HAAR WAVELET METHOD FOR SINGULARLY PERTURBED CONVECTION- DIFFUSION EQUATIONS**

**Mehmet Giyas Sakar, Fevzi Erdogan, Onur Saldır**

Department of Mathematics, Yuzuncu Yil University, Van, Turkey  
giyassakar@hotmail.com, ferdogan@yyu.edu.tr, onursaldir@gmail.com

### **Abstract**

In this study, we present non-uniform Haar wavelet method for solving singularly perturbed convection-diffusion equations. Some problems are solved by using the presented method. The obtained numerical results reveal that our method is reliable and very effective for solving singularly perturbed convection-diffusion problems.

**Keywords:** Haar wavelet method; convection-diffusion problems; boundary layer.

### **REFERENCES**

1. C. M. Bender, S. A. Orszag, Advanced mathematical methods for scientists and engineers: asymptotic methods and perturbation theory, Springer, New York, 1999.
2. U. Lepik, H. Hein, (2014). Haar wavelets with applications. New York, Springer.
3. Y. N. Reddy, P. P. Chakravarthy, Numerical patching method for singularly perturbed two-point boundary value problems using cubic splines, Applied Mathematics and Computation 149 (2004) 441-468.
4. M. K. Kadalbajoo, A. S. Yadaw, D. Kumar, Comparative study of singularly perturbed two-point BVPs via: Fitted-mesh finite difference method, B-spline collocation method and finite element method, Applied Mathematics and Computation 204 (2) (2008) 713-725.
5. H. S. Prasad, Y. N. Reddy, Numerical solution of singularly perturbed two-point singular boundary value problems using differential quadrature method, American Journal of Numerical Analysis 2 (6) (2014) 177-183.
6. P. Zhu, S. Xie, Higher order uniformly convergent continuous/discontinuous Galerkin methods for singularly perturbed problems of convection-diffusion type, Applied Numerical Mathematics 76 (2014) 48-59.

# LEGENDRE REPRODUCING KERNEL METHOD FOR FRACTIONAL TWO POINT BOUNDARY VALUE PROBLEM

**Onur Saldır, Mehmet Gıyas Sakar, Fevzi Erdogan**

Department of Mathematics, Yuzuncu Yil University, Van, Turkey

onursaldir@gmail.com, giyassakar@hotmail.com, ferdogan@yyu.edu.tr

## **Abstract**

In this research, we present reproducing kernel method for solving fractional two-point boundary value problem. We obtain an approximate solution by given method. Convergence analysis is constituted theoretically. Numerical experiments show that approximate solution uniformly converges to exact solution. Additionally, derivatives of approximate solution are also uniformly convergent to the derivatives of exact solution. The results indicate that the proposed method very efficient for fractional two-point boundary value problem.

**Keywords:** Reproducing kernel; Legendre polynomials; Boundary value problem.

## **REFERENCES**

1. I. Podlubny. Fractional differential equations. Academic Press, New York, 1999.
2. M. Cui, Y. Lin., Nonlinear Numerical Analysis in the Reproducing Kernel Space. Nova Science Publishers, New York, 2009.
3. M. G. Sakar, A. Akgül, D. Baleanu. On solutions of fractional Riccati differential equations. Advances in Difference Equations,39 (2017) 1-10. DOI 10. 1186/s13662-017-1091-8.
4. M. G. Sakar. Iterative reproducing kernel Hilbert space method for Riccati differential equations. J. Comput. Appl. Math. 309 (2017) 163-174.

## **SOME NOVEL EXPONENTIAL AND COMPLEX STRUCTURAL PROPERTIES OF THE FISHER EQUATION ARISING IN MATHEMATICAL BIOSCIENCE**

**Hasan Bulut<sup>1</sup>, Sibel Sehriban Atas<sup>1</sup>, Hacı Mehmet Baskonus<sup>2</sup>**

<sup>1</sup>Department of Mathematics, University of Firat, Elazig, Turkey

<sup>2</sup>Department of Computer Engineering, Munzur University, Tunceli, Turkey,  
hbulut@firat.edu.tr, suzundag90@gmail.com, hmbaskonus@gmail.com

### **Abstract**

In this study, we consider the Bernoulli sub-equation function method for obtaining new exponential and complex prototype structures to the Fisher Equation arising in Mathematical biosciences. We obtain new results by using the technique for new properties of model and for more understanding of properties of model. We plot two- and three-dimensional surfaces of the results by using Wolfram Mathematica 9. At the end of this manuscript, we submit a conclusion in the comprehensive manner.

**Keywords:** Fisher Equation, Bernoulli sub-equation function method, Exponential function solution, Rational function solution, complex structures.

### **REFERENCES**

1. A. Giese, R. Bjerkving, M. Westphal, J. Clin. Oncol, 21(8), 1624, 2003.
2. A. Farin, S.O. Suzuki, M. Weiker, J.E. Goldman, J.N. Bruce, P. Canoll, Glia 53(8), 799-808, 2006.
3. H. Hatzikirou, D. Basanta, M. Basanta, M. Simon, K. Schaller, A. Deutsch, Math, Med, Biol, 29, 49-65, 2012.
4. D. Basanta, S. JG, R. Rockne, K. Swanson, A. Alexander, Phys. Biol, 8, 015016. 2011.
5. K.R. Swanson, R.C. Rockne, J. Claridge, M.A. Chaplain, E.C. Alvord, A.R.A. Anderson, Cancer Res. 71, (24), 7366-7375, 2011.
6. E. Khain, M. Katakowski, N. Charteries, F. Jiang. M. Chopp, Phys. Rev. E, 86(1), 2012.



## NUMERICAL STUDY OF CONVECTIVE DRYING OF POROUS MATERIAL

**N. Sotehi, W. Bouaffar**

Physics Department, Faculty of Science, 20 Aout 1955-Skikda  
University, Algeria

n. sotehi@univ-skikda.dz, sotehis@gmail.com

### ABSTRACT

The numerical study of coupled heat and mass transfer in porous media is analyzed in this paper. The mathematical modeling of this phenomenon is obtained with using Philip and Devrai's model. Hence, the system describing temperature and moisture transfer processes within plate of cellular concrete is solved numerically with the finite differential method.

**Keywords:** Porous media, Drying, Transfer, Philip and Devrai's Model, differential method.

### REFERENCES

1. J. R. Philip, D. A. De Vries, Moisture movement in porous material under temperature gradients, Transaction of The American Geophysical Union, Vol. 38 (2), pp. 222- 232, 1957.
2. Z. Zhang, S. Yang, and D. Liu, Mechanism and mathematical model of heat and mass transfer during convective drying of porous materials, Heat transfer-Asian Research, vol.28 (5), pp. 337-351, 1999.
3. Mr. Nemeny, I. Czaba, A. Kvac, and T. Jani, Investigation of simultaneous heat and mass transfer within the maiz kernels during drying, Computers and Electronics Agriculture, vol. 26, pp. 123-135, 2000.
4. P. Meukam, A. Noumowe, Modeling of heat and mass transfer in lateritic building envelopes, J. Heat Mass Transfer, Vol. 42, pp. 158- 167, 2005.
5. N. Sotehi, A. Chaker, Modeling of Heat and Mass Transfers During Drying of A Building Material, phys. Chem. News, Volume 31 p. 1- 5, September 2006.
5. M. Karoglou, A. Moropoulou, M.K. Krokida, Z.B. Maroulis, A powerful simulation for moisture transfer in buildings, Building and Environment, vol. 42, pp. 902-912, 2007.
6. C.M. Tam, V.W.Y. Tam, K.M. Tg, assessing dry ingshrinkage and water permeability of reactive powder concrete produced in Honk Kong, Construction and Building Materials, vol. 26, p p. 79-89,2012.
7. N. Sotehi, A. Chaker, Numerical analysis of simultaneous heat and mass transfer in cork lightweight concretes used in building envelopes, Physics Procedia, Volume 55, p. 429 – 436 2014.

**HYBRID METHODS COUPLING STATIONARY WAVELET TRANSFORM AND  
ARTIFICIAL NEURAL NETWORKS FOR THE CLASSIFICATION OF  
HERCYNIAN GRANITOIDS BASED ON THEIR GEOCHEMICAL  
CHARACTERISTICS: CASE OF AOULI PLUTON (HIGH MOULOUYA,  
MOROCCO)**

**Abdelghani Talhaoui<sup>1</sup>, Imad Manssouri<sup>2</sup>, Abdellah El Hmaidi<sup>1</sup>**

<sup>1</sup>Team of Water Sciences and Environmental Engineering, Faculty of Sciences, Moulay  
Ismail University, B.O. 11201, Zitoune, Meknes- Morocco.

<sup>2</sup>Laboratory of Mechanics, Mechatronics and Comand, Engineering high school ENSAM,  
Moulay Ismail University, B.O. 4042, 50000, Meknes, Morocco.

talhaouiabdelghani25@gmail.com, elhmaidi@yahoo.fr, imade\_mansouri@yahoo.fr

**Abstract**

This work is part of the supervised classification of a database of 167 samples of Hercynian granitoid rocks of the Aouli pluton (Haute Moulouya, Morocco), using a hybrid method (SWT-ANN-MLP) coupling the Stationary Wavelet Transform (SWT) and the artificial neural networks Multi-Layer Perceptron (ANN-MLP). The hybrid method (SWT-ANN-MLP) is applied on a matrix of size (167,20) which corresponds to the contents of major elements, trace elements and rare earth elements, respectively 11 samples of granodiorite, 81 samples of gray granite, 70 samples of pink granite and 5 samples of granite with muscovite. First, the stationary wavelet decomposition was performed by choosing the wavelet Haar and a number of decompositions equal to 2 to represent the database. Then 60% of the database, taken randomly, was used for the formation and the choice of the architecture of the neural network MLP. Finally, unknown test samples (40% of the database) were identified by using the model (SWT-ANN-MLP) determined during the learning phase. The relative performances of this model (SWT-ANN-MLP) were evaluated by the calculation of the coefficient of determination  $R^2$  and the coefficient NSE (Nash-Sutcliffe efficiency). This study made it possible to highlight the supervised classification capacity of the hybrid method (SWT-ANN-MLP) on all the Hercynian granitoid rocks of the Aouli pluton.

**Keywords:** Supervised classification, stationary wavelet decomposition, SWT-ANN-MLP, Hercynian granitoid, Aouli Pluton High Moulouya-Morocco.

**REFERENCES**

1. Adamowski J., Sun K., Development of a coupled wavelet transform and neural network method for flow forecasting of non-perennial rivers in semi-arid watersheds, Journal of Hydrology, Vol:390, No:1, 85–91, 2010.

**USE OF A HYBRID MODEL BASED ON ARTIFICIAL NEURAL NETWORKS-RBF COUPLED TO WAVELET DECOMPOSITION FOR THE CLASSIFICATION OF OPERATING MODES: CASE OF AN INDUSTRIAL INSTALLATION**

**Bouchra Boudebbouz<sup>1</sup>, Imad Manssouri<sup>1</sup>, Ahmed Mouchtachi<sup>2</sup>**

<sup>1</sup>Laboratory of Mechanics, Mechatronics and Command, ENSAM-Meknes, Moulay Ismail University, Meknes, Morocco.

<sup>2</sup>Director of ENSAM, Hassan II University Mohammedia-Casablanca, Morocco  
bouchra.boudebbouz@gmail.com; imade\_mansouri@yahoo.fr, ahmedmouchtachi@yahoo.fr

**Abstract**

This work is placed in the context of the detection and diagnosis of the operating faults of an industrial installation. Indeed, the installation in this study is a Methylcyclohexane continuous column from a mixture of toluene / methylcyclohexane in which the mass composition was defined to 23% of methylcyclohexane. The studied system, allows the separation of the more volatile component which is methylcyclohexane contained in the liquid mixture. The present study describes classification methods based on the coupling of the Stationary Wavelet Transform SWT and the Artificial Neural Networks ANN (RBF) type for the classification of different operating modes of a distillation column of methylcyclohexane (C<sub>6</sub>H<sub>11</sub>-CH<sub>3</sub>) from a mixture of toluene-methylcyclohexane (C<sub>6</sub>H<sub>5</sub>-CH<sub>3</sub>/C<sub>6</sub>H<sub>11</sub>-CH<sub>3</sub>). The model SWT-ANN-RBF (Stationary Wavelet Transform- Artificial Neural Networks- Radial Basis Function) is constituted by the input variables which are: the heating power, the preheating power, the reflux ratio, the feeding rate, the pressure drop and the preheating temperature and the output variable which is the operating speed. Three configurations were proposed in this study and by calculating the performance parameters; only one model was chosen SWT-ANN-RBF which gave a coefficient of determination R<sup>2</sup>, A coefficient of Effectiveness NSE close to 1 and a minimum squared error MSE.

**Keywords:** Classification, Wavelet decomposition, Artificial Neural Network-RBF, Industrial facility, Nash-Sutcliffe efficiency coefficient, coefficient of determination.

**REFERENCES**

1. Liang, R. Du., Model-based Fault Detection and Diagnosis of HVAC systems using Support Vector Machine method, International Journal of Refrigeration, Vol:30, No:6, 1104–1114, 2007.
2. I. Manssouri, Y. Chetouani, and B. El Kihel, Using neural networks for fault detection in a distillation column, Int.J. Computer Applications in Technology, Vol:32, No:3, 181–186, 2008.

# THE PROTECTIVE EFFECTS OF GOLDENBERRY (*Physalisperuviana* L.) EXTRACT AGAINST TO DESTRUCTIVE EFFECTS IN OF TYPE I DIABETES IN LIVER TISSUE OF RATS

Kaya Tubay<sup>1</sup>, Erman Orhan<sup>1</sup>, Aydın Sevinç<sup>2</sup> and Yılmaz Ökkeş<sup>1</sup>.

<sup>1</sup>Firat University, Science Faculty, Biology Department, Elazığ, Turkey

<sup>2</sup>Munzur University, Food Engineering Department, Tunceli, Turkey

sevincaydin2380@gmail.com

## Abstract

Type I diabetes is known as insulin-dependent diabetes mellitus, and the most important factor playing role in its formation is the genetic predisposition. *Physalisperuviana*L. (Goldenberry) is a plant, which has strong antioxidant properties, from Solanaceae family. In this study, it has been investigated the effects of goldenberry on the malondialdehyde (MDA), reduced glutathione (GSH) and total protein which are the indicators of antioxidant defense and the oxidative damages in liver tissue of the rats, on which type I diabetes was induced by STZ. According to the obtained results, among the rats with STZ-induced type I diabetes, it was observed that the level of glutathione (GSH) ( $p < 0.05$ ) increased and the level of malondialdehyde (MDA) ( $p < 0.01$ ) decreased in rats given goldenberry extract. In this study, it was shown that the goldenberry decreased the destructive effects of type-I diabetes by decreasing the lipid peroxidation and increasing the level of glutathione. It is believed that the obtained results would be used in follow-up of diabetic patients and in early diagnosis of the disease in future.

**Keywords:** Goldenberry (*Physalisperuviana*L.), lipid peroxidation (LPO), MDA, GSH, vitamine.

## REFERENCES

1. Ramadan MF. Bioactive phytochemicals, nutritional value and functional properties of cape gooseberry (*Physalisperuviana*): An overview. Food Research International, 44, 1830–1836, 2011.

## **ON NUMERICAL SOLUTION OF FRACTIONAL ORDER BOUNDARY VALUE PROBLEM WITH SHOOTING METHOD**

**Hüseyin DEMİR<sup>1</sup>, Yücel BALTÜRK<sup>2</sup>**

<sup>1</sup>Department of Mathematics Ondokuz Mayıs University, Samsun, Turkey

<sup>2</sup>Department of Mathematics, Ondokuz Mayıs University, Samsun, Turkey  
hdemir@omu.edu.tr, yucelbalturk@gmail.com

### **Abstract**

In this study, the shooting method is used for calculation of the second order boundary value problem with fractional order. This method is found to be useful during the application and the accuracy of the shooting method which is tested and then some examples are given to illustrate the efficiency of the method with respect to different value of fractional orders.

**Keywords:** Boundary value problem, shooting method, numerical solution, fractional order boundary value problem.

### **REFERENCES**

1. Diethelm, K. , The Analysis of Fractional Differential Equations, Berlin: Springer, (2004).
2. Karagöz, I. , Sayısal Analiz Ve Mühendislik Uygulamaları, Ankara: Nobel, (2011).
3. Li, M. , Nie, N.M. ,Jiménez, S. , Tang, Y.F. , Vázquez, L., Solving Two Point Boundary Value Problems of Fractional Differential Equations.
4. Loverro, A. , Fractional Calculus: History, Definitions and Applications for the Engineer, Department of Aerospace and Mechanical Engineering University of Notre Dame, (2004).
5. Mohamed, D.A.S. and Mahmoud, R. A. An Algorithm For The Numerical Solution of System of Fractional Differential Equations, International Journal of Computer Applications, Vol:65, No:11, 27-31, 2013.
6. Podlubny, I. , Fractional Differential Equations, San Diego, California: Academic Press, (1999).

# A FAMILY OF EFFICIENT TIME STEPPING METHODS FOR SEMI-LINEAR STOCHASTIC DIFFERENTIAL EQUATIONS

Utku Erdoğan<sup>1</sup>, Gabriel J. Lord<sup>2</sup>

<sup>1</sup> Department of Mathematics, Uşak University, Uşak, Turkey

<sup>2</sup> Department of Mathematics, Heriot Watt University, Edinburgh, U.K.  
utku.erdogan@usak.edu.tr, g.j.lord@hw.ac.uk

## Abstract

In this study, we present a family of efficient time integrators for the following semi-linear Stochastic Differential Equations

$$du(Au + F(u))dt + \sum_{i=1}^m (B_i u + g_i(u))dW_i(t) \quad , \quad u(0) = u_0 \in R^d$$

where  $W_i(t)$  are iid Brownian Motions,  $F, g_i : R^d \rightarrow R^d$ ,  $i = 1, 2, \dots, m$  and matrices  $A, B_i$  satisfy the zero commutator conditions. New class of exponential integrators are derived by inspring from Geometric Brownian Motion. Strong convergence analysis of the schemes and numerical examples are also included.

**Keywords:** Stochastic Differential Equations, Exponential Integrator, Geometric Brownian Motion

## REFERENCES

1. Erdoğan, Utku, and Gabriel J. Lord. "A New Class of Exponential Integrators for Stochastic Differential Equations With Multiplicative Noise." arXiv preprint arXiv:1608.07096 (2016).
2. Hochbruck, Marlis, and Alexander Ostermann. "Exponential integrators." Acta Numerica 19 (2010): 209-286.

## UNIFORM DIFFERENCE METHOD FOR SINGULARLY PERTURBED DELAY SOBOLEV PROBLEMS

Hakkı Duru<sup>1</sup>, Akbar Barati Chiyaneh<sup>2</sup>

<sup>1</sup>Department of Mathematics, Yüzüncü Yıl University, Van, Turkey

<sup>2</sup>Department of Mathematics, Yüzüncü Yıl University, Van, Turkey  
hakkiduru@gmail.com, baratiakbar@yahoo.com,

### Abstract

In this study, the initial-boundary value problem for singularly perturbed delay Sobolev equations are treated. The exponentially fitted difference schemes on a uniform mesh which is accomplished by the method of integral identities with the use of exponential basis functions and interpolating quadrature rules with weight and remainder term in integral form are presented. The stability and convergence analysis of the method is discussed. The fully discrete scheme is shown to be convergent of order 2 in space and time, independently of the perturbation parameter. Some numerical experiments have been carried out to validate the predicted theory.

**Keywords:** Singular perturbation; Delayed partial differential equation; Sobolev problem; Uniform mesh; Difference schemes.

### REFERENCES

1. Amiraliyev, G.M., Duru, H., Amiraliyeva, I.G, A Parameter-uniform numerical method for a Sobolev problem with initial layer. Numerical Algorithms, (44): 185-203, 2007.
2. Amiraliyev, G. M., Mamedov, Y. D., Difference schemes on the uniform mesh for a singularly perturbed pseudo-parabolic equations. Turkish Journal of Mathematics, (19): 207-222, 1995.
3. Bellen, A., Zennaro, M., Numerical methods for delay differential equations, Numerical Mathematics and Scientific Computation. The Clarendon Press, Oxford University Press, New York, 2003.

## NUMERICAL INTEGRATION OF THE AIRY-TYPE EQUATIONS

Muaz Seydaoğlu<sup>1</sup>, Hüseyin Koçak<sup>2</sup> and Utku Erdoğan<sup>3</sup>

<sup>1</sup>Department of Mathematics, University of Muş Alparslan, Muş, Turkey

<sup>2</sup>Department of Quantitative Methods, Pamukkale University, Denizli, Turkey

<sup>3</sup>Department of Mathematics, University of Uşak, Uşak, Turkey

m.seydaoglu@alparslan.edu.tr, hkocak@pau.edu.tr, utku.erdogan@usak.edu.tr

### Abstract

We consider the numerical integration of the Airy-type second-order nonlinear equations. These equations can be obtained by reducing the modified Korteweg-de Vries (mKdV), Schrödinger, Boussinesq equations and the third-order dispersion equation with second-order diffusion-like nonlinearity. [1,2]. Studies on the Airy-type equations are intriguing because of the nature of the problem, which has both oscillatory slow decay and exponentially fast decay. Most of the existing numerical schemes to solve such equation cannot exhibit its correct physical behaviour. This difficulty can be overcome by using symplectic integrators [3] that are combination of splitting methods with Magnus integrators [4,5]. The obtained numerical results compared with the existing solutions in the literature, and found that they are very accurate.

**Keywords:** Splitting methods; Symplectic integrators; Non-linear Airy-type equations.

### REFERENCES

1. R. R. Rosales, The similarity solution for the Korteweg-de Vries equation the related Painlevé transcendent, Proc. R. Soc. Lond. A, 361 (1978), 265-275.
2. D. Witthaut, H. J. Korsch, Uniform semiclassical approximations of the nonlinear Schrödinger equation by a Painlevé mapping, J. Phys. A: Math.Gen, 39 (2006), 14687-14697.
3. P. Bader, S. Blanes, E. Ponsoda and M. Seydaoğlu, Symplectic integrators for the matrix Hill equation. J. Comput. Appl. Math., 316 (2017), 47-59.
4. M. Seydaoğlu and S. Blanes, High-order splitting methods for separable non-autonomous parabolic equations. Appl. Numer. Math. 84 (2014), 22-32.



## **HIGHER ORDER DIFFERENCE SCHEMES FOR SINGULARLY PERTURBED DIFFERENTIAL EQUATIONS WITH DELAY**

**Fevzi Erdogan, Mehmet Gıyas Sakar, Onur Saldır**

Department of Mathematics, Yuzuncu Yıl University, Van, Turkey  
ferdogan@yyu.edu.tr, giyassakar@hotmail.com, onursaldir@gmail.com

### **Abstract**

An initial value problem for linear second order singularly perturbed delay differential equation is considered. Its second-order derivative is multiplied by a small positive parameter  $\varepsilon$ , which induces boundary layers. Higher order difference schemes are constructed on uniform mesh, which give uniform convergence in the discrete maximum norm. The method is shown to uniformly convergent with respect to the perturbation parameter. A numerical experiment illustrate in practice the result of convergence proved theoretically.

**Keywords:** Difference Schemes; Singularly Perturbed Problem; Uniformly Convergence.

### **REFERENCES**

1. P. A. Farrell, A. F. Hegarty, J. J. H. Miller, E. O'Riordan and G.I. Shishkin, Robust Computational Techniques for Boundary Layers Chapman-Hall/CRC, New York, 2000.
2. H. G. Roos, M. Stynes and L. Tobiska, Numerical Methods for Singularly Perturbed Differential Equations, Convection-Diffusion and Flow Problems, Springer Verlag, Berlin, 1996.
3. G. M. Amiraliyev and H. Duru, A uniformly convergent finite difference method for a initial value problem, Applied Mathematics and Mechanics, 20,4 (1999) 363-370.
4. G. M. Amiraliyev and F. Erdogan, A finite difference scheme for a class singularly perturbed initial value problems for delay differential equations, Numerical Algorithms, 52(4), 2009, 663-675.

## A STUDY ON THE IMPROVED $\tan(\phi(\xi)/2)$ - EXPANSION METHOD

Berat KARAAĞAÇ<sup>1\*</sup>, N. Murat YAĞMURLU<sup>2</sup>, Alaattin ESEN<sup>2</sup>

<sup>1</sup>Department of Mathematics Education, University of Adıyaman, Adıyaman, Turkey

<sup>2</sup>Department of Mathematics, University of Inonu, Malatya, Turkey  
bkaraagac@adiyaman.edu.tr, murat.yagmurlu@inonu.edu.tr, alaattin.esen@inonu.edu.tr

### Abstract

In this study, the improved  $\tan(\phi(\xi)/2)$ -expansion method (ITEM), one of the improved expansion methods, has been applied to Jimbo-Miwa (JM) equation and the Sharma-Tasso-Olver equation using symbolic computation. With the aid of the method, many new and abundant analytical solutions have been obtained. The newly obtained results show that ITEM is a new and significant technique for solving nonlinear differential equations which plays an important role on fluids mechanics, engineering and many diverse physics fields.

**Keywords:** Improved  $\tan(\phi(\xi)/2)$ -expansion method, Jimbo-Miwa (JM) equation, Sharma-Tasso-Olver equation, Analytical solution.

### REFERENCES

1. Jalil Manafian, Optical solutions for Schrödinger type nonlinear evolution equations by the  $\tan(\phi(\xi)/2)$ -expansion method, Optik, Vol:127, No:2016, 4222-4245,2016.
2. Mehdi Fazli Aghdaei, Jalil Manafian, Optical soliton wave solutions to the resonant Davey–Stewartson system, Opt Quant Electron, vol:48, no:413, 1-33, 2016.
3. Yinghui He, Shaolin Li, Yao Long, Exact Solutions to the Sharma-Tasso-Olver Equation by Using Improved  $(G'/G)$ -Expansion Method, Journal of Applied Mathematics, vol: 2013, 1–6, 2013.

## **ANALYSIS OF OUTPUT VOLTAGE HARMONICS OF VOLTAGE SOURCE INVERTER USED PI AND PID CONTROLLERS OPTIMIZED WITH ITAE PERFORMANCE CRITERIA**

**Ozan Gül<sup>1</sup>, Nusret Tan<sup>2</sup>**

<sup>1</sup>Department of Electrical and Electronics Engineering, Bingol University, Bingol, Turkey

<sup>2</sup>Department of Electrical and Electronics Engineering, Inonu University, Malatya, Turkey  
ogul@bingol.edu.tr, nusret.tan@inonu.edu.tr

### **Abstract**

In this study, PI and PID controllers are designed using ITAE (Integral Time Absolute Error) Performance Criteria in order to obtain the controller parameters assuring improved response at selected load. The Three-level AC-DC converter including PI and PID controllers whose parameters are estimated by minimizing errors using ITAE performance criteria are modeled in MATLAB environment. The stability analysis of the control system will be presented. VSI controlled with the PI-ITAE and the PID-ITAE controller are simulated for various loads and the results are analyzed using FFT analysis for observing the total harmonic distortion (THD) of the output voltage. The comparison of the PI-ITAE and the PID-ITAE is presented by taking into consideration their low THD at the inverter output voltage under the same conditions for different types of loads. The quality of the sinusoidal waveform is more important than the quantity in AC. In order to achieve that, we need to reduce the harmonic content in the output.

**Keywords:** Voltage Source Inverter; Harmonic Analysis; ITAE Performance Criteria.

### **REFERENCES**

1. L. Guo, J. Y. Hung, and R. M. Nelms, "PID controller modifications to improve steady-state performance of digital controllers for buck and boost converters," in Proc. IEEE Appl. Power Electron. Conf., 2002, pp. 381–388.
2. D. Maiti, A. Acharya, M. Chakraborty, A. Konar and R. Janarthanan, "Tuning PID and Fractional PID Controllers using the Integral Time Absolute Error Criterion," 4th International Conference on Information and Automation for Sustainability, 2008, pp. 457-462.

## ON ASYMPTOTICALLY LACUNARY STATISTICAL EQUIVALENT OF ORDER $\alpha$ IN PROBABILITY

Mahmut Işık<sup>1</sup> and Kübra Elif Akbaş<sup>2,3</sup>

<sup>1</sup>Faculty of Education, Harran University, Osmanbey Campus, 63190 Şanlıurfa, Turkey

<sup>2</sup>Faculty of Medicine, Fırat University, 23119 Elâzığ, Turkey

<sup>3</sup>Faculty of Medicine, İnönü University, 44280, Malatya, Turkey  
misik63@yahoo.com, elifet41@gmail.com

### Abstract

In this study, we introduce and examine the concepts of asymptotically lacunary statistical equivalent of order  $\alpha$  in probability and strong asymptotically lacunary equivalent of order  $\alpha$  in probability. We give some relations connected to these concepts.

**Keywords:** Statistical convergence of order  $\alpha$  in probability, Cesaro summability of order  $\alpha$  in probability, Lacunary statistical convergence, Asymptotically statistical equivalent

### REFERENCES

1. Çolak, R. Statistical convergence of order  $\alpha$ , Modern Methods in Analysis and Its Applications, New Delhi, India: Anamaya Pub, 2010: 121-129.
2. Connor, J. S. The Statistical and strong  $p$ -Cesaro convergence of sequences, Analysis 8 (1988), 47-63.
3. Ghosal, S. and Som, S. Lacunary statistical convergence of a sequence of random variables in probability, Indian J. Math. 56 (2014), no. 3, 377--395
4. Das, P.; Ghosal, S. and Som, S. Statistical convergence of order  $\alpha$  in probability, Arab J. Math. Sci. 21(2) (2015), 253-265.
5. Ghosal, S.  $S_\lambda$ -convergence of a sequence of random variables, J. Egyptian Math. Soc. 23(1) (2015), 85—89.
6. Marouf, M. S. Asymptotic equivalence and summability, Internat. J. Math. Math. Sci. 16(4) (1993), 755--762.

## ON THE INVERSE PROBLEM FOR DIRAC SYSTEM

Keziban Taş<sup>1</sup> and Etibar S. Panakhov<sup>2</sup>

<sup>1</sup>Vocational School of Pertek Sakine Genc, University of Munzur, Tunceli, Turkey  
kezibantas@munzur.edu.tr

<sup>2</sup>Department of Applied Mathematics, Baku State University, Azerbaijan  
epenahov@hotmail.com

### Abstract

In this study, we have considered inverse problem on two spectra for Dirac operator. We have obtained the following inequality concerning the structure of the potentials difference.

$$\max|\tilde{p}(x) - p(x)| \leq C' \cdot A$$

$$\max|\tilde{q}(x) - q(x)| \leq C' \cdot A$$

where  $A = \sum_{n=1}^{\infty} \left\{ \left| \sigma_n - \rho_n - \frac{b_0' - b_0}{n^2} \right| + |\mu_n - \lambda_n - 2(a_0' - a_0)| \right\} + |\mu_0 - \lambda_0|$   
 $+ |\sigma_0 - \rho_0| + |a_0' - a_0| + |b_0' - b_0|$

**Keywords:** Dirac system, spectral parameter, potential.

### REFERENCES

1. B. M. Levitan, I. S. Sargsjan, Sturm-Liouville and Dirac Operators, Kluwer Academic Publisher, Netherlands, 1991.
2. A. Mizutani, "On the inverse Sturm-Liouville problem," Journal of the Faculty of Science, The University of Tokyo IA, vol. 31, pp. 319–350, 1984.
3. E. S. Panakhov, "The defining of Dirac system in two incompletely set collection of eigenvalues," Doklady Akademii Nauk USSR, vol. 5, pp. 8–12, 1985.
4. M. Sat, E. S. Panakhov, K. Tas; Wellposedness of the Inverse Problem for Dirac Operator, Chinese Journal of Mathematics, 2013.

## SYMMETRY SOLUTION ON FRACTIONAL EQUATION

Gulistan Iskandarova<sup>1</sup>, Dogan Kaya<sup>2</sup>

<sup>1</sup> Department of Mathematics, Istanbul Commerce University, Istanbul, Turkey  
gulistan.iskandarova@gmail.com,

<sup>2</sup> Department of Mathematics, Istanbul Commerce University, Istanbul, Turkey  
dogank@ticaret.edu.tr,

### Abstract

As we know nearly all physical, chemical, and biological processes in nature can be described or modeled by dint of a differential equation or a system of differential equations, an integral equation or an integro-differential equation. The differential equations can be ordinary or partial, linear or nonlinear. So, we concentrate our attention in problem that can be presented in terms of a differential equation with fractional derivative. The fractional derivatives are about three centuries age were presented, but not very popular amongst science and or engineering community [1-2]. Our research in this work is to use symmetry transformation method and its analysis to search exact solutions to nonlinear fractional partial differential equations. For construction a symmetry reductions of a fractional equation we investigated the symmetry properties by using the group analysis method and presented the vector fields the equation based on the point symmetry [3-4]. It is shown that our equation could be transformed into a nonlinear fractional ordinary differential equation with the new independent variable.

**Keywords:** Groups method, symmetry method, Caputo fractional derivative, Riemann-Liouville derivative.

### REFERENCES

1. Diethelm, K., The Analysis of Fractional Differential Equations, Springer, Berlin, 2010.
2. Miller, K.S., Ross, B., An Introduction to the Fractional Calculus and Fractional Differential Equations, Wiley, New York, 1993.
3. Hu, J., Ye, Y., Shen, S. Zhang, J. Lie symmetry analysis of the time fractional dV-type equation, Appl. Math. and Comp., Vol. 223, pp.439–444, 2014.
4. Sahadevan, R., Bakkyaraj, T. Invariant analysis of time fractional generalized Burgers and Kortewegde Vries equations, J. Math. Anal. Appl, Vol.393, p.341– 347, 2012.

## NEW EXACT WAVE SOLUTIONS OF SOME EVOLUTION EQUATIONS WITH FUNCTIONAL VARIABLE METHOD

**Berfin Elma, Emine Mısırlı**

Department of Mathematics, University of Ege, İzmir, Turkey

berfin-elma@hotmail.com, emine.misirli@ege.edu.tr

### **Abstract**

In this study, by using Functional Variable method we are founded some exact solutions of the Space-Time Quadratic Klein-Gordon equation and the nonlinear Coupled Klein-Gordon system. These exact solutions of equations have classified. Also the physical behaviors of the obtained solution functions are examined and graphics are drawn using the Mathematica program. The results clearly show that this method is a mathematical tool for solving some partial differential equations in various scientific and engineering fields.

**Keywords:** Functional variable method, nonlinear partial differential equations, evolution equations.

### **REFERENCES**

1. Akbari, Mojgan, "Application of the Kudryashov method and the functional variable method for the complex KdV equation." *Computational Methods for Differential Equations* 2,1 (2014): 50-55.
2. Bekir, Ahmet and Sait San, "The functional variable method to some complex nonlinear evolution equations." *Journal of Modern Mathematics Frontier* 1,3 (2012): 5-9.
3. Eslami, Mostafa, and Mohammad Mirzazadeh, "Functional variable method to study nonlinear evolution equations." *Open Engineering* 3,3 (2013): 451-458.
4. Mirzazadeh, M., and M. Eslami, "Exact solutions for nonlinear variants of Kadomtsev–Petviashvili (n, n) equation using functional variable method." *Pramana* 81,6 (2013): 911-924.
5. Zerarka, A., and S. Ouamane, "Application of the functional variable method to a class of nonlinear wave equations." *World Journal of Modelling and Simulation* 6,2 (2010): 150-160.

## **THE MODIFIED SIMPLE EQUATION METHOD FOR NEW EXACT WAVE SOLUTIONS OF SOME NONLINEAR PHYSICAL EQUATIONS**

**Gizel Bakıcıerler, Emine Mısırlı**

Department of Mathematics, University of Ege, İzmir, Turkey  
gizelbakicierler@gmail.com, emine.misirli@ege.edu.tr

### **Abstract**

In this study, we are obtained some semi-analytical solutions of the (3+1) dimensional Jimbo-Miwa equation and 1-dimensional Boussinesq equation by using improved Modified Simple Equation method. These equations are appeared in the model of many problems which seems in various fields of engineering and science such as plasma physics, optical fibers, mathematical physics, chemical physics and fluid mechanics. This method has influential and applicative for constructing of exact solutions for some evolution equations in mathematical physics. Also, graphics of solution functions have been drawn using and construe with the Mathematica program.

**Keywords:** Modified simple equation method, nonlinear partial differential equations, evolution equations.

### **REFERENCES**

1. Jawad, Anwar Ja'afar Mohamad, Marko D. Petković, and Anjan Biswas, "Modified simple equation method for nonlinear evolution equations", Applied Mathematics and Computation, 217,2 (2010): 869-877.
2. Kaplan, M., Bekir, A., Akbulut, A., Aksoy, E., "The modified simple equation method for nonlinear fractional differential equations." Romanian J. Phys., 60, 9-10 (2015): 1374-1383.
3. K. Khan and M. A. Akbar, "Traveling wave solutions of some coupled nonlinear evolution equations," ISRN Mathematical Physics, Article ID 685736, 8 pages (2013).
4. MA Khater, Mostafa, "The Modied Simple Equation Method and its Applications in Mathematical Physics and Biology", The Global Journal of Science Frontier Research 15, 4 (2015).
5. Taghizadeh, N., M. Mirzazadeh, A. Samiei Paghaleh, J. Vahidi, Exact solutions of nonlinear evolution equations by using the modified simple equation method. Ain Shams Engineering Journal, 3, 3 (2012): 321-325.



## NUMERICAL SIMULATION OF KDV EQUATION BY FINITE DIFFERENCE METHOD

Asif YOKUS<sup>1</sup> and Hasan BULUT<sup>2</sup>

<sup>1</sup>Department of Actuarial, Firat University, Elâzığ, 23119, TURKEY

<sup>2</sup>Department of Mathematics, Firat University, Elâzığ, 23119, TURKEY  
asfyokus@yahoo.com, hbulut@firat.edu.tr

### Abstract

In this study, we apply the sine-Gordon expansion method (SGEM) to the Korteweg-de Vries (KdV) equation with dual-power law nonlinearity. SGEM is a combination of the travelling wave transformation and sine-Gordon equation. We have succeeded in constructing new solitary wave solutions to the KdV equation with dual power nonlinearity. In addition to finite difference method (FDM) and operators are analyzed. Discretize equation is obtained with the help of finite difference operators. When we used new analytical solution it is considered new initial condition for The KdV equation. It is shown that the FDM is stable for the usage of the Fourier-Von Neumann technique and linear stable. Accuracy of the method is analyzed in terms of the errors in  $L_2$  and  $L_\infty$ . As well as we apply FDM for obtaining the numerical results and construct a table including numerical and exact solution and absolute measuring error. This comparison is supported with the graphics. Then, we have constructed the two and three dimensional surfaces for all analytical solutions obtained in this study by using Wolfram Mathematica 9

**Keywords:** The SGEM, the KdV equation; Finite Difference Method; Linear Stability; Numerical Solution.

### REFERENCES

1. Y. Tan, J. Yang and D.E. Pelinovsky, Semi-Stability of Embedded Solitons in the General Fifth-Order KdV Equation, *Wave Motion*, 36 (2002), 241-255.
2. Y. Brenier and D. Levy, Dissipative Behavior of Some Fully Nonlinear KdV-type Equations, *Physica D*, 147 (2000), 277-294.
3. M. Alquran, R. Al-Omary and Q. Katatbeh, New Explicit Solutions for Homogeneous Kdv Equations of Third Order by Trigonometric and Hyperbolic Function Methods, *Applications and Applied Mathematics*, 7(1) (2012), 211-225.
4. A. Yokus, Solutions of Some Nonlinear Partial Differential Equations and Comparison of Their Solutions, Ph.D. Thesis, Firat University, (2011)

## **A MODIFIED ALGORITHM GENETIC APPLIED TO POWER SYSTEM OPTIMIZATION**

**Djemai Naimi<sup>1</sup>, Ahmed Salhi<sup>1</sup>, Ahboub Dihem<sup>2</sup>**

<sup>1</sup> Department of electrical engineering, University of Mohamed Khider, Biskra, Algeria

<sup>2</sup> Department of electrical engineering, University of Batna, Algeria  
naimi.djemai@gmail.com

### **Abstract**

As genetic algorithms are stochastic methods, their main problem is the risk of losing good solutions when passing from generation to next one. In this study, a new modified genetic algorithm is proposed to remedy this problem, this modification is based on creating a register containing all the solutions of the current generation to be compared with the solutions of the following population before creating the new generation. This procedure will be repeated for each generation, in this way, we will be sure that the solutions of the last generation are the best and each solution has had its chance of comparison. This algorithm is applied to the most well known models of electrical networks such as IEEE 30, 57 14 and 118, in economic and environmental dispatchings and even multiobjective optimization. The results were very satisfactory where a clear superiority was observed after comparison with other types of genetic algorithms having the same parameters and applied to same power system networks.

**Keywords:** Genetic algorithms; Electrical networks; Economic and environmental dispatchings; Multiobjective optimization.

### **REFERENCES**

1. Sarat Kumar, A comparative study of solution of economic load dispatch problem in power systems in the environmental perspective, *Procedia computer science*, Elsevier, Vol: 48, 96-100, 2015.
2. Sudhansu Kumar Mishra, Ganapati Panda, Ritanjali Majhi, A Comparative Performance Assessment of a Set of Multiobjective Algorithms for Constrained Portfolio Assets Selection, *Swarm and Evolutionary Computing*, Elsevier., Vol: 16, pp. 38-51, 2014.

## **ANALYTICAL SOLUTIONS OF THE CONFORMABLE FRACTIONAL DIFFERENTIAL EQUATIONS**

**Meryem Odabasi**

Tire Kutsan Vocational School, Ege University, Izmir, Turkey  
meryemodabasi@gmail.com,

### **Abstract**

Fractional differential equations and their applications in physics, applied mathematics, engineering, biology and in many sciences, have a great deal of importance. Obtaining their analytical solutions allow us to understand the phenomena they describe; hence a lot of methods and different definitions of fractional derivatives have been used so far. Recently, a new definition called conformable fractional derivative have been proposed. In this study, some exact analytical solutions to the nonlinear fractional differential equations in the sense of conformable derivative are obtained using the modified trial equation method.

**Keywords:** Fractional order differential equations; Conformable fractional derivative.

### **REFERENCES**

1. A.A. Kilbas, H.M. Srivastava, J.J. Trujillo, Theory and Applications of Fractional Differential Equations, Elsevier: Amsterdam, 2006.
2. R. Khalil, M. A. Horani, A. Yousef, M. Sababheh, A New Definition of Fractional Derivative, Journal of Computational and Applied Mathematics, 264, 65–701, 2014.
3. C.S. Liu, A New Trial Equation Method and its Applications, Communications in Theoretical Physics, 45(3), 395–397, 2006.

## **CHEBYSHEV WAVELET METHOD FOR NUMERICAL SOLUTIONS OF PDEs**

Alaattin Esen<sup>1</sup>, Ömer Oruç<sup>2</sup>, Fatih Bulut<sup>3</sup>,

<sup>1</sup>Department of Mathematics, Inonu University, Malatya, Turkey

<sup>2</sup>Aralik Anatlia High School, Iğdır, Turkey

<sup>3</sup>Department of Physics, Inonu University, Malatya, Turkey

alaattin.esen@inonu.edu.tr

### **Abstract**

This study deals with the numerical solutions of one dimensional time dependent coupled Burgers' equation with suitable initial and boundary conditions by using Chebyshev wavelets in collaboration with a collocation method. The proposed method converts coupled Burgers' equations into system of algebraic equations by aid of the Chebyshev wavelets and their integrals which can be solved easily with a solver. Benchmarking of the proposed method with exact solution and other known methods already exist in the literature is made by three test problems. The feasibility of the proposed method is demonstrated by test problems and indicates that the proposed method gives accurate results in short cpu times. Computer simulations show that the proposed method is computationally cheap, fast and quite good even in the case of less number of collocation points.

**Keywords:** Chebyshev wavelet method, Chebyshev collocation, Coupled Burgers' equation, Nonlinear phenomena, Numerical solution.

### **REFERENCES**

1. Celik, I. Chebyshev Wavelet collocation method for solving generalized Burgers-Huxley equation, *Mathematical Methods in the Applied Sciences*, (2015) DOI: 10.1002/mma.3487
2. Kumar, M. and Pandit, S. A composite numerical scheme for the numerical simulation of coupled Burgers' equation, *Computer Physics Communications* 185 (3), 809-817, 2014.
3. Kelleci, A. and A. Yildirim, An efficient numerical method for solving coupled Burgers' equation by combining homotopy perturbation and pade techniques, *Numerical Methods for Partial Differential Equations*, 27 (4), 982-995, 2011.

## INVESTIGATION OF NUMBER SENSE ACHIEVEMENTS ON SECONDARY SCHOOL STUDENTS ACCORDING TO VARIOUS VARIABLES

Nejla Gürefe<sup>1</sup>, Ceren Öncül<sup>2</sup>, Hasan Es<sup>3</sup>

<sup>1</sup> Department of Mathematics Education, University of Usak, Usak, Turkey,

<sup>2</sup> Teacher, MEB, Ankara, Turkey, crnoncul@yandex.com

<sup>3</sup> Department of Mathematics Education, University of Gazi, Ankara, Turkey,  
nejlacialik@gmail.com, hasanes@gazi.edu.tr

### Abstract

In this study, it was examined achievement in subscale secondary school students' number sense and its subscales according to various variables. Number sense means that people can make logical estimates about various uses area, be able to recognize arithmetic errors and number patterns, to choose the most effective way of calculation (Hope, 1989). Number Sense Scale evaluates number sense consists of three dimensions: Flexibility in Calculation, Conceptual Thinking in Fractions, and Using Benchmark (reference points). Unrelated samples t-test, one-way Anova, two-way Anova, and Kruskal-Wallis analyzes were used to determine whether students' achievements in all dimensions and sub-dimensions differed significantly by gender and classlevels. From findings obtained from the research, there was no meaningful difference in the students' achievement in numerical sense total and sub-dimensions in terms of gender and in using benchmark (reference points) by classlevel. However, there was a meaningful difference in the total numerical sense, flexibility in calculation and conceptual thinking in fractions. It has been determined that this is in favor of 8th grade students.

**Keywords:** Number sense; Number sense dimensions; Mathematics.

### REFERENCES

1. Hope, J., Promoting number sense in school. *Arithmetic Teacher*, 12–16, 1989.

## **OPINIONS OF PROSPECTIVE MATHEMATICS TEACHERS ABOUT SOME TEACHING-LEARNING MODELS USED IN MATHEMATICS CLASSES**

Nejla Gürefe

Department of Mathematics Education, University of Uşak, Uşak, Turkey

nejlcalik@gmail.com

### **Abstract**

Classical learning system bases on memorization. This situation causes unsuccess of students (Aşkar & Olkun, 2005). It is important teacher in successful of education program. Effective teacher is a person to have ability to achieve the intended learning goals (Perrott, 1982) and must be open-minded, contemporary, self-renewing, taking into account the individual differences (Seiley, 1999). Therefore, it was seen important to determine what teachers will use teaching and learning model in mathematics lessons and in this study, the opinions of 38 prospectiveteachers from 2nd grade mathematics teacher education program were gotten about teaching strategies, methods, techniques, 5E, 7E learning models and conceptualchangetexts on the basis of constructivist learning model. From results, it was found that teaching through invention as strategy and problem solving as techniquecan be used most effectively, teaching through research-examination as strategy, expression and debate as techniques were used most weakly. However, it was determined that 5E, 7E learning models and conceptual change texts can be used effectively in mathematics lessons by the teacher candidates.

**Keywords:** Teaching-learning strategies; Constructivist learning model; Mathematics lessons.

### **REFERENCES**

- 1.Aşkar, P. ve Olkun, S., PISA 2003 Sonuçları Açısından Bilgi ve İletişim Teknolojileri Kullanımı. Eurasian Journal of Educational Research, 19, 15-34. 2005.
- 2.Perrott, E., Effective teaching: A practicalguide to improving your teaching. London and New York: Longman, 1982.
- 3.Seiley, N. The Art of Constructivist Teaching in The Primary Sschool. London: David FultonPublishers. 1999.

## BOUNDARY VALUES FOR AN EIGENVALUE PROBLEM WITH A SINGULAR POTENTIAL

Munever Tuz

Department of Mathematics, Firat University, 23119 Elazığ, Turkey

mtuz@firat.edu.tr

### Abstract

In this study we consider the inverse spectral problem

$$\psi'' + (\lambda - q(r) - \frac{l(l+1)}{r^2})\psi = 0, 0 < r < 1, \psi(1) = 0 \quad l=0,1,2,\dots$$

for the Sturm-Liouville Operator on the interval  $[0,1]$ . This determines the three-dimensional Schrödinger equation with from singular symmetric potential. It is well known that the two spectrum uniquely determine the potential function  $q(\tau)$  in a singular Sturm-Liouville equation defined. In particular we obtain a new proof of Hochstadt's theorem concerning the structure of the difference  $q(\tau) - q(\check{\tau})$ .

**Keywords:** spectrum, invers problem, eigenvalue, second-order differential equation.

### REFERENCES

1. M. Abramowitz and I. Stegun, Handbook of Mathematical Functions, Dover, New York, 1972.
2. P. B. Bailey, W. N. Everitt, A. Zettl, Computing eigenvalues of singular Sturm-Liouville problems. Results Math.20, Nos. 1--2, 391--423 [see also [www.math.niu.edu/zettl/SL2/](http://www.math.niu.edu/zettl/SL2/)].1991
3. G. Borg, Eine Umkehrung der Sturm--Liouvilleschen Eigenwertaufgabe, Acta Math. 78 1-96, 1946.
4. R. Carlson, A Borg--Levinson theorem for Bessel operators, Pacific J. Math. 177,1-26,1977.
5. E. Panakhov and R. Yılmaz, On inverse problem for singular Sturm-- Liouville operator from two spectra, Ukrainian Mathematical Journal 58(1):147-154, 2006

## ON INVERSE STURM- LIOUVILLE PROBLEMS WITH SYMMETRIC POTENTIALS

Münevver Tuz, Etibar Panakhov

Department of Mathematic, Firat University, 23119 Elazığ, Turkey  
mtuz@firat.edu.tr, epenahov@firat.edu.tr

### Abstract

In this study, we consider the inverse problem

$$-y''+q(x)y = \lambda y, \quad hy(0)-y'(0) = 0, \quad hy(\pi)-y'(\pi)=0$$

where  $q$  is integrable on  $[0,\pi]$  and satisfy the symmetry conditions  $q(x)=q(x-\pi)$  almost everywhere in the interval  $0 \leq x \leq \pi$ . We obtained the solution of the inverse Sturm Liouville problem with symmetric potential for finite interval.

**Keywords:** Inverse problem symmetric potential, fixed point theorem, second-order differential equation.

### REFERENCES

1. Levitan, B.M., Expansions in Characteristic Functions of Differential Equations of the Second Order, GITTL, Moscow, 1950.
2. Titchmarsh, E., C., Eigenfunction Expansions Associated with Second-Order Differential Equations II, Oxford, Clarendon Pres. 1958.
3. Olver, F.W.J., Introduction to Asymptotics and Special Functions, New-York and London, Academic Pres. 1974.
4. Levinson, N. The inverse Sturm-Liouville problem Math. Tidsskr. B., 25-30. 1949.
5. Mei Kobayashi, A uniqueness proof for discontinuous inverse Sturm- liouville problems with symmetric potentials, 767-781. 1989.
6. Willis, C., Inverse Sturm- liouville problems with two discontinuities. Inverse problems 2:111.130-1986.



# QUANTUM ENCRYPTION IN WIRELESS NETWORK TECHNOLOGY

Bilgehan Gurunlu<sup>1</sup>, Serkan Ozturk<sup>2</sup>

<sup>1</sup> Department of Informatics, Kahramanmaraş Sutcu Imam University, K.Maras, Turkey  
gurunlu@ksu.edu.tr,

<sup>2</sup> Department of Computer Engineering, Erciyes University, Kayseri, Turkey  
serkan@erciyes.edu.tr,

## Abstract

In this study, we propose a novel method for wireless networks utilizing quantum cryptography which is a new research field of computer science. Key distribution in a wireless network is a major security problem. It is a necessary task in wireless networks that the way of distribution the keys. Quantum key distribution, cryptographic key value within distribution systems, used for secret key known broadcast between the two nodes is a new key distribution system. BB84, which is one of quantum key distribution protocols, have effective capabilities to solve the security issues for wireless networks. In this study, BB84 based key distribution protocol is proposed for wireless networks.

**Keywords:** Wireless Network Security; Quantum Key Distribution; BB84 Quantum Key Distribution, Quantum

## REFERENCES

1. Chaochi, H., Laurent, M. Wireless and Mobile Security. Wiley Publishing. 657 p.,2007.
2. Dubendorf, Vern.A., Wireless Data Technologies, Wiley Publishing, 254p.,2003.
3. Bennett,C., Brassard,G, (1984). Quantum Cryptography: Public Key Distribution and coin tossing, In Proceedings of the IEEE International Conference on Computers, Systems and Signal Processings, Bangalore,p175, 1984.
4. Gurunlu,B. Quantum Encryption in Wireless Network Technology, Graduate Thesis, Erciyes University Graduate School of Natural and Applied Science, Turkey.,2015.
5. Gumus,E. Quantum Encryption and Key Distribution Protocols, Academic Information Conferences, Turkey.,2011.

## POISSON BRACKET ON MEASURE CHAINS

Mehmet Ali Balcı, Sibel Paşalı Atmaca, Ömer Akgüller

Department of Mathematics, Mugla Sıtkı Kocman University, Mugla, Turkey

mehmetalibalcı@mu.edu.tr, sibela@mu.edu.tr, oakguller@mu.edu.tr

### Abstract

The dual  $\mathfrak{h}^*$  of a Lie algebra  $\mathfrak{h}$  carries a Poisson bracket given by

$$\{F, G\}(\mu) = \left\langle \mu, \left[ \frac{\delta F}{\delta \mu}, \frac{\delta G}{\delta \mu} \right] \right\rangle$$

for  $\mu \in \mathfrak{h}^*$ . Lie–Poisson bracket plays an important role in the Hamiltonian description of many physical systems. This bracket is not the bracket associated with any symplectic structure on  $\mathfrak{h}^*$ , but is an example of the more general concept of a Poisson manifold. In this study, we present the generalized Poisson bracket on measure chains which are the arbitrary closed non-empty interval of the reals. The results are presented in the terms of different discrete spaces like  $h\mathbb{Z}$  and  $q^{\mathbb{N}}$ .

**Keywords:** Hamiltonian Systems, Measure Chains, Discretization

### REFERENCES

1. Stefan Hilger, Matrix Lie theory and measure chains, Journal of computational and applied mathematics, Vol: 144, No: 1, 197–217, 2002.
2. Došlý, Ondrej, Symplectic difference systems: natural dependence on a parameter. Proceedings of the International Conference on Differential Equations, Difference Equations, and Special Functions (Patras, 2012), Adv. Dyn. Syst. Appl., Vol. 8., No. 2., 2013.
3. Adamec, Ladislav, Embedding of linear Hamiltonian systems on small time scales. Dynamic Systems and Applications, Vol: 15, No. 3/4, 351, 2006

## AN INVERSE NODAL PROBLEM FOR DIFFERENTIAL PENCILS WITH COMPLEX SPECTRAL PARAMETER DEPENDENT BOUNDARY CONDITIONS

Hikmet Kemalolu<sup>1</sup>, Ünal İç<sup>2</sup> and Tuba Gulsen<sup>1</sup>

<sup>1</sup> Department of Mathematics, University of Firat, Elazig, Turkey

<sup>2</sup> Department of University of Firat, Elazig, Turkey

hkoyunbakan@gmail.com, unalic@firat.edu.tr, tubagulsen87@hotmail.com

### Abstract

In this study, we are concerned with an inverse nodal problem for second order differential pencil on a finite interval with complex spectral parameter dependent boundary conditions by using nodal points. We give some reconstruction formulas for potential functions  $p$  and  $q$  as a limit.

**Keywords:** Inverse Nodal Problem; Differential Pencil; Eigenvalues.

### REFERENCES

1. Hikmet Koyunbakan, Etibar Sadi Panakhov, A uniqueness theorem for inverse nodal problem, *Inverse Problems in Science and Engineering*, 12(6), 517-524, 2007.
2. John R. McLaughlin, Inverse spectral theory using nodal points as data-a uniqueness result, *Journal of Differential Equations*, 73, 342-362, 1988.
3. Vyacheslav Pivovarchik, Direct and inverse three-point Sturm-Liouville problems with parameter dependent boundary conditions, *Asymptotic Analysis*, 26, 219-238, 2001.
4. ChuanFu Yang, Trace Formulae for differential pencils with spectral parameter dependent boundary conditions, *Mathematical Methods in the Applications*, Doi: 10.1002/mma.2893, 2013.
5. Emrah Yilmaz and Hikmet Koyunbakan, Reconstruction of potential function and its derivatives for Sturm-Liouville problem with eigenvalues in boundary condition, *Inverse Problems in Science and Engineering*, 18(7), 935-944, 2010.

## THE STABILITY OF THE INVERSE PROBLEM WITH AN INTEGRO-DIFFERENTIAL OPERATOR

Seyfollah Mosazadeh<sup>1</sup>, Hikmet Kemalolu<sup>2</sup> and Emrah Yılmaz<sup>2</sup>

<sup>1</sup>Department of Pure Mathematics, Faculty of Mathematical Sciences, University of Kashan,  
Kashan 87317-53153, IRAN

<sup>2</sup>Department of Mathematics, Firat University, Elazig, TURKEY  
s.mosazadeh@kashanu.ac.ir, hkoyunbakan@gmail.com, emrah231983@gmail.com

### Abstract

In this study, we study following boundary value problem consisting of an integro-differential equation, together with boundary conditions dependent on the spectral parameter. We obtain the asymptotic form of the eigenvalues, and the generalization of corresponding Volterra integral operator is investigated. Then, we prove the stability theorem of the solution of the inverse problem.

$$\ell u(x) := -u''(x) + q(x)u(x) + \int_a^x K(a+x-y)u(y) dy = \lambda u(x)$$

$$u(a, \lambda) = 0, u'(b, \lambda) + \lambda \alpha u(b, \lambda) = 0,$$

where  $\lambda = \rho^2$ ,  $-\infty < a \leq x \leq b < \infty$ ,  $\alpha$  is a real parameter,  $q(x), K(x)$  are integrable real functions.

**Keywords:** Integro-differential equation; Inverse problem; Stability theorem.

### REFERENCES

1. Sergey A. Buterin, On an inverse spectral problem for a convolution integro-differential operator, Results in Mathematics, Vol:50, 173–181, 2007.
2. Gerhard Freiling and Vyacheslav A. Yurko, Inverse Sturm-Liouville problems and their applications, Nova Science Publishers Inc., New York, 2001.
3. Seyfollah Mosazadeh, The stability of the solution of an inverse spectral problem with a singularity, Bulletin of the Iranian Mathematical Society, Vol:41, 1061–1070, 2015.

## AN INVERSE PROBLEM FOR DIRAC OPERATOR AND THE STABILITY THEOREM

Seyfollah Mosazadeh<sup>1</sup>, Hikmet Kemalolu<sup>2</sup>

<sup>1</sup>Department of Pure Mathematics, Faculty of Mathematical Sciences, University of Kashan,  
Kashan 87317-53153, IRAN

<sup>2</sup>Department of Mathematics, Firat University, Elazig, TURKEY

s.mosazadeh@kashanu.ac.ir, hkoyunbakan@gmail.com

### Abstract

This study is devoted to the stability of the solution of an inverse problem for Dirac operators, which have real-valued potentials, together with separated boundary conditions on the interval  $[0, \pi]$ , as follows. First, we study the asymptotic behaviors of eigenvalues and eigen-vector-functions. Then, by Green function of the Dirac operator and using a form of Riesz basis of eigen-vector-functions and its biorthogonal associated basis, we investigate the stability theorem.

$$\ell y(x) \equiv B y'(x) - Q(x)y(x) = \lambda y(x), \quad 0 \leq x \leq \pi,$$

$$y_1(0, \lambda) \sin \alpha + y_2(0, \lambda) \cos \alpha = 0, \quad y_1(\pi, \lambda) \sin \beta + y_2(\pi, \lambda) \cos \beta = 0,$$

where

$$B = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}, \quad Q(x) = \begin{bmatrix} p(x) & 0 \\ 0 & r(x) \end{bmatrix}, \quad y = y(x) = \begin{bmatrix} y_1(x) \\ y_2(x) \end{bmatrix}.$$

Here  $\lambda$  is a spectral parameter,  $p(x), r(x)$  are real continuous functions, and  $\alpha, \beta$  are real parameters.

**Keywords:** Dirac operator; Stability; Inverse problem.

### REFERENCES

1. B. M. Levitan and I. S. Sargjan, Introduction to Spectral Theory: Selfadjoint Ordinary Differential Operators, American Mathematic Society, Rhode Island, 1975
2. S. Mosazadeh, The stability of the solution of an inverse spectral problem with a singularity, Bulletin of the Iranian Mathematical Society, Vol:41, 1061–1070, 2015.

## **VIRTUAL CONTROL AND CRACK IDENTIFICATION: 2D HEAT EQUATION**

**Anis Bel Hadj Hassin, Sinda Khalfallah**

Université de Tunis El Manar, Ecole Nationale d'Ingénieurs de Tunis, Laboratoire de  
Modélisation Mathématique et Numérique dans les Sciences de  
l'Ingénieur, B.P. 37, 1002 Tunis, Tunisia.

anis.belhadjhassin@enit.utm.tn, sinda\_khalfallah@yahoo.fr

### **Abstract**

This work deals with a specific inverse problem related to crack identification for the heat equation. In our approach, we consider an over-specified boundary condition on the boundary of the cracked domain. We give a theoretical analysis for identifiability for this inverse problem. Then, we consider a recovering process based on coupling domain decomposition method and minimizing an energy-type error functional. The efficiency of the proposed approach is illustrated by several numerical results.

**Keywords:** Inverse problem, identifiability, transient heat equation, ill-posed problem, Cauchyproblem, domain decomposition, virtual control.

### **REFERENCES**

1. A. BenAbdaand H. D. Bui, Planar crack identification for the transient heat equation, *Inv. Ill-Posed Problems*, vol. 11, no 11, 2003.
2. G. Alessandriniand A. DiazValenzuela, Planar crack identification for the transien heat equation, *SIAM J. Control Optim.*, vol. 34, no 3, 1994.
3. F. BenBelgacemand H. El Fekih, On Cauchy's problem: I. A variational Steklov Poincaré theory, *Inverse Problems*, vol. 21, no 6, 2005.
4. A. Friedmanand M. Vogelius, Determining Cracks by Boundary Measurements», *Indiana Univ. Math.*, vol. 38, no 2, 1989.
5. P. LeTallec, Y. H. De Roeckand M. Vidrascu, Domain decomposition methods for large linearly elliptic three-dimensional problems, *Journal of Computational and Applied Mathematics*, vol. 34, no 1, 1991.

## A NEW APPROACH FOR NIZHNIK-NOVIKOV- VESELOV SYSTEM

Seyma Tuluçe Demiray, Hasan Bulut

Department of Mathematics, University of Firat, Elazig, Turkey

seymatuluçe@gmail.com, hbulut@firat.edu.tr

### Abstract

In this study, we establish analytical solutions of Nizhnik-Novikov-Veselov (NNV) system. We apply modified  $\exp(-\Omega(\xi))$ -expansion function method to seek analytical solutions of NNV system. We obtain some new analytical solutions of NNV system via modified  $\exp(-\Omega(\xi))$ -expansion function method. Then, for proper parameters, we plot two and three dimensional graphics of some analytical solutions that we obtained by using this method. Numerical results together with the graphical demonstrations clearly present the reliability of this method. Also, it is observed that the proposed method is consonant with the physical structure of such equations.

**Keywords:** Nizhnik-Novikov-Veselov system; modified  $\exp(-\Omega(\xi))$ -expansion function method; analytical solutions.

### REFERENCES

1. Q. Zhao, S. K. Liu and Z. T. Fu, Exact Periodic-Wave Solutions to Nizhnik Novikov Veselov Equation, Commun. Theor. Phys., Vol:41, No:5, 719–722, 2004.
2. C. Q. Dai, G. Q. Zhou, and J. F. Zhang, Exotic Localized Structures of the (2+1)-Dimensional Nizhnik-Novikov-Veselov System Obtained via the Extended Homogeneous Balance Method, Z. Naturforsch., Vol:61a, 216–224, 2006.
3. J. Tang, F. Han, M. Zhao, W. Fu, Travelling wave solutions for the (2+1) dimensional Nizhnik-Novikov-Veselov equation, Applied Mathematics and Computation, Vol:218, 11083–11088, 2012.
4. O. Tasbozan, N. M. Yagmurlu, A. Esen, The Functional Variable Method for Some Nonlinear (2+1)-Dimensional Equations, Selçuk J. Appl. Math., Vol:14, No:1, 37–45, 2013.

## ANALYTICAL SOLUTIONS OF PHI-FOUR EQUATION

Seyma Tuluçe Demiray, Hasan Bulut

Department of Mathematics, University of Firat, Elazig, Turkey  
seymatuluçe@gmail.com, hbulut@firat.edu.tr

### Abstract

This study bases attention on new analytical solutions of Phi-four equation. The modified  $\exp(-\Omega(\xi))$ -expansion function method which is one of the analytical methods has been handled for finding analytical solutions of the Phi-four equation. By using this method, dark soliton solutions and trigonometric function solution of the Phi-four equation have been obtained. Also, by using Mathematica 9, some graphical simulations were done to see the behavior of these solutions.

**Keywords:** Phi-four equation; modified  $\exp(-\Omega(\xi))$ -expansion function method; dark soliton solutions; trigonometric function solution; Mathematica 9.

### REFERENCES

1. A.M. Wazwaz, A sine-cosine method for handling nonlinear wave equations, *Math. and Comput. Modelling*, Vol:40, 499–508, 2004.
2. Ahmet Bekir, New Exact Travelling Wave Solutions for Regularized Long-wave, Phi-Four and Drinfeld-Sokolov Equations, *International Journal of Nonlinear Science*, Vol: 6, No:1, 46–52, 2008.
3. Muhammad Younis, Asim Zafar, The modified simple equation method for solving nonlinear Phi-Four equation, *International Journal of Innovation and Applied Studies*, Vol:2, No:4, 661–664, 2013.
4. Farshad Ehsani, Farzad Ehsani, Amin Hadi, Nahid Hadi, Analytical Solution of Phi-Four Equation, *Technical Journal of Engineering and Applied Sciences*, Vol:3, No:14, 1378–1388, 2013.



## DEVELOPING M-LEARNING PROTOTYPE SYSTEM

**Saleem Al-Zoubi**

Department of computer science, University of Irbid National University, Jordan

Saleem.alzoubi@inu.edu.jo

### **Abstract**

In this study, mobile learning (m-learning) is considered as the next form of e-learning using mobile technologies to facilitate education for teachers and learners anywhere and anytime. Engaging the m-learning services in the Malaysian higher education could improve the availability of education. Students' awareness of such technology is a key for success acceptance. The main objective is to propose a students' acceptance model of m-learning in the higher education environment. The study investigates the students' acceptance of behavior intention to use m-learning and its effect on usage behavior in the higher education environment.

**Keywords:** Improved Mobile Learning Services, Mobile Learning Acceptance Model, Mobile Learning Prototype.

### **REFERENCES**

1. Allen, M. W, Designing Successful e-Learning. San Francisco: Pfeiff, John Wiley & Sons,2007.
2. Alzaza, N. S, Mobile Based Library Loan Service (MBLLS). Master thesis Master thesis, University Utara Malaysia (UUM), Sintok, Kedah, Malaysia,2007.
3. Alzaza, N. S.,& Zulkifli, A. N, Mobile Based Library Loan Service (MBLLS). Paper presented at the Rural ICT Development Conference '07 (RICTD'07), Executive Development Centre (EDC), Sintok, Malaysia,2007.

## **PREPARATION OF IMPROVED TURKISH DATASET FOR SENTIMENT ANALYSIS IN SOCIAL MEDIA**

**Semiha Makinist<sup>1</sup>, İbrahim Rıza Hallaç<sup>2</sup>, Betül Karakuş<sup>2</sup>, Galip Aydın<sup>2</sup>**

<sup>1</sup> Sentis Software, <sup>2</sup> Department of Computer Engineering, Firat University, Elazig, Turkey  
smakinist@sentis.com.tr, irhallac@firat.edu.tr, betulay@firat.edu.tr, gaydin@firat.edu.tr

### **Abstract**

A public dataset, with a variety of properties suitable for sentiment analysis [1], event prediction, trend detection and other text mining applications, is needed in order to be able to successfully perform analysis studies. The vast majority of data on social media is text-based and it is not possible to directly apply machine learning processes into these raw data, since several different processes are required to prepare the data before the implementation of the algorithms. For example, different misspellings of same word enlarge the word vector space unnecessarily, thereby it leads to reduce the success of the algorithm and increase the computational power requirement. This study presents an improved Turkish dataset with an effective spelling correction algorithm based on Hadoop [2]. The collected data is recorded on the Hadoop Distributed File System and the text based data is processed by MapReduce programming model. This method is suitable for the storage and processing of large sized text based social media data. In this study, movie reviews have been automatically recorded with Apache ManifoldCF (MCF) [3] and data clusters have been created. Various methods compared such as Levenshtein and Fuzzy String Matching have been proposed to create a public dataset from collected data. Experimental results show that the proposed algorithm, which can be used as an open source dataset in sentiment analysis studies, have been performed successfully to the detection and correction of spelling errors.

**Keywords:** Sentiment Analysis, Social Media, Hadoop, Turkish Dataset

### **REFERENCES**

1. Pang, Bo, and Lillian Lee, Opinion mining and sentiment analysis, Foundations and Trends® in Information Retrieval, 1-135, 2008.
2. White Tom, Hadoop: The definitive guide, O'Reilly Media, Inc., 2012.
3. <https://manifoldcf.apache.org/>, Aǧustos, 2015.

**NOVEL BEHAVIORS TO THE NONLINEAR EVOLUTION  
EQUATION DESCRIBING THE DYNAMICS OF IONIC  
CURRENTS ALONG MICROTUBULES** <sup>1\*</sup>Haci Mehmet Baskonus, Fevzi

Erdogan <sup>2</sup>, Arif Ozkul <sup>3</sup>, Ilham Asmouh <sup>4</sup>

<sup>1</sup>Department of Computer Engineering, Munzur University, Tunceli, Turkey

<sup>2</sup>Department of Mathematics, Yuzuncu Yil University, Van, Turkey <sup>3</sup>Department of Mathematics,  
Firat University, Elazig, Turkey <sup>4</sup>Department of Mathematics and Applications, Abdelmalek Essaadi  
University, Morocco

hmbaskonus@gmail.com, fevzier@gmail.com, arifozkul@outlook.com,  
ilham.fst@gmail.com

**Abstract**

In this work, we consider the Bernoulli sub-equation function method for obtaining novel behaviors to the nonlinear evolution equation describing the dynamics of ionic currents along Microtubules. We obtain new results by using this technique. We plot two- and three-dimensional surfaces of the results by using Wolfram Mathematica 9.

**Keywords:** Microtubules, the nonlinear evolution equation describing the dynamics of ionic currents along Microtubules, Bernoulli sub-equation function method, Exponential function solution, Rational function solution.

**REFERENCES**

1. B. Zheng, Application of A Generalized Bernoulli Sub-ODE Method for Finding Traveling Solutions of Some Nonlinear Equations, WSEAS Transactions on Mathematics, 7(11), 618-626, 2012.
2. H.M.Baskonus, H. Bulut, and M. Kayhan, Regarding Analytical Prototype Studies for the Generalized Nonlinear Pochhammer-Chree Equation, International Conference on Pure and Applied Mathematics (ICPAM 2015), Van/ Turkey, 25-28 August, 2015.
3. Nur Alama, Mahbub Alam, An analytical method for solving exact solutions of a nonlinear evolution equation describing the dynamics of ionic currents along microtubules, Journal of Taibah University for Science, <http://dx.doi.org/10.1016/j.jtusci.2016.11.004>, 10 page, 2017.

## **EMULATE ARTIFICIAL NEURAL NETWORK TO MAKE A DECISION IN WIRELESS SENSOR**

**Fouad ESSAHLAOUI, Ahmed EL ABBASSI, Rachid SKOURI**

Department of Physics, My Ismail University, Morocco.

essahlaouifouad@gmail.com

### **Abstract**

This work presents an Artificial Neural Network Implementation in Arduino Board, simulated Network with Proteus ISIS. Artificial Neurons Network (ANN) is used in the decision and control of dynamic systems which can be with a lack of superfluous information which forces the use of fuzzy logic. The network presents a feed-forward back-propagation Network. It is the best general purpose network for either supervised or unsupervised learning. The back-propagation algorithm generates a weight for all nodes in the networks, to minimize absolute error committed in fusion data. As the structure used by human being able to reason and not repeat errors. The write-up provided here gives an overview of artificial neural networks, details of the sketch, it's an introduction to some of the basic concepts employed in feed forward networks and the backpropagation algorithm. Its main applications include temperature, humidity, gas sensor and other types of data monitoring, factory automation, home automation, remote monitoring and home device control or surrounding environment to make an exact decision in shorttime.

**Keywords:** Multi-Sensor, Wireless Signal, Embedded Systems, Emulate, Arduino, NeralNetwork, Backpropagation.

### **REFERENCES**

1. M. Bouamar and M. Ladjal, "Système multicapteur utilisant les réseaux de neurones artificiels pour la surveillance des eaux potables," in 4th International Conference: Sciences of Electronic, Technologies of Information and Telecommunications, LASS, Laboratoire d'analyse des Signaux et Systèmes, Université de Msila, Algérie, 2007, pp. 25–29.
2. M. D. Abdellah, "Répartition économique de L'énergie électrique utilisant les techniques D'intelligence artificielle," Université Mentouri de Constantine, 2010. [Online]. Available: <http://bu.umc.edu.dz/theses/electrotec/DRA5240.pdf>
3. Essahlaoui Fouad, El Abbassi Ahmed, Skouri Rachid, "Implementing and Comparison between Two Algorithms to Make a Decision in a Wireless Sensors Network," vol. 7, no. 8, Aug 2016 p. 12. Available : <http://thesai.org/Publications/ViewPaper?Volume=7&Issue=8&Code=IJACSA&SerialNo=12> .

## INVERSE PROBLEM FOR STURM-LIOUVILLE OPERATOR WITH SINGULARITY

**Murat Şat**

Department of Mathematics, University of Erzincan, Erzincan, Turkey

murat\_sat24@hotmail.com

### **Abstract**

In this study, we give the solution of the inverse problem for singular differential operator. By using McLaughlin and Rundell's method, we also show that a particular set of eigenvalues is sufficient to determine the unknown potential functions.

**Keywords:** Eigenvalue; Eigenfunction; Inverse problem.

### **REFERENCES**

1. J. R. McLaughlin, William Rundell, A uniqueness theorem for an inverse Sturm-Liouville problem, *Journal of Mathematical Physics*, Vol: 28, 1471-1472, 1987.
2. Yu-Ping Wang, Murat Sat, A uniqueness theorem on the inverse problem for the Dirac operator, *Electronic Journal of Differential Equations*, Vol:2016, No:155, 1–10, 2016.
3. Yu-Ping Wang, A uniqueness theorem for indefinite Sturm-Liouville operators, *Applied Mathematics-A Journal of Chinese Universities*, Vol: 27, No:3, 345-352,2012.

## MATHEMATICAL MODELING OF CHURCH GROWTH

E. Bonyah<sup>1,2</sup>, O. K. Okosun<sup>2</sup>, M. Altaf Khan<sup>3</sup>

<sup>1</sup>Department of Mathematics and Statistics, Kumasi Technical University, Kumasi, Ghana.

<sup>2</sup>Department of Mathematics, Vaal University of Technology, Vanderbijlpark, South Africa.

<sup>3</sup>Department of Mathematics Abdul Wali Khan, University Mardan, Pakistan.

ebbonya@yahoo.com, kazeemoare@googlemail.com, altafdir@gmail.com

### Abstract

Church has been in an existence for so many years which has actually changed the lives of many people in the society. The growth of church is essential in the sustainability and spread of the church in any society. In this study, an SEIR church model is proposed. The model properties are studied with the reproduction number  $R_0$  also computed. The steady states of the church model are studied and the church free equilibrium is found to be locally and globally stable. The church endemic state is found to exist whenever  $R_0 > 1$ . Time-dependent controls are included in the church model and Pontryagin's Maximum Principle is explored to characterise the essential condition for promoting church evangelism which will lead to active church members. The numerical simulation results indicate that the combination of all the strategies in order to maximize church evangelism and have more unbelievers being converted to become active believers.

**Keywords:** church, optimal control, bifurcation, centre manifold theory, stability

### REFERENCES

1. Fair Nyabadza A deterministic model for church growth with internal revival Journal of Interdisciplinary Mathematics, 0972-0502
2. A. B. George, The Born Again Process: Conversion and Spiritual Growth in Evangelical Sects, Retrieved January 21, 2006, <http://www.mudrash.com/bornagain.html>



## ON TWO TYPES OF COUNTABLE DENSE HOMOGENEOUS SPACES

**Samer Al Ghour**

Jordan University of Science and Technology, Department of Mathematics and Statistics  
Irbid, JORDAN

### **Abstract**

We introduce the concepts of slightly dense set as well as slightly separable space, and use them to introduce two new types of slightly countable dense homogeneous spaces. Several results, relationships, examples and counter-examples concerning these concepts are obtained.

**Keywords:** Clopen sets, dense set, slight homogeneous space, countable dense homogeneous space.

### **REFERENCES**

1. W. Sierpinski, Sur un proprieté topologique des ensembles de nombrable dense en soi. Fund. Math 1 (1920), 11-28.
2. R. Bennett, Countable dense homogeneous spaces. Fund. Math. 74 (1972), 189—194.
3. A. V. Arhangel'skii and J. van Mill, On the cardinality of countable dense homogeneous spaces. Proc. Amer. Math. Soc. 141 (2013), 4031-4038.
4. R. Hernandez-Gutiérrez and M. Hrušak, Non-meager P-filters are countable dense homogeneous. Colloq. Math. 130 (2013), 281-289.
5. M. Hrusak and J. van Mill, Nearly countable dense homogeneous spaces. Canad. J. Math. 66 (2014), 743-758.
6. D. Repovš, L. Zdomskyy and S. Zhang, Countable dense homogeneous filters and the Menger covering property. Fund. Math. 224 (2014), 233-240.
7. A. R. Singal and R. C. Jain, Slightly continuous mappings. J. Indian Math. Soc. (N.S.) 64 (1997), 195-203.
8. S. Al Ghour and N. Al Khatib, On slight homogeneous and countable dense homogeneous spaces. Mat. Vesnik 63 (2011), 133-144.
9. S. Al Ghour, Minimality and prehomogeneity. Acta Math. Univ. Comenian 72 (2003), 237-244.

## **RADIATIVE MHD FLOW OF SECOND-GRADE FLUID TOWARDS A STRETCHED SPHERE**

**Anum Shafiq<sup>1</sup>, Zakia Hammouch<sup>2</sup>**

<sup>1</sup>Department of Mathematics, Preston University Islamabad Pakistan

<sup>2</sup>Department of Mathematics, Faculty of Sciences and Techniques Errachidia Morocco  
z.hammouch@fste.umi.ac.ma

### **Abstract**

This work deals with the magnetohydrodynamic (MHD) stagnation pointflow of a second-grade fluid due to a stretching sphere. Thermal radiation effects are considered in the analysis of heat transfer phenomenon. Joule heating and viscous dissipation effects are also retained. The resulting nonlinear system is computed for the series solutions. Influence of various physical parameters on the velocity and temperature profiles are scrutinized graphically. Comparison between Newtonian and second-grade fluids is made. Velocity and temperature profiles in the presence/absence of stagnation point are discussed graphically. Numerical values of skin friction and Nusselt number are also computed and interpreted.

**Keywords:** MHD stagnation, second-grade fluid, stretching sphere, Simulation.

### **REFERENCES**

1. T. Hayat, A. Shafiq, A. Alsaedi and M. Awais, MHD axisymmetric flow of third-grade fluid between stretching sheets with heat transfer. *Computers and Fluids*, 86, 103-108 (2013).
2. M. Sheikholeslami, D. D. Ganji, M. Y. Javed and R. Ellahi, Effect of thermal radiation on magnetohydrodynamics nanofluid flow and heat transfer by means of two phase model. *Journal of Magnetism and Magnetic Materials*, 374, 36.43 (2015).



# A CAPUTO-FABRIZIO FRACTIONAL-ORDER NETWORK MODEL FOR ZIKA VIRUS: NUMERICAL SIMULATIONS AND DYNAMICS

Toufik Mekkaoui<sup>1</sup>, Ebenzer Bonyah<sup>2</sup>, Zakia Hammouch<sup>1</sup>

<sup>1</sup>Department of Mathematics, Faculty of Sciences and Techniques Errachidia Morocco

<sup>2</sup> Department of Mathematics and Statistics, Kumasi Polytechnic, Kumasi, Ghana.

t.mekkaoui@fste.umi.ac.ma

## Abstract

In this work, we deal with a fractional-order Zika virus model via Caputo-Fabrizio derivative. The reproduction number  $R_0$  is computed and the steady states are investigated which shown to be locally asymptotically stable in both steady states. An efficient numerical method is used to examine the numerical solution of the Zika virus. It is shown that the numerical and the theoretical results are in good agreement.

**Keywords:** Zika virus, Caputo-Fabrizio derivative, Numerical simulation, Stability.

## REFERENCES

1. Bonyah Ebenezer. On Fractional Order Influenza A Epidemic Model. Applied and Computational Mathematics. Vol. 4, No. 2, 2015, pp. 77-82.
2. Elsaka, H., and E. Ahmed. "A fractional order network model for ZIKA." BioRxiv (2016): 039917.

## **PERCEPTIONS OF HIGH SCHOOL STUDENTS TO USE MOBILE LEARNING IN MATHEMATICS COURSE**

Yunus Çakır<sup>1</sup>, Nesrin Özsoy<sup>2</sup>

<sup>1</sup> Adnan Menderese University Social Sciences Institute,

<sup>2</sup> Adnan Menderes University Education Faculty, yunuscakir45@gmail.com,  
nesrinozsoy@yahoo.com

### **Abstract**

Today, with the innovations that technology has provided, the place of mobile devices in our lives is increasing day by day. Depending on these developments, many habits belonging to our daily lives are left to new habits. One of the most important areas where technology contributes to human life is education. The contributions that technology has made at the point of increasing the quality of education continue to increase. In particular, the facilities that mobile devices bring to this area will greatly contribute to increasing the quality of education. In this research, it was aimed to determine the perceptions of high school students regarding the use of mobile learning in mathematics lessons. However, it has been tried to show how much information students have about "Advantages and Disadvantages of Mobile Devices" and "Mobile Device Usage". Despite the fact that we work abroad in this regard, our country is limited in number. The study is important in terms of researching the relation of mobile learning with mathematics teaching and the limited number of studies at the relevant high school level. In order to learn the knowledge and perceptions of students about mobile learning, 450 students in three different high schools in İzmir provinces and districts conducted this study. "Mobile Learning Survey" developed by researchers was used as data collection tool. As a result of this research, it has been found out that when the answers of the students about the use of mobile learning in mathematics are examined, it has been found out that they have a generally positive approach. It is stated that students are aware of these advantages and disadvantages in the direction of students' responses to the items related to advantages and disadvantages of mobile learning. Finally, it has been shown that students are closely related to the use of mobile devices and that they have a great deal of knowledge about the use of these devices in response to the answers given by the students about the use cases of mobile devices.

### **REFERENCES**

1. Ağca, R. K. Ve Bağcı, H. (2013). Eğitimde Mobil Araçların Kullanımına İlişkin Öğrenci Görüşleri. Eğitim Ve Öğretim Araştırmaları Dergisi, 2, (4)
2. Akkoyunlu, B. (1995). Bilgi Teknolojilerinin Okullarda Kullanımı Ve Öğretmenlerin Rolü. Hacettepe Üniversitesi Eğitim Fakültesi Dergisi, 11, 105-109
3. Aşkar, P. Ve Altun, A. (2006). İlköğretimde Bilişim Teknolojileri. İstanbul: Morpa Kültür Yayınları

## **SOLVING A PROBLEM OF OPTIMIZING THE INITIAL CONDITION IN A HEAT EQUATION**

**S. Şule Şener, Yeşim Saraç**

Department of Mathematics, University of Atatürk, Erzurum, Turkey

senersule@atauni.edu.tr, ysarac@atauni.edu.tr

### **Abstract**

This study is related to the problem of controlling the initial condition in the linear parabolic equation. It is proved that the Frechet differential of the cost functional can be found via the solution of the adjoint parabolic problem. The necessary conditions for the existence and uniqueness of the optimal solution has been given.

**Keywords:** Parabolic Equation; Optimization; Frechet differential.

### **REFERENCES**

1. Huaiqiang Yu, Equivalence of minimal time and minimal norm control problems for semilinear heat equation, Vol:73, 17-24, 2014.
2. Michael V. Klibanov, Estimates of initial conditions of parabolic equations and inequalities via lateral Cauchy data, Inverse Problems, Vol:22, 495–514, 2006.
3. Qun Chen, Jijun Liu, Solving an inverse parabolic problem by optimization from final measurement data, Journal of Computational and Applied Mathematics, Vol:193, 183-203, 2006.
4. Vasilyev, F. P., Ekstremal problemlerin çözüm metotları, Nauka, Moskova, 1981. (Rusça)
5. Jacques Louis Lions, Optimal control of systems governed by partial differential equations, Springer-Verlag, New york, 1971.

## ON STATISTICAL CONVERGENCE OF FUZZY SEQUENCES

Abdulkadir KARAKAŞ<sup>1</sup>, Yavuz ALTIN<sup>2</sup>

<sup>3</sup>Department of Mathematics, SiirtUniversity, Siirt, Turkey

<sup>2</sup>Department of Mathematics, Firat University, Elazig, Turkey

kadirkarakas21@hotmail.com, yaltin23@yahoo.com

### Abstract

In this study, we introduce several sets of fuzzy numbers using various sequence  $\lambda$  and  $\mu$  in class  $\Lambda$ . Furthermore, some inclusion results on these sets are obtained.

**Keywords:** Statistical convergence, Fuzzy sequence.

### REFERENCES

1. H. Altinok, R. Çolak, M. Et,  $\lambda$ -difference sequence spaces of fuzzy numbers, *Fuzzy Sets and Systems*, 160 (21) (2009), 3128-3139.
2. H. Altinok, R. Çolak and Y. Altin, On the Class of  $\lambda$  – Statistically Convergent Difference Sequences of Fuzzy Numbers, *Soft Computing*, 16 (6), (2012), 1029-1034.
3. M. Et, H. Altinok, R. Çolak, On  $\lambda$  – statistical convergence of difference sequences of fuzzy numbers, *Inform. Sci.* 176 (15) (2006), 2268-2278.
4. J. A. Fridy, On statistical convergence, *Analysis* 5(4), (1985), 301-313.
5. M. Mursaleen, M.  $\lambda$  – statistical convergence, *Math. Slovaca*, 50(1), (2000), 111-115.
6. F. Nuray, E. Savaş, *Statistical convergence of fuzzy numbers*, *Math. Slovaca*, 45(3), (1995), 269-273.
7. T. Šalát, On statistically convergent sequences of real numbers, *Math. Slovaca* 30(2), 139-150 (1980).

## **STATISTICAL CONVERGENCE OF ORDER $\alpha$ IN AMENABLE SEMIGROUPS**

**Yavuz Altın, Mikail Etand Hifsi Altınok**

Department of Mathematics, Firat University, Elazığ, Turkey

yaltin23@yahoo.com, mikail68@gmail.com, hifsialtinok@gmail.com

### **Abstract**

In this study we introduce the concepts of asymptotically statistical equivalent functions of order  $\alpha$  and strong asymptotically equivalent functions of order  $\alpha$  defined on discrete countable amenable semigroups.

**Keywords:** Statistical convergence, Cesàro Summability, Amenable semigroups.

### **REFERENCES**

1. J. S. Connor, The statistical and strong  $p$ -Cesàro convergence of sequences, *Analysis* 8(1-2), 47-63 (1988).
2. R.Çolak, Statistical convergence of order  $\alpha$ , *Modern Methods in Analysis and its Applications*, New Delhi, India: Anamaya Pub, 121-129 (2010).
3. J. A. Fridy, On statistical convergence, *Analysis* 5(4), 301-313 (1985).
4. F. Nuray, B.E. Rhoades, Some kinds of convergence defined by Folner sequences, *Analysis*, 31(4), 381-390 (2011).
5. F. Nuray, B.E. Rhoades, Almost statistical convergence in amenable semigroups, *Math. Scand.* 111(1) (2012), 127--134.
6. F. Nuray, B.E. Rhoades, Asymptotically and statistically equivalent functions defined on amenable semigroups, *Thai J. Math.* 11(2) (2013), 303-311.
7. T.Šalát, On statistically convergent sequences of real numbers, *Math. Slovaca* 30(2), 139-150 (1980).

## ON DEFERRED STATISTICAL CONVERGENCE OF ORDER $\alpha$ OF SEQUENCES OF FUZZY NUMBERS

<sup>1</sup>Mikail Et, <sup>2</sup>Yüksel Erol

<sup>1</sup>Department of Mathematics, Firat University, Elazig, Turkey

<sup>2</sup>Institute of Science of Technology, Firat University, Elazig, Turkey  
mikail68@gmail.com, yukselerol87@gmail.com

### Abstract

In this study, we introduce and examine the concept of deferred statistical convergence of order  $\alpha$  of sequences of fuzzy numbers and give some relations between statistical convergence and deferred statistical convergence of order  $\alpha$  of sequences of fuzzy numbers.

**Keywords:** Fuzzy number, Deferred statistical convergence.

### REFERENCES

1. Çolak R. Statistical Convergence of Order  $\alpha$ , Modern Methods in Analysis and Its Applications, NewDelhi, India: Anamaya Pub., 2010: 121-129.
2. J. Fridy, On statistical convergence, Analysis 5 (1985), 301-313.
3. M. Et; H. Altınok and R. Çolak, On  $\lambda$ -statistical convergence of difference sequences of fuzzy numbers, Inform. Sci. 176(15) (2006), 2268-2278.
4. Küçükaslan M. and Yılmaztürk M. On deferred statistical convergence of sequences Kyungpook Math. J. 56 (2016), 357-366.

## **WEAKLY NONLINEAR ANALYSIS OF INTEGRO- DIFFERENCE EQUATIONS FOR GROWTH- DISPERSAL MODELS**

**M. Emre Kavgacı<sup>1</sup>, Hüseyin Bereketoğlu<sup>1</sup>, Özgür Aydoğmuş<sup>2</sup>**

<sup>1</sup>Department of Mathematics, University of Ankara, Ankara, Turkey

<sup>2</sup>Department of Economics, Social Sciences University of Ankara, Ankara, Turkey  
ekavgaci@ankara.edu.tr, bereket@science.ankara.edu.tr, ozgur.aydogmus@asbu.edu.tr

### **Abstract**

In this work, we study of discrete time and continuous space models with nonlocal resource competition. We consider generalization of logistic and Ricker's equations as intraspecific resource competition models with symmetric nonlocal dispersal and interaction terms. Interaction and dispersal are modeled using convolution integrals. Using linear stability analysis, equilibrium points of these models becomes unstable for some kernel functions and parameter values. To analyse the behaviour of the growth of unstable modes we should account nonlinear terms.

**Keywords:** Integro-difference equations; Nonlocal interactions; Pattern formation.

### **REFERENCES**

1. O. Aydogmus, Patterns and transitions to instability in an intraspecific competition model with nonlocal diffusion and interaction, *Mathematical Modelling of Natural Phenomena* 10, 17-29, 2015.
2. R. A. Fisher, The wave of advance of advantageous genes, *Annals of Eugenics*, 7, 355-369, 1937.
3. M. G. Neubert, M. Kot, M. A. Lewis, Dispersal and pattern formation in a discrete-time predator-prey model, *Theoretical Population Biology*, 48, 7-43, 1995.

## **EFFICIENCY ANALYSIS FOR INSURANCE COMPANY WITH DATA ENVOLEPMENT ANALYSIS**

**Müge Yeldan<sup>1</sup>, Samet Gençgönül<sup>2</sup>**

<sup>1</sup> Department of Actuarial Science, Hacettepe University, Ankara, Turkey

<sup>2</sup> Department of Actuarial Science, Hacettepe University, Ankara, Turkey  
mugeyeldan@hacettepe.edu.tr, samet.gencgonul@hacettepe.edu.tr

### **Abstract**

Data Envelopment Analysis (DEA) is a method that evaluates inputs and outputs that are measured with different units. The main feature that distinguishes Data Envelopment Analysis from other methods of similar purpose is that it can be evaluated in cases where there are many inputs and outputs. Both in the state and private sectors, DAE is widely used to measure relative efficiency. In this study, the financial performances of nonlife-insurance companies which operating in Turkey are evaluated using the data of 2015. The dataset is taken from “The Undersecretariat of Treasury”. The relative efficiencies of the companies are analyzed by means of DEA.

**Keywords:** Data Envelopment Analysis (DEA), Insurance Companies, Efficiency

### **REFERENCES**

1. Bülbül, S., Akhisar, I., (2004), Türk Sigorta Şirketlerinin Etkinliğinin Veri Zarflama Analizi ile Araştırılması, M.Ü. Bankacılık ve Sigortacılık Yüksek Okulu, İstanbul.
2. Charnes, A., Cooper W., Arie Y., Lewin ve Seifod L. M., (1994), Data Envelopment Analysis: Theory, Methodology and Applications, Kluwer Academic Publishers, Boston.
3. Sherman H. D., (1984), Data Envelopment Analysis as a new managerial audit methodology –test and evaluation. Auditing: A Journal of Practice and Theory, 4:35-53.



## ON A PARTIAL DIFFERENTIAL EQUATION WITH PIECEWISE CONSTANT MIXED ARGUMENT

**Mehtap Lafci, Hüseyin Bereketoğlu**

Department of Mathematics, Faculty of Sciences, Ankara University, Ankara, Turkey  
mlafci@ankara.edu.tr

### **Abstract**

In this work, we deal with a heat equation with piecewise constant mixed arguments. By using separation of variables method, we obtain a formal solution of this equation. Because of the piecewise constant arguments, we get a difference equation. With the help of qualitative properties of the solutions of this equation, we investigate qualitative properties of the solutions of the partial differential equation.

**Keywords:** Piecewise constant arguments, Heat equation.

### **REFERENCES**

- 1.J. Wiener. Generalized Solutions of Functional Differential Equations. World Scientific, Singapore, 1994.
2. J. Wiener and L. Debnath. A survey of partial differential equations with piecewise continuous arguments. Internat. J. Math. Math. Sci. 18(2):209-228, 1995.

## NEW JACOBI FUNCTION SOLUTIONS OF COMBINED KdV-MKdV EQUATION

Yusuf Pandir<sup>1</sup> and Yusuf Gürefe<sup>2</sup>

<sup>1</sup>Department of Mathematics, Bozok University, Yozgat, Turkey

<sup>2</sup>Department of Econometrics, Usak University, Usak, Turkey  
yusuf.pandir@bozok.edu.tr, yusuf.gurefe@usak.edu.tr

### Abstract

In this study, we obtain new Jacobi function solutions of combined KdV-mKdV equation which seems in the fluid physics and quantum field theory by using new F-expansion method. With this recommended method combined and multiple the non-degenerative Jacobi elliptic functions are presented in the solution function.

**Keywords:** New F-expansion method; combined KdV-mKdV equation; combined and multiple Jacobi elliptic function solutions.

### REFERENCES

1. M.A. Abdou, Further improved F-expansion and new exact solutions for nonlinear evolution equations, *Nonlinear Dynamics*, 52, 227-288, 2008.
2. S. Zhang, T. Xia, A generalized F-expansion method with symbolic computation exactly solving Broer–Kaup equations, *Applied Mathematics and Computation*, 189, 949-955, 2007.
3. G. Cai, Q. Wang, J. Huang, A modified F-expansion method for solving breaking soliton equation, *International Journal of Nonlinear Science*, 2, 122-128, 2006.
4. Yusuf Pandir, Hasan Huseyin Duzgun, New exact solutions of time fractional Gardner equation by using new version of F-expansion method, *Communications in Theoretical Physics*, 67(1), 9-14, 2017.
5. Yusuf Pandir, Nail Turhan, A new version of the generalized F-expansion method and its applications, *AIP Conference Proceedings*, 1798, 020122, 1-5, 2017.
6. YongHuang, YonghongWu, FanningMeng, WenjunYuan, All exact traveling wave solutions of the combined KdV-mKdV equation, *Advances in Difference Equations*, 261, 1-11, 2014.

## **FINITE ELEMENT MODELLING OF A REINFORCED CONCRETE STRUCTURE OCCURING GROUND SETTLEMENT**

**Ali Demir, Ender Başarı, Duygu Dönmez Demir**

Department of Civil Engineering, University of Manisa Celal Bayar, Turkey  
ali.demir@cbu.edu.tr

### **Abstract**

In this study, the effects on the existing neighbor structures of a new foundation construction are investigated and analyzed. Because of a new foundation construction, ground settlement in an existing reinforced concrete (R/C) structure was occurred and so various damages in basement columns and beams of the R/C structure were formed. Generally, it can be very difficult to be resolve this problem. In order to determine causes of the problem and solve the problem, numerical modelling of the structure was prepared and settlement of some column supports for simulation of real situation was provided in FE analysis. As a result of analyses, it was concluded that damages in columns and beams stemmed from ground settlement.

**Keywords:** Numerical modelling; Finite element method; Ground settlement; Reinforced concrete structure.

### **REFERENCES**

1. Dulacska, E. (1992), Soil Settlement Effects on Buildings, Elsevier Science Publishers, Amsterdam.
2. Son, M. and Cording, E. (2011), "Response of buildings with differential structural types to excavation induced ground settlement", Journal of Geotechnical and Geoenvironmental Engineering, Vol. 137 No. 4, pp. 323-333.
3. Kim, Y., Gajan, S. and Saafi, M. (2011), "Settlement rehabilitation of a 35-year old building: case study integrated with analysis and implementation", Practice and Periodical Structure Design and Construction, Vol. 16 No. 4, pp. 215-222.
4. Zhu, M., Gary, T. and Bachus, R. (2012), "Assessment of a building settlement and the litigation process-a case study", Proceedings of the 6th Congress on Forensic Engineering, San Francisco, CA, October 31-November 3.
5. Lin, L., Hanna, A., Sinha, A. and Tirca, L. (2017), High-rise buildings subjected to excessive settlement of its foundation: a case study, International Journal of Structural Integrity, Vol. 8 No. 2, pp. 210-221.

## **THE BOUNDARY CURVATURES OF GRAPH COMMUNITIES**

**Mehmet Ali Balcı, Sibel Paşalı Atmaca, Ömer Akgüller**

Department of Mathematics, Mugla Sitki Kocman University, Mugla, Turkey

mehmetalibalci@mu.edu.tr, sibela@mu.edu.tr, oakguller@mu.edu.tr

### **Abstract**

Complex systems are natural or social systems involving large number of nonlinear interacting agents. The necessity to understand the phenomena in these systems has led many investigators to use the new models and use the complex system tools used in other branches. The most interesting feature of these systems is the existence of phenomena that cannot be obtained in a simple way or that cannot be clearly predicted from the structure of the system and from the individual interaction of the actors.

In this study, we aim to present a new clustering respect to Ricci Curvature of the boundary graph emerge from the clustering of the agents. For the global clustering we use the graph communities. Then it is possible to characterize the pressure the phenomenon in the communities.

**Keywords:** Graph Communities, Boundary Graph, Data Analysis, Complex Networks

### **REFERENCES**

1. Balcı, M. A., Hierarchies in the Communities of Borsa Istanbul Stock Exchange, Hacettepe Hournal of Mathematics and Statistics, In Press
2. Balcı, M. A., Akgüller, Ö., Soft Vibrational Force on Stock Market Networks, Open Acess Library Journal, 3, 2016
3. Ahlswede, R., N. Cai, S. Y R. Li, Yeung, R. W., Network Information Flow, IEEE Transactions on Information Theory Vol. 46, Issue 4, pp. 1204-1216.

## **APPROXIMATION PROPERTIES OF DE LA- VALLEEPOUSSIN MEANS FOR SERIES BY NONLINEAR FOURIER ATOMS**

**Hatice Aslan**

Department of Mathematics, University of Firat, Elazig, Turkey

haticeaslan2017@gmail.com,

### **Abstract**

As a typical family of mono-component signals, the nonlinear Fourier atoms  $e^{ik\theta_\alpha(t)}$ ;  $k \in \mathbb{Z}$ , defined by the nontangential boundary value of the  $M$  Mobius transformation, has attracted much attention in the field of nonlinear and nonstationary signal processing in recent years. In this study, the value of the deviation of a function  $f$  from its de la Vallee-Poussin means  $V_n(f; x)$  with respect to the nonlinear trigonometric system for classes of piecewise smooth  $2\pi$ -periodic functions is estimated.

**Keywords:** Generalized Hölderspaces; nonlinear Fourier basis; de la Vallee-Poussin mean.

### **REFERENCES**

1. DeVore, R., A., Lorentz G.G., Constructive Approximation, New York: Springer-Verlag, 1993.
2. Huang, C. Yang, L. H., Approximation by the nonlinear Fourier basis, SciChina Math, 54(6), 1207-1214, 2011.
3. Leindler L. Meir A. and Totik V., On approximation of Continuous functions in Lipchitz norms, Acta Math. Hung.(45), 441-443, 1985.
4. Leindler L., Generalization of Prössdorf's Theorems, Studia Scientiarum Mathematicarum Hungarica (14), 431-439, 1979.
5. Prössdorf, S., Zur Konvergenz der Fourierreihen Hölderstetiger Funktionen, Math.Nachr.69, 1975.

**NEW SOLITON PROPERTIES TO THE OF ILL-POSED BOUSSINESQ  
EQUATION ARISING IN NONLINEAR PHYSICAL SCIENCE**

**Serbay Duran<sup>1</sup>, Muzaffer Askin<sup>2</sup>, Tukur Abdulkadir Sulaiman<sup>3</sup>**

<sup>1</sup>Faculty of Education, Adiyaman University, Adiyaman, Turkey

<sup>2</sup>Faculty of Engineering, Munzur University, Tunceli, Turkey

<sup>3</sup>Faculty of Science, Firat University, Elazig, Turkey

<sup>3</sup>Department of Mathematics, Federal University, Dutse, Jigawa, Nigeria  
sduran@adiyaman.edu.tr, muzafferaskin@gmail.com, sulaiman.tukur@fud.edu.ng

**Abstract**

In this study, with the help of the Wolfram Mathematica 9, we employ the modified exponential function method in obtaining some new soliton solutions to the ill-posed Boussinesq equation arising in nonlinear media. Results obtained with use of technique, and also, surfaces for soliton solutions are given. We also plot the 3D and 2D of each solution obtained in this study by using the same program in the Wolfram Mathematica 9.

**Keywords:** Ill-posed Boussinesq equation, Modified Exponential Function method, soliton solution.

**REFERENCES**

1. B. Gao, H. Tian, Symmetry reductions and exact solutions to the ill-posed Boussinesq equation, *International Journal of Nonlinear Mechanics*, 72, 80–83, 2015.
2. F. Özpınar, H.M. Baskonus and H. Bulut, On the Complex and Hyperbolic Structures for the (2+1)-Dimensional Boussinesq Water Equation, *Entropy*, 17(12), 8267–8277, 2015.
3. G.B. Whitham, *Linear and Nonlinear Waves*, J Wiley, New York, 1974.
4. H. Bulut, T. A. Sulaiman and H.M. Baskonus, New solitary and optical wave structures to the Korteweg–de Vries equation with dual-power law nonlinearity, *Optical and Quantum Electronics*, 48, 12(564), 1-14, 2016.
5. H.M. Baskonus, T. A. Sulaiman and H. Bulut, On the Novel Wave Behaviors to the Coupled Nonlinear Maccari's System with Complex Structure, *Optik- International Journal for Light and Electron Optics*, 131, 1036–1043, 2017.
6. H. Bulut, T. A. Sulaiman, H.M. Baskonus, Anna A. Sandulyak, New Solitary and Optical Wave Structures to the (1+1)-Dimensional Combined KdV-mKdV Equation, *Optik: International Journal for Light and Electron Optics*, 135, 327-336, 2017.

## KEROSENE OIL BASED SQUEEZING FLOW OF CARBON NANOTUBE BETWEEN TWO RIGA DISKS

Anum Shafiq<sup>a</sup>, Faiza Naseem<sup>b</sup>, Lifeng Zhao<sup>b</sup> and Anum Naseem<sup>b</sup>

<sup>a</sup>Department of Mathematics, Preston University 45320 Islamabad 44000, Pakistan

<sup>b</sup>School of Mathematical Sciences, University of Science and Technology of China, Hefei,  
Anhui 230026, China

### Abstract:

In this study, squeezing flow of carbon nanotubes between two parallel riga disk is investigated through homotopy analysis method. Carbon nanotubes (single-wall and multi-wall) are used as nanoparticles which are homogeneously distributed in the base fluid (kerosene oil). A set of non-linear differential equations for the governing flow is attained by employing suitable transformations through the conservative laws. Behavior of different emerging parameters on the velocity and temperature distributions are sketched graphically and discussed comprehensively. Analysis of skin fraction coefficient and Nusselt number are also elaborated numerically. It is observed that velocity is smaller for squeezing parameter in the case of multi-wall carbon nanotubes when compared with single-wall carbon nanotubes.

**Keywords:** Squeezing flow; carbon nanotubes; Riga disks.

## THE QUADRATICITY OF LINEAR COMBINATIONS OF A QUADRATIC AND A CUBIC MATRIX THAT COMMUTE

**Burak Tufan Gökmen, Tuğba Petik, Halim Özdemir**

Department of Mathematics, University of Sakarya, Sakarya, Turkey  
tg.tufangokmen@gmail.com, tpetik@sakarya.edu.tr, hozdemir@sakarya.edu.tr,

### Abstract

Let  $A_1$  and  $A_2$  be an  $\{\alpha_1, \beta_1, \gamma_1\}$ -cubic matrix and an  $\{\alpha_2, \beta_2\}$ -quadratic matrix, respectively, with  $\alpha_1 \neq \beta_1$ ,  $\alpha_1 \neq \gamma_1$ ,  $\beta_1 \neq \gamma_1$ , and  $\alpha_2 \neq \beta_2$ . The aim of this work is to characterize all situations where the linear combination  $A_3 = a_1 A_1 + a_2 A_2$  with  $A_1 A_2 = A_2 A_1$  is a quadratic matrix. The results obtained cover many of the results in the literature related to idempotency or involutivity of the linear combinations of an idempotent (or involutive) and a tripotent matrix.

**Keywords:** Quadratic matrix, cubic matrix, linear combination, diagonalization.

### REFERENCES

- 1 Baksalary, J.K., Baksalary, O.M., and Styan, G.P.H., Idempotency of linear combinations of an idempotent matrix and a tripotent matrix, *Linear Algebra Appl.*, 354, 21-34, 2002.
- 2 Özdemir, H. and Özban, A.Y., On idempotency of linear combinations of idempotent matrices, *Appl. Math. Comput.*, 159, 439-448, 2004.
- 3 Özdemir, H., Sarduvan, M., Özban, A.Y., and Güler, N., On idempotency and tripotency of linear combinations of two commuting tripotent matrices, *Appl. Math. Comput.*, 207, 197-201, 2009.
- 4 Petik, T., Uç, M., and Özdemir, H., Generalized quadraticity of linear combination of two generalized quadratic matrices, *Linear and Multilinear Algebra*, 63, 12, 2430-2439, 2015.
- 5 Sarduvan, M. and Özdemir, H., On linear combinations of two tripotent, idempotent, and involutive matrices, *Appl. Math. Comput.*, 200, 401-406, 2008.
- 6 Uç, M., Özdemir, H., and Özban, A.Y., On The Quadraticity of Linear Combinations of Quadratic Matrices, *Linear and Multilinear Algebra*, 63, 1125-1137, 2015.
- 7 Uç, M., Petik, T., Özdemir, H., The generalized quadraticity of linear combinations of two commuting quadratic matrices, *Linear and Multilinear Algebra*, 64, 9, 1696-1715, 2016



## SYNCHRONIZATION OF IDENTICAL AND NON-IDENTICAL CHAOTIC DYNAMICAL SYSTEMS

S. Ali-Tahir<sup>1</sup>, A. Bouhamidi<sup>2</sup> M. Sari<sup>1</sup>

<sup>1</sup>Department of Mathematics, Yildiz Technical University, Istanbul, Turkey

<sup>2</sup>LMPA, University of Littoral, Calais, France

tahirshko@gmail.com,

### Abstract

In this study, we present a generalized framework for a synchronization of a coupled chaotic identical and non-identical dynamical systems. We consider two approaches for constructing chaotic unidirectionally synchronized between two identical or non-identical dynamical systems for different dimensions. The first one, is based on the classical Lyapunov stability theory and the second one required the non-linear part of response system to be enough smooth and uses the expansion of such a function. To show the effectiveness and feasibility of those approaches, various numerical simulations are presented.

**Keywords:** Dynamical systems, synchronization, chaotic system, stabilization, Lyapunov theory, numerical analysis.

### REFERENCES

1. L. Kocarev, U. Parlitz, Generalized synchronization predictability and equivalence of unidirectionally coupled dynamical systems, Phys revlett, 76, 1816-9, 1996.
2. S. Kuntanapreda, Chaos synchronization of unified chaotic systems via LMI, Phys. Lett., A 373, 2837-2840, 2009
3. L. M. Pecora and T. L. Carroll, Synchronization in chaotic systems, Physical Review Letters, 64, 821-824, 1990.
4. H-O. Peitgen, H. Jürgens and D. Saupe, Chaos and Fractals, Springer-Verlag, 1992.
5. YG. Yu and SC. Zhang, The synchronization of linearly bidirectional coupled chaotic systems. Chaos Solitons and Fractals, 22, 189-97, 2004.

## NEW FUNCTION METHOD TO THE (N+1)- DIMENSIONAL NONLINEAR PROBLEMS

**Tolga Akturk<sup>1</sup>, Yusuf Gurefe<sup>2</sup>, Hasan Bulut<sup>3</sup>**

<sup>1</sup> Department of Mathematics and Science Education, Ordu University, Ordu, Turkey

<sup>2</sup> Department of Econometrics, Usak University, Usak, Turkey

<sup>3</sup> Department of Mathematics, Firat University, Elazig, Turkey  
tolgaakturk@gmail.com, ygurefe@gmail.com, hbulut@firat.edu.tr

### Abstract

In this study, we apply the new function method based on the trigonometric, hyperbolic functions and their basic transformations. Thus, we construct the wave solutions including the Jacobi elliptic functions. Also, some properties of the derived doubly periodic solutions are shown graphically. It can be seen that this method is forceful mathematical tool for the (N+1)-dimensional nonlinear physical problems.

**Keywords:** New function method; Wave solution; Jacobi elliptic function.

### REFERENCES

1. Jonu Lee, Rathinasamy Sakthivel, Travelling wave solutions for (N+1)-dimensional nonlinear evolution equations, Pramana-Journal of Physics, Vol:75, No:4, 565–578, 2010.
2. Deng Shan Wang, Zhenya Yan, Hongbo Li, Some special types of solutions of a class of the (N+1)-dimensional nonlinear wave equation, Computers and Mathematics with Applications, Vol:56, No:6, 1569–1579, 2008.
3. Hasan Bulut, Tolga Akturk, Yusuf Gurefe, Traveling wave solutions of the (N+1)-dimensional sin-cosine-Gordon equation, AIP Conference Proceedings, Vol:1637, No:1, 145–149, 2014.
4. Hasan Bulut, Tolga Akturk, Yusuf Gurefe, An application of the new function method to the generalized double sinh-Gordon equation, AIP Conference Proceedings, Vol:1648, No:370014, 4 pages, 2015.

## **EDX ANALYSIS, MICROSTRUCTURE AND TRANSPORT PROPERTIES OF MgO DOPED Bi2212 SUPERCONDUCTORS**

**N. Boussouf<sup>2,3</sup>, C. Benhamideche<sup>1,5</sup>, H. Sahraoui<sup>2</sup>, M. F. Mosbah<sup>3,4</sup>**

<sup>1</sup> Department Of chemistry, Faculty of Sciences, 20<sup>th</sup> August 1955 University, B.P.26 route d' El-Hadaiek, 21000 Skikda. Algeria.

<sup>2</sup> University Centre of Mila Abdalhafid Boussouf, Algeria, Institute of Science and Technology. Department of Technical Science.

<sup>3</sup> Material Science and Applications Research Unit, Physics Department, Constantine 1 University, Route d'Ain-el-Bey 25017 Constantine, Algeria.

<sup>4</sup> National Polytechnic School of Constantine, Ville Universitaire, Nouvelle Ville Ali Mendjeli, Algeria

<sup>5</sup> Chemistry of the Environmental and Structural Molecular Research Unit, Constantine 1 University, Algeria. boussoufnora@yahoo.fr, chahrazedb2002@yahoo.fr, h.sahraoui2003@yahoo, faycalmos@yahoo.fr

### **Abstract**

Superconducting ceramics of  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{Mg}_x\text{O}_{8+\delta}$  ( $x = 0, 0.01, 0.02, 0.03, 0.04, 0.05$ ) are synthesized by simple solid-state reaction route. The influences of Mg doping on microstructures properties and superconducting behavior has been investigated by X-ray diffraction (XRD), Scanning Electron Microscopy (SEM) equipped with energy-dispersive, The DC resistivity versus temperature. X-ray diffraction experiments and SEM observations revealed the degree of texture in the superconductor. The analysis of the X-ray diffraction results reveals that all the samples are composed of only Bi2212 and Bi2201 phases. SEM photographs show that the addition of MgO affects the mechanism of the grains growth due to the change of thermodynamic properties. All the samples appear to have a multiphase character as shown by DC resistivity and XRD data. Mg was found to be effective in the formation of the high- $T_c$  phase at 5% of doping in this system. The onset temperature  $T_c$  (onset) of all the samples remains within the temperature range 80–82 K.

**Keywords:** Bi-based high- $T_c$  superconductors; Scanning electron microscopy; X-ray diffraction.

### **REFERENCES**

1. N. Darma, R. Rawat, V. Ganesan, B. Das. J. Supercond. Novel Magn. DOI: 10.1007/s10948-011-1210-9, 2011.
2. H. Maeda, Y. Tanaka, M. Fukutomi, and T.A. Asano, Jpn. J. Appl. Phys. Vol. **27**, N° 2, pp.209-210, 1988.
3. Kaya, B. Özçelik, B. Özkurt, A. Sotelo, M. A. Madre, Mater Electron. 24(5), Page 1580, 2013.
4. P. Nurmalita. Proceedings of the 2<sup>nd</sup> Annual International Conference Syiah Kuala University, 2012.
5. M. A. Suazlina, S. Y. S. Yusainee, H. Azhan, R. Abd-Shukor, R. M. Mustaqim. Jurnal Teknologi, 69(2), 49-52. DOI: 10.11113/jt. v69.3106, 2014.

## **STUDY OF THE TRIBOLOGICAL BEHAVIOR OF A SLIDING CONTACT BRASS-STEEL COUPLE**

**Choubeila Boubechou<sup>1</sup>, Ali Bouchoucha<sup>2</sup>, Hamid Zaidi<sup>3</sup>**

<sup>1</sup> Faculté de Technologie, Département de Génie Mécanique, Université de 20 Août 1955, Skikda 21000, Algérie.

<sup>2</sup> Laboratoire de Mécanique, Faculté des Sciences de la Technologie, Département de Mécanique Engineering, Université Des Frères Mentouri Constantine, 25000, Algérie.

<sup>3</sup> Laboratoire LMS (UMR-6610-CNRS), SP2MI, Téléport 2, Boulevard Marie et Pierre Curie, Université of Poitiers, BP 30179, 86962 Futuroscope Chasseneuil Cedex, France  
choubeila\_boubechou@yahoo.fr

### **Abstract**

The aim of this study is to consider the tribological behavior of a dynamic contact steel-brass couple with electric current. This study looks at a dry contact brass-steel couple where friction and wear are studied in terms of mechanical and electrical parameters. For this reason, a tribometer, pin-rotary disc is used in an atmospheric atmosphere. The test parameters are as follows: The normal load (5-30N) and the sliding speed (0.1 to 0.5 m / s). The duration of each test is 30 minutes. The experimental results show that these parameters have a significant effect on the tribological behavior of the couple studied. The discussion of results is based on observations, using an optical microscope, MEB and a profilometer, worn surfaces and interface phenomena resulting from the process of sliding contact.

**Keywords:** Brass-steel couple, Dry friction, Morphology, Normal load, Sliding speeds, Wear.

### **REFERENCES**

1. Choubeila Boubechou, Ali Bouchoucha, Hamid Zaidi, Youcef Mouadji, Thermal and tribological analysis of the dry sliding steelsteel couple traversed by an electrical current, Physics Procedia 55 ( 2014 ) 165 – 172.

## **MEASUREMENT UNCERTAINTY ON A GEOMETRICAL SPECIFICATION IN THREE-DIMENSIONAL MEASUREMENT**

**Gheribi Hassina<sup>1</sup>, Boukebbab Salim<sup>2</sup>**

<sup>1</sup>Département de génie mécanique Faculté de Technologie Université de 20 Aout 55 Skikda,  
Algeria, gheribi\_hassina@yahoo.fr

<sup>2</sup>University of Mentouri Constantine, Laboratory of Engineering Transport and Environment,  
Algeria, boukebbab@yahoo.fr

### **Abstract**

The measurement of the parts on a Coordinate Measuring Machine (CMM), is carried out by an operation of palpation, when the feeler comes into contact with the part, the actual contact between the probe and the measured surface is unknown, it is substituted by a estimated or measured contact point. The point is calculated from the taken point coordinates (center of the probe), the approach direction and the radius of the probe. This creates a doubt about the actual position of the point being felt. This doubt is spreading even on the parameters of the associated surface, as well as the geometric construction for the technical verification specifications. In this case, the automation of the calculation of uncertainties of measurement makes it possible to the metrologist to make decisions to declare the conformity of the products. In this context, this article presents an example of a control of a geometrical condition of a part manufactured. To be able to carry out this checking a data-processing model was produced, it made it possible to determine the whole of the parameters characterizing surfaces to be measured, and to calculate uncertainty associated with these parameters, as well as the geometrical defect, which is also attached to an uncertainty.

**Keywords:** CMM; Association and optimisation; Geometrics specifications; Uncertainty.

### **REFERENCES**

1. Arencibia R V, Souza C, Henara L, Antonio F, Simplified model to estimate uncertainty in CMM. J Braz. Soc. Mech. Sci. Eng, 37(1), 2014.
2. Gestel NV, Determining measurement uncertainties of feature measurements on CMMs, these of Doctorate, Katholieke Universiteit Leuven – Faculteit Ingenieur wetensc happen Kaste el park Arenberg 1 - bus 2200, B-3001 Heverlee, 2011.



## **A PACKAGED SOFTWARE FOR SOLUTION OF THE PROBLEM OF OPTIMAL PLACEMENT AND INTEGRATION OF OIL AND GAS PLATFORMS**

**Elnur Nuri, Elvin Nasibov**

Ege University, Faculty of Science, Department of Mathematics, İzmir, Turkey  
nurielnur@gmail.com, elvin.nasibov755@gmail.com

### **Abstract:**

The number of the wells to be drilled in order to reach to oil and gas reserves with a sloping route are determined by geology experts. First of all platforms need to be constructed for drilling, and after that communication and transportation lines must be boned which needs sizeable amount of money. Therefore, modelling problems that contains optimal execution of all these process, developing efficient algorithms to solve these problems and designing software systems for these algorithms have great importance.

In this study, the problem of the placament and integration of oil and gas platforms for directional drilling is discussed. In order to solve the problem an approximate solution algorithm which is based on the mathematical model and solution method that is proposed by the first author is suggested. In the proposed algorithm, the K-Means algorithm for clustering problems is used for deciding optimal placement of platforms and Kruskal algorithm which is known for solving Minimum Spanning Tree problem is used for integrating platforms and a new software system in C# programming language is designed. Taking into consideration that some fuzzy parameters are used in the mathematical models, developing a new fuzzy mathematical model, preparing solution algorithms which is based on the model and preparing interactive software systems that use visual programming techniques has been planned. If some parameters (maximumvalue of drillingangle, drillingcosts) are given as fuzzy number, performance of the program will be higher, flexibility and suitability to the real life circumstances will increase. Thus, decision-maker can make more realist judgments.

**Keywords:** Oil and gas platforms, optimal placement and integration of platforms, directional drilling in offshore fields, Mathematical modelling, C# programming language, Clustering, Spanning Tree, K-Means Algorithm, Kruskal Algorithm.

### **REFERENCES**

- [1] Nuri E., Nuriyeva F., Nasiboğlu E., 2016, A Fuzzy Model of the Problem of Optimal Placement and Integration of Offshore Oil and Gas Platforms. *Journal of Modern Technology and Engineering*, 1(1), 30-38.
- [2] Pacheco M.A.C., Vellasco, M. M. B. R. 2009. *Intelligent Systems in Oil Field Development under Uncertainty*, Studies in Computational Intelligence, Ed. Springer Berlin/Heidelberg, 288p.

# ON MOMENTS GENERATING FUNCTIONS OF SAMPLE EXTREMES OF ORDER STATISTICS FROM DISCRETE UNIFORM DISTRIBUTION

Ayşe T. Bugatekin and Sinan Çalık

<sup>1</sup> Department of Statistics, University of Firat, Elazığ, Turkey  
aturan@firat.edu.tr, scalik@firat.edu.tr

## Abstract

In this study, the moment generating functions of sample extremes of order statistics from discrete uniform distribution are given. Finally, the results of these moment generating functions of order statistics of random variable for the independent and identically discrete uniform distribution are obtained.

**Keywords:** Order Statistics; Moment Generating Functions; Distribution Functions.

## REFERENCES

1. Ahsanullah, M., and Nevzorov, V. B., Ordered Random Variables, *Nova Science Publishers, Inc.*, New York, 2001.
2. Çalık, S. and Güngör, M., On the Expected Values of the Sample Maximum of Order Statistics from a Discrete Uniform Distribution. *Applied Mathematics and Computation*, 157, 695-700, 2004.
3. David, H. A., Order Statistics. Second Edition, *John Wiley and Sons, Inc.* Newyork, 1981.
4. Khatri, C. G., Distribution of Order Statistics for Discrete Case. *Ann. Inst. Statist. Math.*, 14, 167-171, 1962
5. Nagaraja, H. N., Order Statistics from Discrete Distribution (with discussion). *Statistics*, 23, 189-216, 1992.

# USEFUL INEQUALITIES FOR UPPER AND LOWER BOUNDS OF REPAIRABLE AGING COLD STANDBY SYSTEM

Gökhan Gökdere

<sup>1</sup>Department of Statistics, University of Firat, Elazig, Turkey

g.g.gokdere@gmail.com

## Abstract

In many engineering systems, cold standby redundancy is an effective way to achieve high system reliability while preserving limited power resources. Cold standby redundancy technique uses one or more redundant components that are unpowered, do not consume any energy and do not fail until being activated to replace a faulty online component. Whenever working component fails, then an available cold standby component, i.e. inactive standby component, is immediately powered up to take over the mission task. Some recent works on the research of the cold standby systems are in Wu and Wu (2011), Levitin et al. (2013), Eryilmaz (2014), Gökdere and Gürcan (2016). In this paper, we study a cold standby repairable system consisting of two non-identical components and a single repair facility with one repairman. It is assumed that, one of the two components is operating while the other is in cold standby and also two components follow a geometric process. Under these assumptions, at first we present Laplace-Stieltjes transform of the system lifetime and then we give some useful inequalities about the mean lifetime of the system.

**Keywords:** Laplace-Stieltjes transform of system, Aging cold standby system, System lifetime, Geometric process.

## REFERENCES

1. Q. Wu and S. Wu. Reliability analysis of two-unit cold standby repairable systems under Poisson shocks, *Applied Mathematics and Computation*, 218, 171-182, 2011.
2. G. Levitin, L. Xing and Y. Dai. Cold-standby sequencing optimization considering mission cost, *Reliability Engineering and System Safety*, 118, 28-34, 2013
3. S. Eryilmaz. A study on reliability of coherent systems equipped with a cold standby component, *Metrika*, 77: 349-359, 2014.
4. G. Gökdere and M. Gürcan, Laplace-Stieltjes Transform of the System Mean Lifetime via Geometric Process Model, *Open Mathematics*, 14, 384-392, 2016.



# SEQUENCES WITH RANDOM INDICE IN CLASSICAL BANACH SPACE

Mehmet Gürcan, Sinan Çalık, Yunus Güral

<sup>1</sup>Department of Statistics, University of Firat, Elazig, Turkey

mehmetgurcan2000@yahoo.com; scalik@firat.edu.tr; ygural@firat.edu.tr

## Abstract

In this study we define sequences with random indice in classical Banach space and analyzing it's some properties. After then we define differences sequence space on sequences with random indice. The difference operation is based on indice, and the generated difference sequence has a free stepwise. And here an important definition is the embedding space. Consequently we showed that  $l_\infty$  is a embedding space to  $c$ .

**Keywords:** Sequence Space, Embedding Space, Random Variable.

## REFERENCES

1. H. Kizmaz, On certain sequence space, Canad. Math. Bull, 24(2), 169-76, 1981.
2. M. Et and C.A. Bektaş, Generalized strongly  $(V, \lambda)$  summable sequences defined by Orlicz function, Mathematica Slovaca, 54(4), 411-422, 2004.
3. H. Altınok, M. Et and Y. Altın, Strongly almost summable difference sequences, Vietnam J. of Math. 34(3), 331-339, 2006.
4. B. Chandra Tripathy, M. Et and Y. Altın, Generalized difference sequence spaces by Orlicz function in a locally concex space, J. of An. And Ap. 1(3), 175-192, 2003.
5. B. Chandra Tripathy, Generalized difference paranormed statistically convergent sequences defined by Orlicz function in locally convex space, Soochow J. of Math. 30(4), 431-446, 2004.

## AN INTEGRAL FORMULA ON THE LORENTZIAN MANIFOLD

**Mehmet Bektaş**

Department of Mathematics, University of Firat, Elazig, Turkey

mehmetbektas@firat.edu.tr

### **Abstract**

Integral formulas have always been an important tool for studying various analytical and geometric problems on Riemannian manifolds. In Riemannian geometry, integral formulas have been studied by many mathematicians and proven to be a quite useful tool in differential geometry. Perhaps the Reilly's formula is one of the most well known integral formula in Riemannian geometry as well as a very powerful tool for obtaining global results. Nonetheless, a Reilly's Formula in Lorentzian geometry has not been available. On the other hand Reilly formula is actually an integral Bochner formula for gradient vector fields on manifolds with boundary in references.

In this note, The Reilly's integral formula well known for Riemann manifolds is obtained and introduced a application about it in n-dimensional Lorentzian space. Also We established a Reilly type formula in spacelike boundry hypersurfaces.

**Keywords:** Reilly's Formula, Lorentzian space

### **REFERENCES**

1. M. Bektaş and Ergüt, M, The Reilly's Integral Formula on with Nondegenerate Space-like Boundary Lorentzian Manifolds, F.Ü Fen ve Müh.Bilimleri Dergisi Vol:10, No:2, 89–97, 1998.
2. N.S., Al-Medhadi, and Marzouk, M.D., An Integral Formula and, Applied Mathematics and Computation, Vol:84, 137–144, 1992.
3. M. Ergüt and Külahcı, M., 2013, The Reilly's Integral Formula on Semi-Riemannian Manifolds with Nondegenerate Boundary, Bol. Soc. Paran. Mat Sun, Vol:31, No:1, 125– 144, 2013.
4. D. Martin, Manifolds Theory, Ellis Horwood Lmt., West Sussex, PO191EB, England,1991.

## ON SOME SPECTRAL PROBLEMS FOR DIFFUSION OPERATOR

Mine Babaoglu<sup>1</sup> and Etibar S. Panakhov<sup>2</sup>

<sup>1</sup>Faculty of Education, University of Kahramanmaras Sutcu Imam, Kahramanmaras, Turkey

<sup>2</sup>Institute of Applied Mathematics, University of Baku State, Baku, Azerbaijan

mnbabaoglu@gmail.com<sup>1</sup>, epenahov@hotmail.com<sup>2</sup>

### Abstract

In this study, we attain several spectral results for Diffusion operator. In particular, the solution functions belong to Paley-Wiener space:

$$PW_{\pi} = \left\{ f \text{ entire, } |f(\mu)| \leq Ce^{\pi|\text{Im}\mu|}, \int_{\mathbb{R}} |f(\mu)|^2 d\mu < \infty \right\}.$$

so that required theorems are proved.

**Keywords:** Diffusion operator; Paley-Wiener space; Sampling theory.

### REFERENCES

1. B. M. Levitan, I. S. Sargsjan, Introduction to Spectral Theory: Selfadjoint Ordinary Differential Operators, American Mathematical Society, Providence, Rhode Island, 1975.
2. M. G. Gasymov, G. Sh. Guseinov, Determination of diffusion operator on spectral data, Dokl. Akad. Nauk Azerb. SSSR, 37, 2, 19–23, 1981.
3. H. Koyunbakan, E. S. Panakhov, Half inverse problem for diffusion operators on the finite interval, J. Math. Anal. Appl., 326, 1024–1030, 2007.
4. B. Chanane, Computing eigenvalues of regular Sturm-Liouville problems, Appl. Math. Lett., 12, 119–125, 1999.
5. A. Boumenir, B. Chanane, Computing eigenvalues of Sturm-Liouville systems of Bessel type, Proc. Edinburgh Math. Soc., 42, 257–265, 1999.

## MULTIPLICATIVE LIE TRIPLE HIGHER DERIVATION ON UNITAL ALGEBRA

Aisha Jabeen

Department of Mathematics, Aligarh Muslim University, Aligarh, 202002, India  
ajabeen329@gmail.com

### Abstract

Let  $R$  be a commutative ring with identity and  $A$  be a unital algebra over  $R$ : Let  $N$  be the set of all non negative integers and  $L = \{L_i\}_{i \in N}$  be a family of maps  $L_i : A \rightarrow A$  such that  $L_0 = L_A$ ; the identity map on  $A$ . Then  $L$  is said to be a multiplicative Lie triple higher derivation on  $A$  if  $L_i([x, y], z) = \sum_{r+s+t=i} [[L_r(x), L_s(y)], L_t(z)]$  for all  $x, y, z \in A$  and for each  $i \in N$ . In this article we show that under certain assumptions every multiplicative Lie triple higher derivation  $L = \{L_i\}_{i \in N}$  on  $A$  is of standard form, i.e., each component  $L_i$  has the form  $L_i = \delta_i + \gamma_i$ ; where  $\{\delta_i\}_{i \in N}$  is an additive higher derivation on  $A$  and  $\{\gamma_i\}_{i \in N}$  is a sequence of mapping  $\gamma_i : A \rightarrow Z(A)$  vanishing at Lie triple products in  $A$ :

## **LIE ALGEBRA REPRESENTATIONS AND 1- PARAMETER 2D-HERMITE POLYNOMIALS**

**Mahvish Ali<sup>1</sup>**

<sup>1</sup>Department of Mathematics, Aligarh Muslim University, Aligarh, India

mahvishali37@gmail.com

### **Abstract**

The representations of the Lie algebras generate in a natural way all known classical special polynomials. This allows one to greatly simplify the theory of orthogonal polynomials by expressing them in terms of the corresponding Lie algebra or Lie group. In this article, the problem of framing the 1-parameter 2D-Hermite polynomials (1P2DHP)  $Z_{m,n}^{(\beta)}(z_1, z_2)$  (which are 2D orthogonal polynomials), into the context of the irreducible representations  $\uparrow_{\omega, \mu}$  and  $\downarrow_{\omega, \mu}$  of the four-dimensional Lie algebra  $\mathcal{G}(0,1)$  is considered. This approach stress the mathematical relevance of 2D-orthogonal polynomials and Lie algebras. Certain relations involving the 1P2DHP  $Z_{m,n}^{(\beta)}(z_1, z_2)$  are obtained using the approach adopted by Miller. The linear differential operators serve as useful tools towards obtaining these relations. The analysis has been carried out by generalizing the formalism relevant to 1P2DHP  $Z_{m,n}^{(\beta)}(z_1, z_2)$ . Certain examples involving 2D-Hermite polynomials  $H_{m,n}(z_1, z_2)$  and Laguerre polynomials  $L_n^{(\alpha)}(z)$  are obtained as special cases.

**Keywords:** 2D-Hermite polynomials; Lie group; Lie algebra; representation theory; implicit formulae.

# **POSTER PRESENTATIONS**

**POSTER PRESENTATIONS WILL BE IMPLEMENTED  
BETWEEN 21.05.2017 AND 22.05.2017 AT 14.30-18.00**



**THE ANTIOXIDANT EFFECTS OF GOLDENBERRY  
(*PHYSALISPERUVIANA* L.) EXTRACT AGAINST TO THE OXIDATIVE  
EFFECTS OF TYPE I DIABETES IN MUSCLE TISSUE OF RATS**

**Kaya Tubay<sup>1</sup>, Erman Orhan<sup>1</sup>, Aydın Sevinç<sup>2</sup> and Yılmaz Ökkeş<sup>1</sup>**

<sup>1</sup>Firat University, Science Faculty, Biology Department, Elâzığ, Turkey

<sup>2</sup>Munzur University, Food Engineering Department, Tunceli, Turkey

sevincaydin2380@gmail.com

**Abstract**

Type I diabetes is known as insulin-dependent diabetes mellitus, and the most important factor playing role in its formation is the genetic predisposition. *Physalis peruviana* L. (Goldenberry) is a plant, which has strong antioxidant properties, from Solanaceae family and, because of its fructose content, plays regulatory role in blood glucose level of diabetics. In this study, it has been investigated the effects of goldenberry on the malondialdehyde (MDA), reduced glutathione (GSH), total protein which are the indicators of antioxidant defense and the oxidative damages in muscle tissues of the rats. According to the obtained results, among the rats with STZ-induced type I diabetes, it was observed that the level of glutathione (GSH) increased and the level of malondialdehyde (MDA) decreased in rats given goldenberry extract. In this study, it was shown that the goldenberry decreased the destructive effects of type-I diabetes by decreasing the serum glucose and lipid peroxidation and increasing the level of glutathione.

**Keywords:** Goldenberry (*Physalis peruviana* L.), lipid peroxidation (LPO), MDA, GSH, Muscle.

**REFERENCES**

1. Ramadan MF. Bioactive phytochemicals, nutritional value and functional properties of cape gooseberry (*Physalis peruviana*): An overview. Food Research International, 44, 1830–1836, 2011.
2. Horn RC, Soares JC, Mori NC, Gelatti GT, Manfio CE, Golle DP, Koefender J, Deuschle RA and Oliveira C. Antioxidant Effect of *Physalis peruviana* Fruit Aqueous Extract – The Antioxidant Effect of *Physalis*. Journal of Agricultural Science, 7, 137-143, 2015.
3. Hassan AI and Ghoneim MAMA. Possible Inhibitory Effect of *Physalis* (*Physalis pubescens* L.) On Diabetes in Male Rats. World Applied Sciences Journal, 21(5), 681-688, 2013.
4. Mora AC, Aragon DM. and Ospina LF. Effects of *Physalis peruviana* Fruit Extract on Stress Oxidative Parameters in Streptozotocin-Diabetic Rats. Latin American Journal of Pharmacy, 29(7), 1132-6, 2010.

## THE CHARACTERIZATIONS OF NULL QUATERNIONIC CURVE IN $R_1^4$

**Ebru Koçak, Mehmet Bektaş**

Department of Mathematics, University of Firat, Elazig, Turkey  
mbektas@firat.edu.tr

### **Abstract**

It is well known that there exist spacelike quaternionic curve and timelike quaternionic curve in the Minkowski space. However, null quaternionic curves have many properties which are very different from spacelike quaternionic curve and timelike quaternionic curve. In this paper, we introduce the geometric properties of null quaternionic curves in Minkowski space which given by [1]. Later we obtained the conditions for null quaternionic curves to lie on some subspaces of  $R_1^4$  and we give some characterizations and theorems for these curves.

**Keywords:** Minkowski space; Kundu-Eckhaus; null quaternionic curves.

### **REFERENCES.**

1. A. Tuna Aksoy, Pseudo-Spherical Null Quaternionic Curves in Minkowski Space  $R_1^4$ , Acta Physica Polonica A, vol:130, 259-261, 2016.
2. A. Tuna Aksoy and A.C. Coken, Serret-Frenet Formulae for Null Quaternionic Curves in Semi Euclidean 4-Space  $R_1^4$ , Acta Physica Polonica A, B-, vol:128, 293-296, 2015.
3. K.L. Duggal, D.H. Jin, Null Curves and Hypersurfaces of Semi-Riemannian Manifolds, World Scientific Publishing, p. 83, 2007.
4. Bharathi, K. and Nagaraj, M., Geometry Of Quaternionic And Pseudo Quaternionic Multiplications, Ind. J. Pure. App. Math., vol:16, no:7, 741-756, 1985.
5. B.O. Neill, Semi-Riemannian geometry with applications to relativity, Academic Press, New York, 1983.
6. A.C. Coken, and U. Ciftci, On the Cartan Curvatures of a Null Curve in Minkowski Spacetime, Geometriae Dedicata, vol:114, 71-78, 2005.



## A NOTE ON SIACCI'S THEOREM

Mehmet BEKTAŞ, Münevver YILDIRIM YILMAZ

Department of Mathematics, University of Firat, Elazig, Turkey

mbektas@firat.edu.tr, myildirim@firat.edu.tr

### Abstract

In this study, using new kinematical decomposition of the acceleration vector related to the osculating plane, we give a new proof and examples for a space curves. We also give some special examples and plot figures related to the subject.

**Keywords:** Space curve, Frenet formulae, kinematics, acceleration vector.

### REFERENCES

1. J Casey, Siacci. Sresolution of the acceleration vector for a space curve, *Meccanica*, 46: 471-476, 2011.
2. J Casey, Areal velocity and angular momentum for non-planar problems in particle mechanics. *Am J. Phys* 75:677-685, 2007.
3. A A Ergin, The one parameter Lorentzian Motion, *Commun. Fac. Sci. Univ. Ank. Series A*, V.40, 59-66, 1991.
4. A. Yücesan, A C Çöken, A.C., N Ayyildiz, On the Darboux Rotation Axis of Lorentz Space curve, *Applied Mathematics and Computation*, 155(2), 345-351, 2004.
5. K Nomizu, Kinematics and Differential Geometry of Submanifolds, *Tohoku Math. Journal*, 30 (1978) 623-637.
6. O. Neill, Semi Riemannian geometry with application to Relativity, New York Academic Press, (1983).
7. T. Ikawa, On curves and Submanifolds in an Indefinite-Riemannian manifold, *Tsukuba J. Math.* Vol.9 No.2, (1985), 353-371.

## A NEW APPROACH FOR SMARANDACHE CURVES IN THE THE NULL CONE $Q^3$

Mihriban K ulahci<sup>1</sup>, Fatma Almaz<sup>2</sup>, Mehmet Bektaş<sup>3</sup>

<sup>1</sup>Department of Mathematics, University of Firat, Elazig, Turkey  
mihribankulahci@gmail.com, fb\_fat\_almaz@hotmail.com, mbektas@firat.edu.tr

### Abstract

Smarandache geometry is a geometry which has at least one Smarandachely denied axiom, [2]. An axiom is said to be Smarandachely denied, if it behaves in at least two different ways within the same space. Smarandache curve is defined as a regular curve whose position vector is composed by Frenet frame vectors of another regular curve. In this study, we define special Smarandache curves such as  $x\alpha, x\beta, xy, \alpha y, \alpha\beta, \beta y$ -Smarandache curves according to asymptotic orthonormal frame in the null cone  $Q^3$  and we investigate the curvature and the asymptotic orthonormal frame's vectors of Smarandache curves. We give theorems related to these Smarandache curves.

**Keywords:** Smarandache curve, Asymptotic orthonormal frame, Cone frame formulas.

### REFERENCES

1. A. T. Ali, Special Smarandache Curves in the Euclidean Space, International Journal of Math. Comb., 2: 30-36, 2010.
2. C. Ashbacher, Smarandache Geometries, Smarandache Notions Journal, 8(1-3), 212-215, 1997.
3. N. Bayrak, O. Bayrak, S. Yuce, Special Smarandache Curves in  $IR_1^3$ , Commun. Fac. Sci. Univ. Ank. Ser. A1 Math. Stat., 65(2), 143-160, 2016.
4. O. Bektaş, S. Yuce, Special Smarandache Curves According to Darboux frame in  $E^3$ , Romanian J. Math. and Computer Science, 3(1), 143-160, 2013.
5. M. Cetin, H. Kocayigit, On the Quaternionic Smarandache Curves in Euclidean Space 3-Space, Int. J. Contemp. Math. Sciences, 8(3), 139-150, 2013.
6. M. Kulahci, M. Bektaş, M. Ergut, Curves of AW(k)-type in 3-dimensional null cone, Physics Letters A, Vol.371, 275-277, 2007.
7. M. Kulahci, F. Almaz, Some characterizations of osculating curves in the lightlike cone, Bol. Soc. Paran. Math., 35(2), 39-48, 2017.

## NEW GENERALIZATIONS OF SOME MULTIPLE HYPERGEOMETRIC FUNCTIONS

M. BakiYağbasan<sup>1</sup>, Recep Şahin<sup>2</sup>, İ. Onur Kıymaz<sup>1</sup>, Ayşegül Çetinkaya<sup>1</sup>, Oğuz Yağcı<sup>2</sup>

<sup>1</sup>Department of Mathematics, University of Ahi Evran, Kırşehir, Turkey

<sup>2</sup>Department of Mathematics, University of Kırıkkale, Kırıkkale, Turkey

mbyagbasan@ahievran.edu.tr

### Abstract

In this work, by using a new generalization of extended beta function we introduced new generalizations of some multiple hypergeometric functions. We also obtained their integral representations, transformation formulas and Mellin transforms.

**Keywords:** Beta function; Multiple hypergeometric functions; Integral representations; Mellin transform.

**Acknowledgement:** This work was supported by Ahi Evran University Scientific Research Projects Coordination Unit. Project Number: FEF.E2.17.028

### REFERENCES

1. Agarwal P., Junesang C., Shilpi J., Extended hypergeometric functions of two and three variables, Commun. Korean Math. Soc., 30, No. 4, 403-414, 2015.
2. Bailey W.N., Generalized Hypergeometric Series, Cambridge Tracts in Mathematics and Mathematical Physics, vol. 32, Cambridge University Press, Cambridge, 1935.
3. Chaudhry M. A., Qadir A., Rafique M., Zubair S. M., Extension of Euler's beta function, J. Comput. Appl. Math., 78, 19-32, 1997.
4. Chaudhry M. A., Qadir A., Srivastava H. M., Paris R. B., Extended hypergeometric and confluent hypergeometric functions, Appl. Math. Comput, 159 (2), 589-602, 2004.
5. Erdélyi A., Magnus M., Oberhettinger F., Tricomi F.G., Higher Transcendental Functions, vol. I, McGraw-Hill Book Company, New York, 1953.
6. Srivastava H. M., Karlsson P. W., Multiple Gaussian Hypergeometric Series, Ellis Horwood Limited, 1985.

## ON A SPECIAL CLOPENNESS

Ayşe Arslan<sup>1</sup>, Erdal Ekici<sup>2</sup>

<sup>1</sup> CanakkaleOnsekiz Mart University, Graduate School of Natural and Applied Sciences,  
Department of Mathematics, TerzioğluCampus, Canakkale, TURKEY

<sup>2</sup> Corresponding Author: Department of Mathematics, CanakkaleOnsekiz Mart University,  
TerzioğluCampus, 17020, Canakkale, TURKEY

eekici@comu.edu.tr (prof.dr.erdalekici@gmail.com)

### Abstract

In 2007, Ekici introduced the concept of  $C^*$ -sets in topological spaces [5]. The relationships between  $C^*$ -sets and special spaces were introduced by Ekici in 2007. In 2009, Ekici and Noiri introduced the concepts of BC-sets and AC-sets [3]. The aim of this study is to study a special clopen set in topological spaces.

**Keywords:** Special set, Clopen set, Topology.

This work is a part of Ayşe Arslan's Master of Science Thesis.

### REFERENCES

1. M. Caldas, E. Ekici, S. Jafari and R. M. Latif, On weakly BR-open functions and their characterizations in topological spaces, *Demonstratio Mathematica*, 44(1), 159-168, 2011.
2. E. Ekici, On  $A_I^*$ -sets,  $C_I$ -sets,  $C_I^*$ -sets and decompositions of continuity in ideal topological spaces, *Analele Stiintifice Ale Universitatii Al. I. Cuza Din Iasi (S. N.) Matematica*, 59(1), 173-184, 2013.
3. E. Ekici and T. Noiri, Decompositions of continuity,  $\alpha$ -continuity and AB-continuity, *Chaos, Solitons and Fractals*, 41, 2055-2061, 2009.
4. E. Ekici, Generalization of weakly clopen and strongly  $\theta$ -b-continuous functions, *Chaos, Solitons and Fractals*, 38, 79-88, 2008.
5. E. Ekici, On  $C^*$ -sets and decompositions of continuous and  $\eta\zeta$ -continuous functions, *Acta Mathematica Hungarica*, 117 (4), 325-333, 2007.
6. E. Ekici, On  $\gamma$ -normal spaces, *Bull. Math. Soc. Sci. Math. Roumanie*, 50(98) No. 3, 259-272, 2007.
7. E. Ekici and J. H. Park, On weakly s-precontinuous multifunctions, *Arabian Journal for Science and Engineering*, Volume 32, Number 1A, 83-92, 2007.
8. E. Ekici and T. Noiri, On a generalization of normal, almost normal and mildly normal spaces II, *Filomat*, 20: 2, 67-80, 2006.
9. E. Ekici, Almost nearly continuous multifunctions, *Acta Mathematica Universitatis Comenianae*, Vol. LXXIII, 2, pp. 175-186, 2004.
10. A. S. Mashhour, M. E. Abd El-Monsef and S. N. El-Deep, On precontinuous and weak precontinuous mappings, *Proc. Math. Phys. Soc. Egypt*, 53, 47-53, 1982.
11. M. H. Stone, Applications of the theory of Boolean rings to general topology, *Trans. Amer. Math. Soc.*, 41, 375-381, 1937.

## ON APPLICATIONS OF A GENERALIZED MAP

Elif Karataş<sup>1</sup>, Erdal Ekici<sup>2</sup>

<sup>1</sup> CanakkaleOnsekiz Mart University, Graduate School of Natural and Applied Sciences,  
Department of Mathematics, TerzioğluCampus, Canakkale, TURKEY

<sup>2</sup> Corresponding Author: Department of Mathematics, CanakkaleOnsekiz Mart University,  
TerzioğluCampus, 17020, Canakkale, TURKEY

eekici@comu.edu.tr (prof.dr.erdalekici@gmail.com)

### Abstract

Generalized notions are generalizations of the subjects in topology and near areas, for example analysis etc. There are many papers on these investigations and properties. Generalized sets, topologies, structures, maps etc. The goal of this work is to study a generalized map. Main properties on this generalized map are investigated.

**Keywords:** Generalized set, Generalized map, Topological space.

**Acknowledgement:** This work was supported by Çanakkale Onsekiz Mart University The Scientific Research Coordination Unit, Project number: FYL-2016-811.

This work is a part of Elif Karataş's Master of Science Thesis.

### REFERENCES

1. C. W. Baker and E. Ekici, A note on almost contra-precontinuous functions, International Journal of Mathematics and Mathematical Sciences, Volume 2006, Article ID 96032, 1-8.
2. E. Ekici, On weak structures due to Császár, Acta Mathematica Hungarica, 134 (4), 565-570, 2012.
3. E. Ekici, Generalized submaximal spaces, Acta Mathematica Hungarica, 134 (1-2), 132-138, 2012.
4. E. Ekici and B. Roy, New generalized topologies on generalized topological spaces due to Császár, Acta Mathematica Hungarica, 132 (1-2), 117-124, 2011.
5. E. Ekici, On  $e^*$ -open sets and  $(D, S)$   $*$ -sets, Mathematica Moravica, Vol. 13-1, 29-36, 2009.
6. E. Ekici, S. Jafari and T. Noiri, On upper and lower contra-continuous multifunctions, Analele Stiintifice Ale Universitatii Al I. Cuza Din Iasi (S. N.), Matematica, 54(1), 75-85, 2008.
7. E. Ekici, On contra  $\pi g$ -continuous functions, Chaos, Solitons and Fractals, 35, 71-81, 2008.
8. E. Ekici, On almost and weak forms of nearly continuous multifunctions, Proceedings of the Jangjeon Mathematical Society, 9 (2), 109-120, 2006.
9. E. Ekici and T. Noiri, On a generalization of normal, almost normal and mildly normal spaces II, Filomat, 20: 2, 67-80, 2006.
10. N. Levine, Semi-open sets and semi-continuity in topological spaces, Amer. Math. Monthly, 70, 36-41, 1963.
11. N. V. Velicko, H-closed topological spaces, Amer. Math. Soc. Transl., 78, 103-118, 1968.

## A NEW CLOSED MAPPING

Burak Meral<sup>1</sup>, Erdal Ekici<sup>2</sup>

<sup>1</sup> CanakkaleOnsekiz Mart University, Graduate School of Natural and Applied Sciences,  
Department of Mathematics, TerzioğluCampus, Canakkale, TURKEY

<sup>2</sup> Corresponding Author: Department of Mathematics, CanakkaleOnsekiz Mart University,  
TerzioğluCampus, 17020, Canakkale, TURKEY

eekici@comu.edu.tr (prof.dr.erdalekici@gmail.com)

### Abstract

Weakly BR-closed functions were studied by Caldas et al. in 2009 [1]. Applications of weakly BR-closed functions were investigated by Caldas et al. in 2009. Also, Ekici considered generalized mappings for some investigations in 2011 [2]. In this study, a new closed mapping and investigations of this closed mapping are studied.

**Keywords:** Closed mapping, Closed set, Topology.

**Acknowledgement:** This work was supported by Çanakkale Onsekiz Mart University The Scientific Research Coordination Unit, Project number: FYL-2016-810.

This work is a part of Burak Meral's Master of Science Thesis.

### REFERENCES

1. M. Caldas, E. Ekici, S. Jafari and S. P. Moshokoa, On weakly BR-closed functions between topological spaces, *Mathematical Communications*, 14 (1), 67-73, 2009.
2. E. Ekici, Generalized hyperconnectedness, *Acta Mathematica Hungarica*, 133 (1-2), 140-147, 2011.
3. E. Ekici, On (LC, s)-continuous functions, *Chaos, Solitons and Fractals*, 38, 430-438, 2008.
4. E. Ekici, On e-open sets, DP\*-sets and DPE\*-sets and decompositions of continuity, *Arabian Journal for Science and Engineering*, Volume 33, Number 2A, 269-282, 2008.
5. E. Ekici and S. Jafari, On DS\*-sets and decompositions of continuous functions, *Filomat*, 22:2, 65-73, 2008.
6. E. Ekici and T. Noiri, On separation axioms and sequences, *Mathematica Moravica*, Vol. 11, 39-46, 2007.
7. E. Ekici and T. Noiri, On a generalization of normal, almost normal and mildly normal spaces II, *Filomat*, 20: 2, 67-80, 2006.
8. E. Ekici, Generalization of perfectly continuous, regular set-connected and clopen functions, *Acta Mathematica Hungarica*, 107 (3), 193-206, 2005.
9. E. Ekici, Nearly continuous multifunctions, *Acta Mathematica Universitatis Comenianae*, Vol. LXXII, 2, pp. 229-235, 2003.
10. A. S. Mashhour, M. E. Abd El-Monsef and S. N. El-Deep, On precontinuous and weak precontinuous mappings, *Proc. Math. Phys. Soc. Egypt*, 53, 47-53, 1982.
11. N. V. Velicko, H-closed topological spaces, *Amer. Math. Soc. Transl.*, 78, 103-118, 1968.

## THERMAL STABILITY AND ELASTIC PROPERTIES OF $Mg_3CuH_{0.6}$ TERNARY HYDRIDE

Said BOUCETTA, Boubaker OTHMANI

Laboratoire d'Elaboration de Nouveaux Matériaux et leurs Caractérisations (ENMC),  
Département de Physique, Université SETIF 1, 19000, Sétif, Algérie.

sd.boucetta@gmail.com

### Abstract

Theoretical study of thermal stability and elastic properties of a new intermetallic hydride compound  $Mg_3CuH_{0.6}$  have been carried out based on density functional theory (DFT), within local density approximation (LDA). The calculated structural parameter of  $Mg_3CuH_{0.6}$  compound is consistent with the experimental data. The calculated heat of formation shows that this compound has strongest alloying ability and structural stability. The elastic constants were determined from a linear fit of the calculated stress-strain function according to Hooke's law. From the elastic constants, the bulk modulus  $B$ , shear modulus  $G$ , Young's modulus  $E$ , Poisson's ratio  $\sigma$ , anisotropy factor  $A$  and the ratio  $B/G$  for  $Mg_3CuH_{0.6}$  compound are obtained. The sound velocities and Debye temperature are also predicted from elastic constants and discussed for the first report. This is the first quantitative theoretical prediction of these properties.

**Keywords:** Intermetallic hydride; Thermal stability; Elastic properties; DFT.

### References

1.C.X. Shi, J. Magnesium and Alloys, 1 (2013) 1.

# INVESTIGATION ON STRUCTURAL, ELASTIC AND THERMODYNAMIC PROPERTIES OF MgNi<sub>3</sub> INTERMETALLIC COMPOUND

Boubeker OTHMANI, Said BOUCETTA

Université Ferhat Abbas SETIF 1, Laboratoire d'Elaboration de Nouveaux Matériaux et leurs  
Caractérisations (ENMC), Département de Physique, 19000, Sétif, Algérie.

sd.boucetta@gmail.com

## Abstract

In this work, we have used the density functional theory (DFT) plane-wave pseudo potential method, with generalized gradient approximation (GGA) to investigate the structural, elastic, and thermodynamic properties of the intermetallic compound MgNi<sub>3</sub>. Comparison of the calculated equilibrium lattice constant and experimental data shows very good agreement. The elastic constants were determined from a linear fit of the calculated stress-strain function according to Hooke's law. From the elastic constants, the bulk modulus  $B$ , shear modulus  $G$ , Young's modulus  $E$ , Poisson's ratio  $\sigma$ , anisotropy factor  $A$ , and the ratio  $B/G$  for MgNi<sub>3</sub> compound are obtained. Our calculated elastic constants indicate that the ground state structure of MgNi<sub>3</sub> is mechanically stable. The calculation results show that this intermetallic crystal is stiff, elastically anisotropic and ductile material. The Debye temperature is also predicted from elastic constants. The temperature dependence of the enthalpy  $H$ , free energy  $F$ , entropy  $S$ , and heat capacity at constant volume  $C_v$  of MgNi<sub>3</sub> crystal in a quasi-harmonic approximation have been obtained from phonon density of states and discussed for the first report.

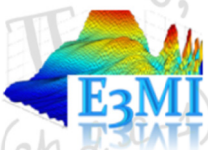
**Keywords:** MgNi<sub>3</sub>; Elastic properties; Thermodynamic properties; DFT

## References

1. C.X. Shi, J. Magnesium and Alloys, 1 (2013) 1.
2. K.U. Kainer, Magnesium-Alloys and Technology, Wiley-VCH, Weinheim, 2003.
3. M.D. Segall, P.J.D. Lindan, M.J. Probert, C.J. pickard, P.J. Hasnip, S.J. Clark, M.C. Payne, J. Phys. Condens. Matter 14 (2002) 2717.



**2<sup>nd</sup> INTERNATIONAL  
CONFERENCE ON  
COMPUTATIONAL  
MATHEMATICS AND  
ENGINEERING  
SCIENCES - CMES2017**  
*20-22 May 2017, Istanbul,  
TURKEY*



<https://cmes.sciencesconf.org>  
[cmes2017istanbul@gmail.com](mailto:cmes2017istanbul@gmail.com)